Formal Analysis and Run-time Monitoring of Information Flows in Chromium: Technical Appendix

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Formal Analysis and Run-time Monitoring of Information Flows in Chromium: Technical Appendix*

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1 Labels and Policies

We use labels to specify information flow policies. We first introduce the syntax of labels and operations on labels. Then, we discuss how these labels can be used to implement various policies present in browsers today.

1.1 Syntax of Labels

An information flow label, written \((S, I, D)\), is composed of a secrecy label \(S\), an integrity label \(I\), and a declassification label \(D\). The syntactic constructs used in defining labels are summarized below.

\[
\begin{align*}
\text{Label} & \quad \ell \quad ::= \quad (S, I, D) \\
\text{Simple Label} & \quad \kappa \quad ::= \quad (\sigma, \iota) \\
\text{Secrecy label} & \quad S \quad ::= \quad C(\sigma) \mid F(\sigma, \sigma) \\
\text{Secrecy tags} & \quad \sigma \quad ::= \quad \{s_1, \ldots, s_n\} \\
\text{Secrecy tag} & \quad s \quad ::= \quad \text{prin} \mid \text{url.prin} \mid \ast_u . \text{prin} \mid \dagger . \text{prin} \\
\text{Principal} & \quad \text{prin} \quad ::= \quad \text{id} . \text{ext} \mid \text{user} \mid \ast_p \\
\text{Integrity label} & \quad I \quad ::= \quad \{i_1, \ldots, i_m\} \\
\text{Integrity tag} & \quad i \quad ::= \quad \text{API} \\
\text{Declassification tags} & \quad D \quad ::= \quad \{d_1, \ldots, d_n\} \\
\text{Declassification tag} & \quad d \quad ::= \quad -s \mid +i \mid s \rightarrow s' \mid i \rightarrow i'
\end{align*}
\]

**Basic labels** The basic secrecy label is a set of secrecy tags \(\{s_1, \ldots, s_n\}\). Each secrecy tag represents an origin of a secret. We treat the hostname parts of URLs, extension IDs, and the user operating the browser (notated as the tag user) as origins. The integrity label is a set of integrity tags \(\{i_1, \ldots, i_m\}\). Each integrity tag represents the privilege to access a sensitive resource (namely, APIs). Even though these tags are reminiscent of permissions, our enforcement mechanism treats them in such a way that it can prevent the privilege escalation that commonly occurs in permission-based systems. The declassification label is a set of capabilities for endorsement \((+i)\), declassification \((-s)\), and reclassification \((s_1 \rightarrow s_2, i_1 \rightarrow i_2)\); we explain these later.

A simple label \(\kappa\) is a pair of a set of secrecy tags \(\sigma\) and a set of integrity tags \(\iota\).

Ignoring declassification, an entity labeled \((S_1, I_1, \{\})\) can send data to an entity labeled \((S_2, I_2, \{\})\) if \(S_1 \subseteq S_2\) (the destination is authorized for at least as many secrets as the source) and \(I_1 \supseteq I_2\) (the source has at least as many “permissions” as the destination).

For example, a DOM subtree that represents content loaded from ad.com would have a label that includes the secrecy tag \(ad\); APIs that allow extensions to access the browser’s local storage have labels that include a local Storage integrity tag. Data from a script labeled \(\{\{\text{cnn}, \text{ad}\}\}, \{\}, \{\}\) wouldn’t be allowed to flow to a DOM node labeled \(\{\{\text{cnn}\}, \{\}, \{\}\}\) because the latter is permitted fewer secrets (e.g., isn’t permitted secrets labeled ad).

**Floating labels** The basic secrecy label is too rigid to allow entities to adapt to the browser’s dynamic environment. E.g., the label of a DOM node on a cnn.com page might initially contain only a cnn secrecy tag to reflect that it contains information from cnn.com; after a password manager fills in a form field on the page, however, the label of the form field’s DOM node needs to change to reflect that it also contains information from another source.

We express the policy that allows dynamic tainting of an entity as a floating secrecy label. This is similar to JIF’s parametric labels. A floating secrecy label, written \(F(\sigma_1, \sigma_2)\), has two components: \(\sigma_1\) is the set of secrecy tags that the entity has at initialization time; \(\sigma_2\) is a ceiling (upper limit) of the secret that this entity can be tainted with. In other words, a secrecy label \(F(\sigma_1, \sigma_2)\) can float to \(F(\sigma_1', \sigma_2)\) as long as \(\sigma_1' \subseteq \sigma_2\).

This is useful when we want to prevent information from reaching an entity. For example, a floating secrecy label of the form \(F(\{\text{siteA}\}, \{\text{siteA}, \text{siteB}\})\) indicates that the labeled entity possesses siteA secrets and is willing to

---

1For brevity, we write ad instead of ad.com throughout.
receive siteB secrets. Its label will then change to $F(\{\text{siteA, siteB}\}, \{\text{siteA, siteB}\})$, continuing to protect the siteB secret. To clearly distinguish floating labels from ordinary ones, we henceforth write non-floating secrecy labels as, e.g., $C(\{\text{siteA}\})$.

**Compound labels** Going back to the password example, the password field is owned by cnn.com, but can be written to by the user or an extension. We would want both labels, as both secrets are involved, but we may want to maintain the notion of a primary owner, for purposes that we will shortly show. To this end, we introduce dot-separated compound tags: $s_1.s_2$ indicates that $s_1$ is the primary owner of the data.

Returning to our example, the secrecy tag cnn.user would be part of the label of a DOM node originally loaded from cnn.com (hence cnn) at the user’s behest (hence user), e.g., if the tab was opened and the URL typed in by the user. More concretely, nodes in the DOM of the cnn.com page would initially be labeled with the secrecy tag $F(\{\text{user}\}, \{\text{user}\})$; the $\{\text{user}\}$ ceiling indicates that it is OK for the node to be tainted (repeatedly) with secrets of all entities whose secrecy label has the form $\{\text{user}\}$. In contrast, $F(\{\text{pwdMgr}\}, \{\text{pwdMgr}\})$ means that an entity with that label can be tainted exactly once, e.g., to $F(\{\text{pwdMgr}\}, \{\text{user}\})$. This label is suitable for content scripts, which are injected into multiple pages, but any script instance is injected into exactly one page.

One purpose for compound labels is to allow labels to reflect which entities influenced the content, while retaining the ability to leave a specific entity in control of the content. For example, we may choose to allow requests to send requests to cnn.com only if they are compatible with the destination label $(C(\{\text{cnn}\}), \{\text{network}\}, \{\text{pwd\_mgr}\})$, which concisely expresses the policy that only cnn.com pages are allowed to make requests to cnn.com, and that they can do so even if their content has absorbed input from the user or other entities (e.g., they include a secrecy tag like cnn.user). Similar policies can be expressed with declassification, which we discuss next.

**Declassification, reclassification, and endorsement** Declassification and endorsement capabilities allow an entity (e.g., an extension core) to circumvent constraints that it would otherwise incur because of its secrecy and integrity tags. Declassification is a powerful (and dangerous) operation, and declassification capabilities should be granted to entities only judiciously. At the same time, declassification is necessary, since some extensions, like the password manager, collect many secrets, yet their functionality requires that they (selectively) copy those secrets into arbitrary web pages.

In our password manager example, the ext.pwdMgr core has the $-\ast .\text{ext\_pwd}$ capability. This is to ensure that no matter how many secrecy tags like someSite.\text{ext\_pwd} it accumulates in its secrecy label as a result of saving passwords, it is still able to send data (passwords) to individual web pages (e.g., cnn.com). Without declassification, those secrecy tags in ext.pwdMgr’s label would normally cause the label check to fail, since the same tags are not present in cnn.com’s secrecy tag, including its ceiling. Declassification (and reclassification and endorsement) are used only when a label check would otherwise fail; they don’t affect an entity’s secrecy and integrity tags beyond the label check.

Reclassification is a weaker form of declassification: the $s_1 \rightarrow s_2$ reclassification tag indicates that a secrecy tag $s_1$ can be converted (for the purpose of a label check) to a secrecy tag $s_2$.

Endorsement tags are similar to declassification tags. To protect the local storage API, we give the API the integrity label $\{\text{localStorage}\}$; only entities that have localStorage in their integrity label, or can add it via endorsement, can use it. Hence, we give the ext.pwdMgr core the $+\text{localStorage}$ capability, allowing it to elevate its privileges sufficiently to use the local storage API is needed. As with de- and reclassification, endorsement only enables a label check to succeed, and has no persistent effect on the integrity tags in a label.

### 1.2 Basic Label Operations

Our enforcement mechanism uses a set of label operations to compute labels for components and make policy decisions.
computes the largest set of secret tags that a component with \( \ell \) labels of Definition 1 (Label order) receive data from. The partial order over simple labels is defined as follows:

\[
\text{Simple labels form a lattice } (L, \sqsubseteq), \text{ where } L \text{ is a set of simple labels and } \sqsubseteq \text{ is a partial order over simple labels.}
\]

Intuitively, the more secrecy tags a component has, the more secrets it can gather, and the fewer components it can send data to. The fewer integrity tags a component has, the fewer APIs it can access, and the more components it can receive data from. The partial order over simple labels is defined as follows:

**Definition 1** (Label order). \((\sigma_1, t_1) \sqsubseteq (\sigma_2, t_2) \iff \forall s \in \sigma_1, \exists s' \in \sigma_2 \text{ s.t. } s \leq s' \text{ and } t_2 \sqsubseteq t_1.\)

For integrity labels, we can do a simple subset comparison. For secrecy tags we use another relation, \(s_1 \leq s_2\), to compare individual tags. It is defined as follows:

\[
s_1 \leq s_2 \text{ if } \begin{cases} 
  s_1 = s_2 \\
  s_1 = \text{url and } s_2 \in \{u, t\} \\
  s_1 = \text{prin and } s_2 = *p \\
  s_2 = a.s.b \text{ and } s_1 \leq s_a \\
  s_1 = a.s.b, s_2 = a', s'_b, s_a \leq s'_a \text{ and } s_b \leq s'_b
\end{cases}
\]

The \(\leq\) relation is reflexive. The wildcard is higher than a concrete label. \(s_a\) is lower than the compound label \(a.s.b\). We do not include a rule for \(s_b \leq a.s.b\), because a component with label \(s_b\) may generate information independent of \(s_a\).

Assume that component A has label \(\ell_A\) and B has \(\ell_B\). Each time information flows from component A to B, our enforcement mechanism checks whether B’s label allows B to learn all the secrets A knows. Formally: \(\ell_A^\sim \sqsubseteq \ell_B^\ast\). If the check succeeds, B’s label is updated to \(\ell_A^\sim \triangleright \text{tnt} \ell_B\).

Our enforcement mechanism checks labels before web requests or data are sent to remote servers. We define \(\text{NetDeclassify}(\kappa, \text{url})\) to decide whether data (web requests) with label \((\sigma, t)\) can be sent to url as follows.

\[
\text{NetDeclassify}((\sigma, t), \text{url}) = \begin{cases} 
  \text{allowed} \quad & \text{if } \forall s \in \sigma, s = \text{url}, s' \text{ or url} \\
  \text{disallowed} \quad & \text{otherwise}
\end{cases}
\]

Declassification capabilities are exercised when components make API calls. We define \(\ell \Rightarrow \kappa\) to mean that by raising or declassifying \(\ell\) we can obtain \(\kappa\).
A webpage is composed of components from different origins. Each component comes with its own information flow policy. For instance, an extension’s content script’s policy is specified in the manifest file of that extension. When the content script is injected into a page, the hosting page has its own information flow policies, which may include policies regarding allowed information flows between the injected script and its surrounding environment. This is where policy composition is necessary.

There are two situations where such policy composition needs to be considered: (1) a host webpage includes external resources such as scripts (including content scripts from extensions) and images; and (2) a host page embeds another page in an iframe or an extension injects an iframe into a host page.

As there are multiple ways to compose policies, we provide a notion of generalized CSP (GCSP), which allows a page to specify how to compose the page’s policy with that of the external resources. Here, external resources include both page resources and content scripts. We provide four pre-defined composition operations: (1) allow flows allowed by either policy, (2) the page’s policy overrides the external resource’s policy, (3) the external resource’s policy overrides the page’s policy, and (4) allow flows allowed by both policies.

1.3 Label Composition

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GCSP Syntax Each generalized CSP item, denoted $\chi$, maps a principal to a pair of an integrity policy and a natural number indicating which composition rules to use to compute the secrecy label. Below are the definitions.

\[
\begin{align*}
\text{Integrity Pol} & \quad \omega ::= \cdot | \text{IF}(API_1, \ldots, API_n) \\
\text{GCSP} & \quad \chi ::= \cdot | \chi, \text{prim} \mapsto (\omega, n)
\end{align*}
\]

GCSP uses a natural number to index the compositions. (1) simply takes the union of the secrecy labels, and thus allows the content script to learn the secrets of the DOM and secrets allowed in its manifest file. (2) allows the DOM’s policy to override the extension’s policy. (3) allows extension’s policy to override the DOM’s policy. (4) is a strict composition policy that takes the intersection of the policies. If the intersection is empty, we do not inject the script.

The integrity policy is used to specify which interfaces the external scripts can have access to. The effect of $\text{IF}(APIs)$ is that the external script has the API names in $APIs$ in its integrity label. This allows the script to access the APIs, but prevents the script from receiving any data from a component that cannot access these APIs. Therefore, we prevent privilege escalation. The effect of $\text{IFD}(APIs)$ is that the external script has the endorsement of API names in $APIs$ in its declassification label. This is closer to having the permission to access the APIs. Using endorsement capabilities, the external script can launder data for other components.
Label composition functions

Next we formally define the two label composition functions, one for page resources such as content scripts, page scripts, and images; and the other for iframe'd pages.

\(\text{computeResLab}(url, \kappa_d, \chi, \ell, \text{prin})\) Computes an external resource’s label based on \(url, \kappa_d, \chi,\) and \(\ell\). \(url, \kappa_d,\) and \(\chi\) are the host page/document’s URL, simple label, and GCS, respectively. If the external resource is a content script, \(\ell\) denotes the content script’s initial label. If the external resource is an image or other object loaded from an external URL, \(\ell\) is the resource label computed from its URL.

The function \(\text{computeResLab}(url, \kappa_d, \chi, \ell)\) works as follows. Suppose \(\kappa_d = (\sigma_d, I_d)\) and \(\ell = (F(\sigma_1, \sigma_2), I, D)\). Let \((\omega, n)\) denote the composition policy for \(\text{prin}\) based on \(\chi\). The function computes a secrecy label \(\sigma'\) using \(\text{computeResLab}_{S_n}(url, \sigma_d, F(\sigma_1, \sigma_2))\), an integrity label \(I'\) using \(\text{computeResLab}_{I_d}(\omega, I)\), and an endorsement label \(D'\) using \(\text{computeResLab}_{D_n}(\omega, D)\). The function outputs a label \(\ell' = (\sigma', I', D')\).

Before defining \(\text{computeResLab}_{S_n}(url, \sigma_d, F(\sigma_1, \sigma_2))\), we define an operation that instantiates the secrecy label of a content script to a specific URL. If the external resource is a content script, its initial label will contain some \(\dagger, s\) tags. For a secrecy tag with the form \(\dagger, s\), the operation \(url \succ \dagger, s\) instantiates \(\dagger, s\) to \(url, s\). For a secrecy tag that does not contain \(\dagger\), \(url \succ s\) is still \(s\).

\[
url \succ s = \begin{cases} 
url, s' & \text{if } s = \dagger, s' \\
\phantom{url,} s & \text{otherwise}
\end{cases}
\]

In the following, we define the function \(\text{computeResLab}_{S_n}(url, \sigma_d, F(\sigma_1, \sigma_2))\).

- Allowed by either \(\text{computeResLab}_{S_1}(url, \sigma_d, F(\sigma_1, \sigma_2)) = F(\sigma_1, \sigma_d \cup (url \succ \sigma_2))\)
- Allowed by CS’s manifest \(\text{computeResLab}_{S_2}(url, \sigma_d, \sigma) = url \succ \sigma\)
- Allowed by DOM’s label \(\text{computeResLab}_{S_3}(url, \sigma_d, F(\sigma_1, \sigma_2)) = F(\cdot, \sigma_d)\)
- Stricter of CS and DOM \(\text{computeResLab}_{S_4}(url, \sigma_d, F(\sigma_1, \sigma_2)) = F(\sigma_1 \cap \sigma_d, \sigma_d \cap (url \succ \sigma_2))\)

Then we define the function \(\text{computeResLab}_{I_d}(\omega, I)\), where \(\omega = (\text{IF}(\tau_1), \text{IFD}(\tau_2)) = (\text{IF}(API_{a_1}, \cdots, API_{a_n}), \text{IFD}(API_{b_1}, \cdots, API_{b_n}))\).

- Allowed by either \(\text{computeResLab}_{I_1}(\omega, I) = \text{IF}(\tau_1) \cup I\)
- Allowed by CS’s manifest \(\text{computeResLab}_{I_2}(\omega, I) = I\)
- Allowed by DOM’s label \(\text{computeResLab}_{I_3}(\omega, I) = \text{IF}(\tau_1)\)
- Stricter of CS and DOM \(\text{computeResLab}_{I_4}(\omega, I) = \text{IF}(\tau_1) \cap I\)

Last, we define the function \(\text{computeResLab}_{D_n}(\omega, D)\), where \(\omega\) is decomposed as above. We write \(+\iota\) to denote the set of endorsement capabilities obtained from the set of integrity tags \(\iota\).

- Allowed by either \(\text{computeResLab}_{D_1}(\omega, D) = \text{IFD}(\tau_2) \cup D\)
- Allowed by CS’s manifest \(\text{computeResLab}_{D_2}(\omega, D) = D\)
- Allowed by DOM’s label \(\text{computeResLab}_{D_3}(\omega, D) = \text{IFD}(\tau_2)\)
- Stricter of CS and DOM \(\text{computeResLab}_{D_4}(\omega, D) = \text{IFD}(\tau_2) \cap D\)

\(\text{computeFrameLab}(\ell_1, \ell_2, \chi, \text{prin})\) Computing a framed page’s label based on the frame’s policy and the page’s policy. The label composition functions for iframe’d pages are similar. Unlike content scripts, the label does not need to be instantiated by the host page’s URL; and therefore the composition function takes the label of the iframe and the label of the embedded page as inputs.

Suppose \(\ell_1 = (F(\sigma_1, \sigma_2), I_1, D_1), \ell_2 = (F(\sigma_a, \sigma_b), I_2, D_2)\), then
Browsers currently implement many security policies. Some of these policies are clearly about information flow and map cleanly to our framework; for others the mapping is less clear. We next revisit several such policies, examining to what extent they map into a framework like ours, as well whether the framework’s expressiveness allows richer or more powerful variants of the policies to be stated and enforced.

**Same-origin policy** Browsers use the same-origin policy (SOP) to manage access to different origins. Origins are usually defined as the tuple (scheme, host, port). Scripts from one origin cannot read content from another origin (e.g., via XMLHttpRequest). Thus, a page from login.a.com cannot access a page from cnn.com.

The definition of $\text{computeResLab}_{D_a}(\omega, D)$ is the same as $\text{computeResLab}_{D_a}(\omega, D)$.

### 1.4 Policies

Browsers currently implement many security policies. Some of these policies are clearly about information flow and map cleanly to our framework; for others the mapping is less clear. We next revisit several such policies, examining to what extent they map into a framework like ours, as well whether the framework’s expressiveness allows richer or more powerful variants of the policies to be stated and enforced.

**Domain relaxation** A page can set its `document.domain` value to a suffix of its current domain, allowing pages with different prefixes of the same hostname to communicate. E.g., a page from login.a.com and a page profile.a.com can both set their domain to a.com, at which point their origins will be considered the same, and the pages will be allowed to access each other’s DOM.

Domain relaxation can be implemented in our framework in several ways. One is for profile.a.com to have the secrecy tag $F(\{\text{profile.a.com}\}, \{\text{profile.a.com}, \text{login.a.com}\})$, which allows it to receive secrets from login.a.com; and for login.a.com to have a corresponding secrecy label.

2 All our hostname-based tags include the scheme and port, though we generally elide this for clarity.
Another option is to give each page the $name.a.com \rightarrow a.com$ reclassification capability. This would allow such pages to talk to $a.com$, but not yet to each other (because we currently apply reclassification only if necessary to complete a request, and only on the source entity). To accomplish that, their respective secrecy tags $name.a.com$ would additionally need to be replaced with $a.com$, which could be accomplished by the browser crawling over the page’s DOM and changing the secrecy tags of any nodes with the appropriate labels from $name.a.com$ to $a.com$.

**CSP** A CSP allows a page to specify from where page resources (e.g., 3rd-party scripts) can be loaded. The policy applies to images, scripts, etc. CSPs can be broadly interpreted as policies that a host page sets to constraint the information flow between the host page and remote servers from which external resources originate. When the request (e.g., HTTP GET) is sent to a remote server, information flows from the browser to the remote server. The host page can send arbitrary information to the remote server in this way by, e.g., embedding it in the URL string of the HTTP GET request. Once loaded, external resources such as scripts can interact with the rest of the page as well as with remote servers. Our generalized CSP (GCSP) (Section 1.3) can be used to specify the above-mentioned information-flow constraints present in CSPs.

There are two main differences between our GCSP and the existing CSP. First, the existing CSP takes effect only at resource-loading time and does not constrain transitive information flows. E.g., if $url$’s CSP forbids scripts from $ad.com$, it doesn’t mean that an extension’s content script running in the same page is prevented from sending to or receiving information from $ad.com$. GCSP enforces a stricter policy: Any information tagged with a $url$ secrecy tag cannot be sent to components that do not have that tag. Second, CSPs also enforce policies other than information flow. For instance, not loading resources from an external resource also prevents the external resource from using local resources such as the screen or CPU. This will effectively protect the user from seeing offensive ads, prevent scripts from draining the laptop battery, etc.

In modern browsers, web pages are allowed to embed third-party content with little restriction. Our modified browser has stricter constraints. To allow web pages to load third-party content, we explicitly enable two-way communication between the page and the external resources.

**postMessage** postMessage is a JavaScript API which allows web pages to communicate across domains on the client side. postMessage works in two conditions: A parent page embeds another page in an iframe or a parent page opens another page in a new tab. In both cases, the API allows two-way communication. The postMessage send needs to specify the destination, and the receiver can check the source.

To allow communications using postMessage APIs in our system, the sender and receiver’s labels need to be adjusted. If a host page were to send data directly to an iframe from a different origin, the request would be denied by our browser. To allow postMessages to work, labels are assigned to the host and iframed page in similar ways as discussed for SOP and CSP.

**iframe policies** iframes were introduced as an isolation mechanism for a parent page to confine untrusted pages. However, iframes have been abused to embed trusted pages within malicious pages, which then mount phishing and clickjacking attacks.

To prevent such attacks, a server can specify, using the X-Frame-Options header, that the page should not be rendered inside a iframe, or should only be rendered inside an iframe of a page from a specified origin.

In a pure information-flow approach, disallowing a page from loading in an iframe cannot easily be done. We can, however, prevent the parent from gaining information from a loaded iframe. For example, if $a.com$ tries to place $victim.com$ in an iframe on its page and receive information from the iframe, it would have to have a secrecy label that can float to include $victim.com$’s secrets. To prevent $a.com$ from having a label that allows this, the browser would have to generate $a.com$’s label from something other than $a.com$’s (self-supplied) CSP. While such restrictions could be expressed cleanly in our framework using composition operators (Section 1.3), we have not yet explored this approach.
Extension host permissions  Extensions specify host permissions in its configuration files to ask for permissions to access different pages. The browser matches the URL in the host permissions and the URL of the page to decide whether to inject the script. Our label system can enforce the host permission checking. The label for the content script is formed as \( F(\{\text{extension}\}, \{\text{extension, host, permission}\}) \). When the script is going to be injected, the label check happens and verifies whether the extension is allowed to access the page. We can even do better for blocking information leakage if we use the stricter label composition, in which case if the page is tainted with information from other domains, the content script cannot collect information from other domains.

Extension API permissions  Extensions can access some browser APIs if they declare these APIs in the configuration file.

We use integrity labels for controlling access to APIs, which also guards against privilege escalation. If an extension has access to one API, the API will be included in its integrity label, and when information is about to flow from the extension to another party, our system will compare the labels to make sure that the information does not flow to a party which does not have access to that API.

2 System States

Scripts  Executable code present in browser extensions as well as webpages is abstractly represented as commands, denoted \( cmd \). We model basic script functionality including updating variables, making function and API calls, and branching on conditions.

\[
\begin{align*}
\text{Command} & \quad \text{cmd} \quad ::= \\
& \quad \text{skip} \mid \text{ret \ exp} \mid x := \exp \mid API_a(\vec{\exp}) \mid \text{let } x = f(\exp) \text{ in cmd} \\
& \quad \mid \text{let } x = API_s(\vec{\exp}) \text{ in cmd} \mid \text{cmd}_1; \text{cmd}_2 \mid \text{if } \exp \text{ then } \text{cmd}_1 \text{ else } \text{cmd}_2
\end{align*}
\]

\[
\begin{align*}
\text{Expression} & \quad \exp \quad ::= \\
& \quad x \mid c \mid \exp_1 \text{ bop } \exp_2 \mid \text{uop } \exp \mid (\exp_1, \cdots, \exp_n)
\end{align*}
\]

\[
\begin{align*}
\text{Function decl} & \quad f\text{decl} \quad ::= f(x) = \text{cmd} \mid x.\text{cmd} \\
\text{Variable Env} & \quad \Gamma \quad ::= \cdot \mid \Gamma, x \mapsto v
\end{align*}
\]

API calls include label checking. Asynchronous API calls are treated as a command \( API_a(\vec{\exp}) \). Synchronous API calls, denoted let \( x = API_s(\vec{\exp}) \) in \( cmd \), block for return values.

Events and event handlers  The syntax of events and event handlers is summarized below. We write \( e \) to denote an event, \( E \) to denote an event queue, \( \text{EventHandler} \) to denote an event handler, and \( \text{EventHandlers} \) to denote a set of event handlers.

\[
\begin{align*}
\text{Event} & \quad e \quad ::= \quad (id_e, \text{eventType}, \text{return}, \text{info}, \kappa) \\
\text{Event Queue} & \quad E \quad ::= \quad \cdot \mid E++ e \\
\text{Return channel} & \quad \text{return} \quad ::= \quad \text{none} \mid \text{some} \text{(asyncRet, id)} \mid \text{some(e, id)} \\
\text{Event handlers} & \quad \text{EventHandlers} \quad ::= \quad \cdot \mid \text{EventHandlers, EventHandler} \\
\text{Event handler} & \quad \text{EventHandler} \quad ::= \quad (id, \text{eventType}, x.\text{cmd}, E, \text{BlockingFlag}, \text{cmd}, id_e, \text{return}) \\
\text{Blocking flag} & \quad \text{BlockingFlag} \quad ::= \quad \text{blocking} \mid \text{nonblocking}
\end{align*}
\]

An event is a tuple consisting of a unique event ID (\( id_e \)), an event type (\( \text{eventType} \)), whether actions are needed after the event is processed (\( \text{return} \)), additional arguments of the event (\( \text{info} \)), and the information flow label for the event (\( \kappa \)). \( \text{eventType} \) should contain sufficient information for dispatching an event. For instance, the \( \text{eventType} \) for a button onClick event is \text{button1.onclick} and the \( \text{eventType} \) for a tab onCreated event is \text{tabs.onCreated}. \( \text{return} \) is either none indicating when the event handler for that event finishes, no action needs to be taken; or \text{some} (asyncRet, id) indicating this event is generated in relation to an asynchronous call, and when its event handler finishes
processing, the event handler need to invoke a callback function specified by \( id \). \( \some(e, id) \) is only used by event handlers and is explained later.

There are two kinds of events in terms of processing modes, namely, blocking events and non-blocking events. For blocking events, event handlers can register to run in blocking mode. The browser finishes processing a blocking event only when all its handlers in blocking mode have been executed. For non-blocking events, handlers cannot run in blocking mode. After dispatching a non-blocking event, the browser can move to the next step without executing all the event handlers. Note that we don’t introduce an index to indicate whether an event is blocking or non-blocking. Only the events with certain event types are blocking events, e.g., \( \text{webRequest.onBeforeRequest} \) events. Given an event, from its type, we can tell whether it is a blocking event. The return channel for an event handler can be \( \some(e, id) \) when the event handler is a blocking event handler, processing event \( e \) with a unique ID \( id \).

An event handler has its own unique ID, the type of event that it processes, and the code for processing events \( (x.cmd) \). An event handler can only process one event at a time; events waiting to be processed are stored in an event queue \( \mathcal{E} \). The \( \text{BlockingFlag} \) indicates whether a handler is a blocking event handler. The last three fields in the event handler are the script processing the current event, the ID of the event being processed, and the return information of the event being processed. For page script handlers, \( id \) is the node ID of the corresponding script node.

### Extensions

An extension is a tuple consisting of: a unique ID, one extension core, several content scripts, local storage, an active flag, and a policy label. A static extension core is a tuple consisting of a variable environment \( \Gamma \), commands \( cmd \) corresponding to the main function of the core, and a list of event handlers. A content script contains three identifiers (the ID of the extension it belongs to, its own unique ID, and the ID of the tab in which it runs); programs modeled as \( \Gamma, cmd, \\text{EventHandlers} \); an index \( \text{runat} \) for indicating when to inject the script to a tab; and a policy label. The active flag \( a\text{Flag} \) indicates whether an extension is active.

\[
\begin{align*}
\text{Installed extension} & \quad \text{Ext} \quad ::= \quad (id_{ext}, \text{ExtCore}, \text{ExtCSs}, \text{Storage}, a\text{Flag}, \ell) \\
\text{Content scripts} & \quad \text{ExtCSs} \quad ::= \quad \cdot | \text{ExtCSs}, \text{ExtCS} \\
\text{Content script} & \quad \text{ExtCS} \quad ::= \quad (id_{ext}, id_{cs}, id_{t}, \Gamma, cmd, \text{EventHandlers}, \text{runat}, \ell) \\
\text{Injection time tag} & \quad \text{runat} \quad ::= \quad \text{DocBegin} | \text{DocEnd} | \text{DocIdle} \\
\text{Extension core} & \quad \text{ExtCore} \quad ::= \quad (\Gamma, cmd, \text{EventHandlers}) \\
\text{Ext active setting} & \quad a\text{Flag} \quad ::= \quad \text{active} | \text{inactive} \\
\text{Storage} & \quad \text{Storage} \quad ::= \quad \text{objects}, \ell \\
\text{Objects} & \quad \text{objects} \quad ::= \quad \cdot | \text{objects}, \text{object} \\
\text{Object} & \quad \text{object} \quad ::= \quad (id, \text{content}) \\
\text{Installed extensions} & \quad \text{Exts} \quad ::= \quad \cdot | \text{Ext} :: \text{Exts}
\end{align*}
\]

### Simplified DOM

We model the main page and the iframed subpages contained in a browser tab as a list of documents \( \text{Docs} \). A document \( \text{Doc} \) is defined as \( (id_{d}, \text{url}, \text{nodes}, \text{DocCSs}, \chi, \ell) \). \( id_{d} \) is the document ID. \( \text{url} \) is the page URL. \( \text{nodes} \) denotes the page elements. \( \text{DocCSs} \) are the content scripts injected by extensions. \( \chi \) denotes the content security policies of the page. Each document is associated with a policy label.

A page consists of many elements, e.g., images, scripts, forms, etc. In the Document Object Model (DOM), the elements in a page are organized in a tree structure. Our model inherits the tree structure from the DOM. The elements in a page are modeled as tree nodes in a document. A node is defined as \( (id, \text{attributes}, \text{nodes}, \text{content}, \ell) \). \( id \) denotes the node ID. \( \text{attributes} \) contains general information about the node, e.g., the content type, the URL (if the node loads external object), and the parent node ID, etc. If the node is a script node, \( \text{attributes} \) also contains the script’s event handlers’ IDs. \( \text{nodes} \) are the child nodes. \( \text{content} \) is a piece of data with a specific format, e.g., an image file. \( \ell \) is the policy label attached on the node.
Documents  Docs ::= · | Docs, Doc
Document    Doc ::= (id, url, nodes, DocCSs, χ, ℓ)
Node        node ::= (id, attributes, nodes, content, ℓ)
Nodes       nodes ::= · | nodes, node
Attributes  attributes ::= (type, url, · · ·)
Content Type type ::= stylesheet | script | image | · · ·

Bookmarks   Like the DOM, bookmarks have a tree structure. Operations on bookmarks include insertion, deletion, and mutation of nodes and subtrees. As with the DOM, we could allow each node to be tainted with the label of the entity that updates the data structure. The drawback is that to prevent information leakage, many simple operations would be prohibited. For instance, if a script with many secrets wrote to the root of the bookmark tree, then no entities that are allowed fewer secrets could read any bookmark. Since bookmarks have a long life cycle, this is too prohibitive. Instead, we borrow ideas from multi-level secure execution. We implement a multi-level bookmark MBookmarks data structure, consisting of a set of pairs of a bookmark bookmark and a simple label κ. The label indicates the secrecy and integrity level of the bookmark. A bookmark is a tree: each leaf node is a bookmark entry and each non-leaf node represents a directory.

Multi-level bookmarks MBookmarks ::= · | MBookmarks, MBookmark
Bookmarks   MBookmark ::= bookmarks, κ
Bookmarks   bookmarks ::= · | bookmarks, bookmark
Bookmark    bookmark ::= (id, title, bookmarks | id, title, url)

Cookies     Cookies are similar to bookmarks in that they are long lived; tainting them would interfere with normal functionality. Hence, we label each with a simple label κ. For cookies, the label corresponds to the cookie’s domain, so web sites can set and retrieve their cookies, which is the main functionality needed of cookies. To operate on cookies, an entity needs to be able to reclassify to the secrecy label of a cookie’s domain, which is consistent with having the ability to access content from that domain.

Cookies    Cookies ::= · | Cookies, Cookie
Cookie      Cookie ::= (name, value, url, κ)

Histories   History entries have simple labels as well. Each history item history has the secrecy and integrity label of the entity that caused the history entry to be created. When querying history, an entity with label ℓ is given results composed of entries whose label is lower than or equal to ℓ. When deleting history entries, only entries with label equal to or higher than ℓ are removed.

Histories  histories ::= · | histories, history
History     history ::= (id, url, name, visitTime, visitType, κ)

Runtime extension instances When an extension core injects a content script using API chrome.tabs.executeScript, the injected script may not run right away. Instead, it is stored in progInjCSs. DocCSs is the list of active content scripts. idr is the unique identifier for that runtime instance. The runtime instance of an extension core is denoted ExtCoreR.

Injected content scripts progInjCSs ::= · | progInjCSs, ExtCS
Doc content scripts DocCSs ::= · | DocCSs, DocCS
Doc content script DocCS ::= (idext, idcs, idr, Γ, cmd, EventHandlers, ℓ)
Runtime Core ExtCoreR ::= idext, ExtCore, ℓ
Extension cores ExtCoreRs ::= · | ExtCoreRs, ExtCoreR
**Browser state**  The top-level system state $\Sigma$ contains tabs in the browser (Tabs), run-time extension cores (ExtCoreRs), static copies of programmatically injected content scripts (progInjCSs) installed extensions (Exts), cookies (Cookies), bookmarks (MBookmarks), histories (histories), and user actions (UI).

$$\Sigma := (\Psi, \text{Tabs, ExtCoreRs, progInjCSs, Exts, Cookies, MBookmarks, histories, UI})$$

**Async Call Browser States**  For an asynchronous API call, a corresponding asynchronous call state ayncRet is generated. With these states, we know whether a blocking event has been processed by all the matching block-state.

**Evalution contexts**  We first define script variable context environments as follows.

<table>
<thead>
<tr>
<th>Docs script env</th>
<th>DocsEnv(id) ::=</th>
<th>Docs :: DocsEnv(id)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Doc script env</td>
<td>DocEnv(id) ::=</td>
<td>id, url, DocEnv(id), EextCSs, Q</td>
</tr>
<tr>
<td>Node script env</td>
<td>nodeEnv(id) ::=</td>
<td>id, attributes, nodes, content, Q, Q</td>
</tr>
<tr>
<td>Nodes script env</td>
<td>nodeEnv(id) ::=</td>
<td>nodes :: nodeEnv(id)</td>
</tr>
</tbody>
</table>
These contexts include a hole \( \Box \) in the place of the variable environments (\( \Gamma \)). The purpose of the variable context is to identify such \( \Gamma \)'s so values of variables can be looked up and the environment itself can be updated.

We define the execution contexts, which contain a hole \( \Box \) indicating the position of the current evaluation.

\[
\begin{align*}
\text{State context} & : \quad \Sigma_{\text{ctx}}(id) \\
& ::= \Psi, \text{Tabs}_{\text{ctx}}(id), \text{ExtCoreRs}_{\text{ctx}}(id), \text{ExtCSs}_{\text{ctx}}(id), \text{Exts}_{\text{ctx}}(id), \text{Cookies}, \text{Histories} \\
& \quad \mid \Psi, \text{Tabs}, \text{ExtCoreRs}_{\text{ctx}}(id), \text{ExtCSs}_{\text{ctx}}(id), \text{Exts}, \text{Cookies}, \text{Histories} \\
\text{Tabs context} & : \quad \text{Tabs}_{\text{ctx}}(id) \\
& ::= \cdot \mid \text{Tabs} :: \text{Tabs}_{\text{ctx}}(id) \\
\text{Tab context} & : \quad \text{Tab}_{\text{ctx}}(id) \\
& ::= \text{id}, \text{Doc}_{\text{ctx}}(id), \text{url}, \text{EventHandlers}, \ell \\
& \quad \mid \text{id}, \text{Doc}_{\text{ctx}}(id), \text{url}, \text{EventHandlers}_{\text{ctx}}(id), \ell \\
\text{Doc content scripts context} & : \quad \text{DocCS}_{\text{ctx}}(id) \\
& ::= \cdot \mid \text{DocCS} :: \text{DocCS}_{\text{ctx}}(id) \\
\text{Doc content script context} & : \quad \text{DocCS}_{\text{ctx}}(id) \\
& ::= \text{id}_{\text{ext}}, \text{id}_{\text{cs}}, \text{id}, \cdot \mid \text{cmd}_{\text{ctx}}, \text{EventHandlers}, \ell \\
& \quad \mid \text{id}_{\text{ext}}, \text{id}_{\text{cs}}, \text{id}, \cdot \mid \text{cmd}, \text{EventHandlers}_{\text{ctx}}(id), \ell \\
\text{Docs context} & : \quad \text{Docs}_{\text{ctx}}(id) \\
& ::= \cdot \mid \text{Docs} :: \text{Docs}_{\text{ctx}}(id) \\
\text{Doc context} & : \quad \text{Doc}_{\text{ctx}}(id) \\
& ::= \text{id}, \text{url}, \text{nodes}, \text{DocCS}_{\text{ctx}}(id), \ell \\
\text{Event handlers context} & : \quad \text{EventHandlers}_{\text{ctx}}(id) \\
& ::= \cdot \mid \text{EventHandlers} :: \text{EventHandlers}_{\text{ctx}}(id) \\
\text{Event handler context} & : \quad \text{EventHandlers}_{\text{ctx}}(id) \\
& ::= \text{id}, \text{eventType}, \text{x.cmd}, \text{E}, \text{cmd}_{\text{ctx}}, \text{id}, \text{BlockingFlag}, \text{return} \\
\text{Extension cores context} & : \quad \text{ExtCoreRs}_{\text{ctx}}(id) \\
& ::= \cdot \mid \text{ExtCoreRs} :: \text{ExtCoreRs}_{\text{ctx}}(id) \\
\text{Extension core context} & : \quad \text{ExtCoreRs}_{\text{ctx}}(id) \\
& ::= \text{id}_{\text{ext}}, \text{cmd}_{\text{ctx}}, \text{EventHandlers}, \ell \\
& \quad \mid \text{id}_{\text{ext}}, \text{cmd}, \text{EventHandlers}_{\text{ctx}}(id), \ell \\
\text{Command context} & : \quad \text{cmd}_{\text{ctx}} \\
& ::= \cdot \mid \text{let} \text{x} = \cdot \mid \text{in} \text{cmd} | \text{cmd}_{\text{ctx}}; \text{cmd} \\
\text{UI context} & : \quad \text{UI}_{\text{ctx}}(\text{user}) \\
& ::= \text{user}, \text{cmd}, \text{cmd}_{\text{ctx}}, \ell
\end{align*}
\]

We write \( \Sigma_{\text{ctx}} \mid x \Box_{\text{ctx}}(\text{id}) \) to denote the state resulting from plugging construct \( x \) into context \( \Sigma_{\text{ctx}}(\text{id}) \). In terms of script context, we plug in two constructs, \( \Sigma_{\text{ctx}} \mid \Gamma \Box_{\text{ctx}}(\text{id}) \), where \( \Gamma \) is the context that maps global variables to their values. We define a function \( \text{ctxOfId}(\Sigma, \text{id}) \) to return the label of the closest enclosing context of the element with identifier \( \text{id} \) in the system state \( \Sigma \).

3 Transition Rules

The top-level transition rules are of the form \( \Xi; \Sigma; \mathcal{E} \xrightarrow{\beta} \Xi'; \Sigma'; \mathcal{E}' \). Here, \( \Xi \) denotes remote servers, which are active entities that exchange information with the browser. \( \Sigma \) is the browser state. \( \mathcal{E} \) denotes events waiting to be processed. Events can be user inputs, API requests, and other internal browser events. Each transition is labeled with an action \( \beta \), representing the observable effects of that transition. In this technical report, for rules where \( \Xi \) stay the same, we omit them from the rules.

3.1 Auxiliary Definitions

Web servers The purpose of modeling the web servers is to model web attackers. Each web server is a pair of its URL and program. A web server either listens to a request (listen), or sends a header to the browser (sendHeader(\( h \)), or sends content to the browser (sendContent(\( h \))).

\[
\begin{align*}
\text{Web servers} & : \quad \Xi ::= \cdot \mid \Xi, (\text{url}, \text{exp}) \\
\text{Server Program} & : \quad \text{exp} ::= \text{listen}; \text{x.exp} \mid \text{sendHeader}(\text{h}); \text{exp} \mid \text{sendContent}(\text{h}); \text{exp} \mid \text{skip}
\end{align*}
\]
Actions Observable actions, denoted $\alpha$, include API calls, invocations of callbacks, and processed events. These actions pass on information to event handlers. The browser makes internal transitions, which do not produce observable effects. We use $\tau$ to label such transitions, and call them silent transitions. We define an execution trace $\rho$ as the sequence of non-silent actions in a transition sequence.

\[
\text{Actions} \quad \alpha ::= e \mid \text{API}(\kappa, \text{args}) \mid \text{Ret}(\kappa, \text{args})
\]

\[
\text{Generalized Action} \quad \beta ::= \alpha \mid \tau
\]

\[
\text{Traces} \quad \rho ::= e \mid \rho, \alpha
\]

Definition of enqueuing an event We define $e \sim_t Tab$ to mean that event $e$ is related to the tab $Tab$. We assume that each event carries the identifier of the tab that it is generated from. For events that are returns to asynchronous API calls, it is related to a tab if that tab contains an event handler which is the callback function of that event. This can be checked by examining the event type. An event will be added to each matching event handler’s event queue. Labels are checked when an event handler is about to process the event. Events are not propagated across frames.

\[
\text{EventHandler} \judge \rho e =
\left\{
\begin{array}{l}
\text{EventHandler} \judge \text{eventQueue } \leftarrow \text{eventQueue } :: e \quad \text{eventTypeOf(EventHandler)} \neq \text{eventTypeOf(e)} \\
\text{EventHandler} \judge \text{eventQueue } :: e \quad \text{eventTypeOf(EventHandler)} = \text{eventTypeOf(e)}
\end{array}
\right.
\]

We define $\text{EventHandlers} \judge \rho e$ to be the lifting of $\text{EventHandler} \judge \rho e$ to the list of event handlers.

\[
\text{ExtCoreR} \judge \rho e = \text{ExtCoreR}[\text{EventHandlers} \judge \text{EventHandlers} \judge \rho e]
\]

\[
\text{DocCS} \judge \rho e = \text{DocCS}[\text{Docs} \judge \text{Docs} \judge \rho e]
\]

\[
\text{Doc} \judge \rho e = \text{Doc}[\text{DocCSs} \judge \text{DocCSs} \judge \rho e]
\]

\[
\text{Tab} \judge \rho e = \left\{
\begin{array}{l}
\text{Tab} \judge \text{EventHandlers} \judge \text{EventHandlers} \judge \rho e \quad e \sim_t \text{Tab} \\
\text{Tab}
\end{array}
\right.
\]

\[
\text{Tab} \judge \rho e = \left\{
\begin{array}{l}
\text{Tab} \judge \text{Docs} \judge \text{Docs} \judge \rho e \quad e \sim_t \text{Tab} \\
\text{Tab}
\end{array}
\right.
\]

\[
\text{Tab} \judge \rho e = \text{Tab} \judge \rho e \judge \rho e
\]

Relations between internal browser state and events For web requests, the browser processes a sequence of events in a particular order. We use internal browser state to track such ordering; an event in this sequence can only be processed when the browser is in a corresponding state.

We define two relations to specify the correspondence between an internal browser state and an event: $\psi \sim_b e$ and $\psi \sim_{nb} e$. Because events can be blocking or non-blocking, $\sim_b$ relates a state and a blocking event and $\sim_{nb}$ relates a state and a non-blocking event. We list the elements in both relations below.

\[
\text{ws.beforeRequest}(\kappa, \text{id}ch, (\text{id}t, \text{id}d, \text{id}n), \text{id}e, \text{url}, \text{info}) \sim_b (\text{id}e, \text{webRequest.onBeforeRequest}, \ldots, \kappa)
\]

\[
\text{ws.beforeSendHeader}(\kappa, \text{id}cb, (\text{id}t, \text{id}d, \text{id}n), \text{id}e, \text{url}, \text{info}) \sim_b (\text{id}e, \text{webRequest.onBeforeSendHeaders}, \ldots, \kappa)
\]

\[
\text{ws.headerReceived}(\kappa, \text{id}cb, (\text{id}t, \text{id}d, \text{id}n), \text{id}e, \text{url}, \text{info}) \sim_b (\text{id}e, \text{webRequest.onHeadersReceived}, \ldots, \kappa)
\]

\[
\text{ws.beforeRequest.redirect}(\kappa, \text{id}cb, (\text{id}t, \text{id}d, \text{id}n), \text{id}e, \text{url}, \text{info}) \sim_nb (\text{id}e, \text{webRequest.onBeforeRedirect}, \ldots, \kappa)
\]

\[
\text{ws.headerSent}(\kappa, \text{id}cb, (\text{id}t, \text{id}d, \text{id}n), \text{id}e, \text{url}, \text{info}) \sim_nb (\text{id}e, \text{webRequest.onSendHeaders}, \ldots, \kappa)
\]

\[
\text{ws.responseStarted}(\kappa, \text{id}cb, (\text{id}t, \text{id}d, \text{id}n), \text{id}e, \text{url}, \text{info}) \sim_nb (\text{id}e, \text{webRequest.onResponseStarted}, \ldots, \kappa)
\]

\[
\text{ws.completed}(\kappa, \text{id}cb, (\text{id}t, \text{id}d, \text{id}n), \text{id}e, \text{url}, \text{info}, (\text{content}, \kappa_1)) \sim_nb (\text{id}e, \text{webRequest.onCompleted}, \ldots, \kappa)
\]

\[
\text{ws.failed}(\kappa, \text{id}cb, (\text{id}t, \text{id}d, \text{id}n), \text{id}e, \text{url}, \text{info}, \ell) \sim_nb (\text{id}e, \text{webRequest.onErrorOccurred}, \ldots, \kappa)
\]

\[
\text{readytoCreateDoc}(\text{id}t, \text{id}d, \text{id}e, \ell_{doc}) \sim_nb (\text{id}e, \text{webNavigation.onCommitted}, \ldots, \kappa)
\]
Each web request state contains several IDs. If a web request state is for loading external object to a node or doc, \( id_{cb} \) is set as \( \cdot \) and \((id_t, id_d, id_n)\) stores tab ID, Doc ID and node ID. If a web request state is from a direct web request API call, \( id_{cb} \) is the callback handler’s event type, \((id_t, id_d, id_n)\) is set to null.

### 3.2 Browser Internal State Transition Rules

A browser can change its internal state. We define two state transition functions to specify to which state the browser should transition based on the current internal state. The first function \( \text{nextState}(\psi, \text{arg}) \) takes the current state and an auxiliary argument which could be \( \text{void} \) or \( \text{noChange} \) or \( \text{Blocked}(c) \) as inputs, and returns a new state and a list of events. Generally, the second argument is set as \( \text{void} \). However, when processing a blocking event, the browser’s next state depends on the event handlers’ return value as well. If there is no blocking event handler for the event, the second argument is set as \( \text{noChange} \); else, it is set as \( \text{Blocked}(c) \) where \( c \) is the return value. This function is used in the sequence of transitions that a browser takes to process web requests.

The second function \( \text{nextStateC}(\Sigma, \psi) \) takes the entire browser state and the current browser state as arguments, and returns an updated browser state and a list of events. This function is used when the internal transition also alters other pieces of the browser state such as the DOM.

\[
\Sigma = (\Psi, \ldots) \quad \Psi = \Psi' :: \psi
\]

\[
(\psi', E_1) = \text{nextState}(\psi, \text{void/noChange/Blocked}(c)) \quad \Sigma' = \Sigma[\Psi' :: \psi'] \]  

**INTERNAL STATE Transition 1**

\[
\Sigma = (\Psi, \ldots) \quad \Psi = \Psi' :: \psi \quad (\Sigma', E_1) = \text{nextStateC}(\Sigma, \psi)
\]

**INTERNAL STATE Transition 2**

### 3.3 Script Transition Rules

**Beta rules for scripts** Given \( f, \text{id}, \) and \( \ell \), \( \text{getFunction} \) will find the code of the function \( f \) in the matching scope, and execute it. The content script run at the end of Doc loading can refer to the global variables and functions defined in the content scripts run at the beginning of Doc loading, but not vise versa.

\[
\Gamma, e \Downarrow v \quad \Gamma, x := e \rightarrow \beta \Gamma[x \mapsto v], \text{skip} \quad \text{ASSIGN}
\]

\[
\Gamma, e \Downarrow \text{true} \quad \Gamma, \text{if} e \text{then } cmd_1 \text{ else } cmd_2 \rightarrow \beta \Gamma, cmd_1 \quad \text{IF-T}
\]

\[
\Gamma, e \Downarrow \text{false} \quad \Gamma, \text{if} e \text{then } cmd_1 \text{ else } cmd_2 \rightarrow \beta \Gamma, cmd_2 \quad \text{IF-F}
\]

\[
\Gamma, \text{let } x = v \text{ in } cmd \rightarrow \beta \Gamma, cmd[v/x] \quad \text{LET}
\]

\[
\Gamma, f(e) \rightarrow \beta \Gamma, cmd[e/v] \quad \text{FUNCTION CALL}
\]

**Top-level beta**

\[
\Sigma, cmd \rightarrow \beta \Gamma' \quad \Sigma', cmd' \rightarrow \beta \Gamma' \quad \Sigma' \rightarrow \Sigma \quad \text{CONTEXT}
\]
Returns  The last instruction of an event handler is the return instruction. If the return field of the event handler is
none, indicating that no one is waiting for the return value of this handler, then the script evaluates to skip. The three
rules RETURN-N-CORE, RETURN-N-CS, and RETURN-N-PAGE are for core scripts, content scripts, and page scripts
respectively.

\[
\Sigma_{ctx}(id) = (\Psi, Tabs, ExtCoreR_{ctx}(id), \cdots) \quad ExtCoreR_{ctx}(id) \in ExtCoreR_{ctx}(id)
\]

EVENTHANDLER_{ctx}(id) = (id, \cdot, EventHandlers :: EventHandler_{ctx}, \ell)

\[
\Sigma_{ctx}[\Gamma, ret v | id; \mathcal{E}] \xrightarrow{r} \Sigma_{ctx}[\Gamma, skip | id; \mathcal{E}]
\]

**RETURN-N-CORE**

\[
\Sigma_{ctx}(id) = (\Psi, Tabs_{ctx}(id), \cdots)
\]

\[
t_{ctx}(id) \in Tabs_{ctx}(id) \\
t_{ctx}(id) = (\cdots, Docs_{ctx}(id), \cdots) \quad Docs_{ctx}(id) \in Docs_{ctx}(id)
\]

\[
Doc_{ctx}(id) = (\cdots, DocCS_{ctx}(id), \cdots) \quad DocCS_{ctx}(id) \in DocCS_{ctx}(id)
\]

\[
DocCS_{ctx}(id) = (_, id, \cdots, EventHandlers :: EventHandler_{ctx}(id), \ell,)
\]

\[
\Sigma_{ctx}[\Gamma, ret v | id; \mathcal{E}] \xrightarrow{r} \Sigma_{ctx}[\Gamma, skip | id; \mathcal{E}]
\]

**RETURN-N-CS**

\[
\Sigma_{ctx}(id) = (\Psi, Tabs_{ctx}(id), \cdots)
\]

\[
t_{ctx}(id) \in Tabs_{ctx}(id)
\]

\[
t_{ctx}(id) = (id, Docs(id), url, EventHandlers :: EventHandler_{ctx}(id))
\]

\[
Doc(id) \in Docs(id) \\
Doc(id) = (\cdots, nodes(id), \cdots) \quad node(id) \in nodes(id)
\]

\[
node(id) = (id, attributes, nodes_1, content, \ell) \\
\]

\[
\Sigma_{ctx}[\Gamma, ret v | id; \mathcal{E}] \xrightarrow{r} \Sigma_{ctx}[\Gamma, skip | id; \mathcal{E}]
\]

**RETURN-N-PAGE**

The next three rules RETURN-CORE, RETURN-CS, and RETURN-PAGE are for core scripts, content scripts, and
page scripts to return to callback functions respectively. The *return* of the event handler is some(R, id, r), indicating
that there is a callback function waiting for the completion of this event handler. Here, the event handler is actually an
asynchronous API call (or a callback), R is the name of the original asynchronous API call. When the event handler
returns, the internal browser state is updated to include a new state asyncAPIRetState(R, \ell, id, v), stating that the
asynchronous API call to R has completed with return value v, label \ell, and the callback’s ID is id. We will show
an example at the end of this section.
We model two types of API calls: synchronous calls and asynchronous calls. In general, a caller calls an API. Here, we allow the caller to apply declassification capabilities before the call.

\[ \psi_{\text{ctx}} \]

When the returning event handler is a blocking event handler in the core, a new browser state \( \text{DoneBlkEvtState}(\ell^-, id_r, e, v) \) is generated to signal the completion of processing that blocking event.

\[ \Sigma_{ctx}(id) = (\Psi, \text{Tabs}_{ctx}(id), \cdots) \quad \text{ExtCore}_{ctx}(id) \in \text{ExtCore}_{ctx}(id) \]
\[ \text{ExtCore}_{ctx}(id) = (id, \_ \cdot, \text{EventHandlers} :: \text{EventHandler}_{ctx}, \ell) \]
\[ \text{EventHandler}_{ctx}(id) = (\_ \cdot, \_ \cdot, \text{some}(R, id_r)) \]
\[ \psi = \text{asyncAPIRetState}(R, \ell^-, id_r, v) \quad \Sigma'_{ctx}(id) = \Sigma_{ctx}(id)[\Psi \leftarrow \Psi :: \psi] \]

\[ \Sigma_{ctx}(id) \mid \Gamma, \text{ret } v \\ E \rightarrow \Sigma'_{ctx} \mid \Gamma, \text{skip } id; E \]

Calls are modelled by two types of API calls: synchronous calls and asynchronous calls. In general, a caller calls an API with an argument vector \( \vec{v} \). The label checking for an API call checks whether the caller has permission to call the API. Here, we allow the caller to apply declassification capabilities before the call.

\[ \ell = \text{ctxOfl}(\Sigma_{ctx} \mid \Gamma, API_s(\vec{v}) \mid id; id) \quad \ell^- \neq \text{labOf}(API_s) \]
\[ \Sigma_{ctx} \mid \Gamma, API_s(\vec{v}) \mid id; id; E \rightarrow \Sigma_{ctx} \mid \Gamma, \text{void } id; E \]

\[ \ell = \text{ctxOfl}(\Sigma_{ctx} \mid \Gamma, API_s(\vec{v}) \mid id; id) \]
\[ \ell^- \Rightarrow \text{labOf}(API_s) \quad \Sigma_{ctx} \mid \Gamma, API_s(\vec{v}) \mid id; id; E \rightarrow_{\beta} API_s, \Sigma' ; E' \]

\[ \ell = \text{ctxOfl}(\Sigma_{ctx} \mid \Gamma, API_s(\vec{v}) \mid id; id) \]
\[ \ell^- \neq \text{labOf}(API_s) \]
\[ \Sigma_{ctx} \mid \Gamma, API_s(\vec{v}) \mid id; id; E \rightarrow_{\beta} \Sigma' ; E ; E' \]

\[ \ell = \text{ctxOfl}(\Sigma_{ctx} \mid \Gamma, API_s(\vec{v}) \mid id; id) \]
\[ \ell^- \neq \text{labOf}(API_s) \]
\[ \Sigma_{ctx} \mid \Gamma, API_s(\vec{v}) \mid id; id; E \rightarrow_{\beta} \Sigma_{ctx} \mid \Gamma, \text{skip } id; E \]
There are three asynchronous API fire rules; each adds a new event handler to the context and adds to the browser state an indication that the call has fired. This state will be processed using rule INTERNAL\STATE\TRANSITION2 (Section 3.9). When calling an API, the scripts can use declassification capabilities, and therefore the browser state associated with the call has the declassified label. For calls that include callback functions, the callback functions will be added as new event handlers in the system. The event type of the event handler for a callback function should uniquely identify that function. Events triggering these event handlers will be generated once the asynchronous API finishes and returns its result.

\[
\Sigma_{ctx}(id) = (\Psi, Tabs, ExtCoreRs_{ctx}(id), \ldots) \quad ExtCoreRs_{ctx}(id) \in ExtCoreRs_{ctx}(id) \\
ExtCoreRs_{ctx}[\Gamma, API_a(\vec{v})]_{id} = (id, \ldots, EventHandlers, \ell) \quad \ell \in labOf(API_a) \\
\ell \Rightarrow \kappa_t \\
callbackOf(\vec{v}) = x.cmd \\
fresh(id_{cb}) \quad fresh(id_h) \quad eh = (id_h, id_{cb}, x.cmd, \ldots, skip, void, nonblocking, none) \\
ExtCoreRs_{ctx}'(id) = ExtCoreRs_{ctx}(id)[EventHandlers \Leftarrow EventHandlers :: eh] \\
ExtCoreRs_{ctx}(id) = ExtCoreRs_{ctx}(id)[ExtCoreRs_{ctx}(id) \Leftarrow ExtCoreRs_{ctx}(id)] \\
\psi = agncAPIstate(\kappa_t, id_{cb}, API_a(\vec{v})) \\
\Sigma_{ctx}(id) = \Sigma_{ctx}(id)[ExtCoreRs_{ctx}(id) \Leftarrow ExtCoreRs_{ctx}'(id)[\Psi \Leftarrow \Psi :: \psi] \\
\Sigma_{ctx}[\Gamma, API_a(\vec{v})]_{id}; \mathcal{E} \xrightarrow{\tau} \Sigma'_{ctx}[\Gamma, skip]_{id}; \mathcal{E}
\]

\[
\Sigma_{ctx}(id) = (\Psi, Tabs_{ctx}(id), \ldots) \quad t_{ctx}(id) \in Tabs_{ctx}(id) \\
t_{ctx}(id) = (\ldots, Docs_{ctx}(id), \ldots) \quad Doc_{ctx}(id) \in Docs_{ctx}(id) \\
Doc_{ctx}(id) = (\ldots, DocCS_{ctx}(id), \ldots) \quad DocCS_{ctx}(id) \in DocCS_{ctx}(id) \\
DocCS_{ctx}(id) = (\ldots, id, \ldots, EventHandlers_{ctx}(id), \ell) \quad \ell \in labOf(API_a) \\
\ell \Rightarrow \kappa_t \\
callbackOf(\vec{v}) = x.cmd \\
fresh(id_{cb}) \quad fresh(id_h) \quad eh = (id_h, id_{cb}, x.cmd, \ldots, skip, void, nonblocking, none) \\
DocCS_{ctx}'(id) = DocCS_{ctx}(id)[EventHandlers_{ctx}(id) \Leftarrow EventHandlers_{ctx}(id) :: eh] \\
DocCS_{ctx}(id) = DocCS_{ctx}(id)[DocCS_{ctx}(id) \Leftarrow DocCS_{ctx}'(id)] \\
Doc_{ctx}'(id) = Doc_{ctx}(id)[DocCS_{ctx}(id) \Leftarrow DocCS_{ctx}'(id)] \\
t_{ctx}'(id) = t_{ctx}(id)[Doc_{ctx}(id) \Leftarrow Doc_{ctx}'(id)] \quad \psi = agncAPIstate(\kappa_t, id_{cb}, API_a(\vec{v})) \\
\Sigma_{ctx}(id) = \Sigma_{ctx}(id)[t_{ctx}(id) \Leftarrow t_{ctx}'(id)][\Psi \Leftarrow \Psi : \psi] \\
\Sigma_{ctx}[\Gamma, API_a(\vec{v})]_{id}; \mathcal{E} \xrightarrow{\tau} \Sigma'_{ctx}[\Gamma, skip]_{id}; \mathcal{E}
\]

\[
\Sigma_{ctx}(id) = (\Psi, Tabs_{ctx}(id), \ldots) \quad t_{ctx}(id) \in Tabs_{ctx}(id) \\
t_{ctx}(id) = (\ldots, Docs(id), url, EventHandlers_{ctx}(id), \ldots) \\
Doc(id) \in Docs(id) \quad Doc(id) = (\ldots, nodes(id), \ldots) \quad node(id) \in nodes(id) \\
node(id) = (id, attributes, nodes_1, content, \ell) \quad \ell \in labOf(API_a) \\
\kappa_t, \ell \Rightarrow \kappa_t \\
callbackOf(\vec{v}) = x.cmd \\
fresh(id_{cb}) \quad eh = (id, id_{cb}, x.cmd, \ldots, skip, void, nonblocking, none) \\
t_{ctx}'(id) = t_{ctx}(id)[EventHandlers_{ctx}(id) \Leftarrow EventHandlers_{ctx}(id) :: eh] \\
\psi = agncAPIstate(\kappa_t, id_{cb}, API_a(\vec{v})) \\
\Sigma_{ctx}(id) = \Sigma_{ctx}(id)[t_{ctx}(id) \Leftarrow t_{ctx}'(id)][\Psi \Leftarrow \Psi :: \psi] \\
\Sigma_{ctx}[\Gamma, API_a(\vec{v})]_{id}; \mathcal{E} \xrightarrow{\tau} \Sigma'_{ctx}[\Gamma, skip]_{id}; \mathcal{E}
\]
3.4 Event Enqueue Rules

**Fire nonblocking stateless events** For each handler \(eh\) of \(e\), the system adds \(e\) to the event queue of the handler \(eh\). If the event is not linked to any browser state, it can be processed regardless of the browser state.

\[
e \text{is not a blocking event} \quad \Sigma = (\Psi, Tabs, ExtCoreRs, \cdots) \\
\Sigma' = \Sigma[ExtCoreRs \leftarrow ExtCoreRs \sqsubseteq Q_e][Tabs \leftarrow Tabs \sqsubseteq Q_e] \\
\Sigma; E :: e \rightarrow^* \Sigma'; E
\]

The following rule enqueues a nonblocking event that can only be processed at certain browser states. Further, after going through all the extensions, the browser moves to the next state.

For instance, \(\psi = \text{ws.requestStarted}(\kappa, id_r, id_d, id_n, id_e', url, info')\) is related to \(e = (id_e', \text{webRequest.onResponseStarted}, \text{none, info'}, \kappa)\) \(\psi \sim e\), and the next browser state \(\psi\) is \(\text{ws.completed}(\cdots)\).

\[
e \text{is not a blocking event} \quad \Sigma = (\Psi, Tabs, ExtCoreRs, \cdots) \\
\Psi = \Psi' :: \psi \quad \psi \sim_{nb} e \quad (\psi', e') = \text{nextState}(\psi, \text{void}) \\
\Sigma' = \Sigma[\Psi \leftarrow \Psi' :: \psi'][ExtCoreRs \leftarrow ExtCoreRs \sqsubseteq Q_e][Tabs \leftarrow Tabs \sqsubseteq Q_e] \\
\Sigma; E :: e \rightarrow^* \Sigma'; E :: e'
\]

We may also use \(\text{nextStateC}\) to advance state. In the following rule, besides the event queues of the event handlers, updates other parts of the system as well.

\[
e \text{is not a blocking event} \quad \Sigma = (\Psi, Tabs, ExtCoreRs, \cdots) \\
\Psi = \Psi' :: \psi \quad \psi \sim_{nb} e \quad (\psi', e') = \text{nextStateC}(\Sigma', \psi) \\
(\Sigma'', \xi_1) = \text{nextStateC}(\Sigma', \psi) \\
\Sigma; E :: e \rightarrow^* \Sigma''; E :: \xi_1
\]

**Fire blocking events that have no blocking handlers** In Chromium, only extension cores contain blocking event handlers. Given a blocking event, the non-blocking handlers with a label higher than the event’s and the blocking handlers with a label the same as the event’s can process the event. The browser can only move to the next state after all the blocking handlers have processed the event. If there is no blocking event handler with the same label as the event’s, after enqueuing the event to all its handlers, the browser can advance to the next step directly.

\[
e \text{is a blocking event} \quad \Sigma = (\Psi, Tabs, ExtCoreRs, \cdots) \\
\Psi = \Psi' :: \psi \quad \psi \sim_{b} e \\
\forall \text{ExtCoreR} \in \text{ExtCoreRs}, \text{EHs} = \text{getActiveHandlers}(\text{ExtCoreR}, e), \\
\forall eh \in \text{EHs}, \text{labOf}(eh) = \text{labOf}(e) \Rightarrow \text{isBlocking}(eh) = \text{false} \\
(\psi', e') = \text{nextState}(\psi, \text{void}) \\
\Sigma' = \Sigma[\Psi' :: \psi'][\text{ExtCoreRs} \leftarrow \text{ExtCoreRs} \sqsubseteq Q_e] \\
\Sigma; E :: e \rightarrow^* \Sigma'; E :: e'
\]

**Fire a blocking event** There must exist at least one blocking handler with the same label as the event’s. The browser enqueues the event.

\[
e \text{is a blocking event} \quad \Sigma = (\Psi :: \psi, Tabs, ExtCoreRs, \cdots) \\
\exists \text{ExtCoreR} \in \text{ExtCoreRs}, \text{EHs} = \text{getActiveHandlers}(\text{ExtCoreR}, e), \\
\exists eh \in \text{EHs}, \text{isBlocking}(eh) = \text{true} \land \text{labOf}(eh) = \text{labOf}(e) \\
\Sigma' = \Sigma[\text{ExtCoreRs} \leftarrow \text{ExtCoreRs} \sqsubseteq Q_e] \\
\Sigma; E :: e \rightarrow^* \Sigma'; E
\]
BlockFinished1

Blocking handler finished (1) All the blocking handlers for the event have finished processing the event, and none of them returns a value to change the browser behavior. The browser moves to the next step using nextstate based on the browser state related to the event.

\[
e \text{is a blocking event } e \sim_\eta \psi \quad \Sigma = (\Psi, Tabs, ExtCoreRs, \cdots) \quad \Psi = \Psi_1 :: \psi :: \Psi_2 \\
\#\psi \in \Psi_1, \text{s.t. } \psi = \text{ProcBlkEvtState}(\_, \_, e) \text{ or DoneBlkEvtState}(\cdots, e, \_) \\
\Psi_2 \text{ contains matching pairs of ProcBlkEvtState}(\_, id_r, e) \text{ and DoneBlkEvtState}(\_, id_r, e, 0) \\
\forall ExtCoreR \in ExtCoreRs, EHs = \text{getActiveHandlers}(ExtCoreR, e), \\
\forall eh \in EHs, labOf(eh^-) = labOf(e) \land isBlocking(eh) = true, e \notin Qof(eh) \\
(\psi', \mathcal{E}_1) = \text{nextState}(\psi, \text{noChange}) \\
\Sigma' = \Sigma[\Psi \leftarrow \Psi_1 :: \psi] \\
\Sigma; \mathcal{E} \xrightarrow{\tau} \Sigma'; \mathcal{E} :: \mathcal{E}_1
\]

BlockFinished2

Blocking handler finished (2) All the blocking handlers for the event have finished processing the event. Every blocking handler with the same label as the event’s has returned a value. The system chooses the return value that comes from the last installed extension’s handler. Then the browser moves to a new state according to the current browser state and the selected return value. \(\mathcal{E}_1\) denotes the subsequent events triggered.

\[
e \text{is a blocking event } e \sim_\eta \psi \quad \Sigma = (\Psi, Tabs, ExtCoreRs, \cdots) \quad \Psi = \Psi_1 :: \psi :: \Psi_2 \\
\#\psi \in \Psi_1, \text{s.t. } \psi = \text{ProcBlkEvtState}(\_, \_, e) \text{ or DoneBlkEvtState}(\cdots, e, \_) \\
\Psi_2 \text{ contains matching pairs of ProcBlkEvtState}(\_, id, e) \text{ and DoneBlkEvtState}(\_, id, e, c_j) \\
\forall ExtCoreR \in ExtCoreRs, EHs = \text{getActiveHandlers}(ExtCoreR, e), \\
\forall eh \in EHs, labOf(eh^-) = labOf(e) \land isBlocking(eh) = true, e \notin Qof(eh) \\
\text{getLastInstalledReturn}(\Psi_2) = (\kappa, id_j, c_j) \text{ s.t. } c_j \neq 0 \\
(\psi', \mathcal{E}_1) = \text{nextState}(\psi, \text{Blocked}(c_j)) \\
\Sigma' = \Sigma[\Psi \leftarrow \Psi_1 :: \psi] \\
\Sigma; \mathcal{E} \xrightarrow{\tau} \Sigma'; \mathcal{E} :: \mathcal{E}_1
\]

3.5 Event Dequeue Rules

Dequeue an event in CS In content scripts, after finishing the processing of an event, a handler dequeues the next event \(e\) in its event queue. If \(e\)’s label is not lower than the hosting content script’s label, \(e\) will be discarded; else, the event handler starts processing \(e\). As long as \(e\) is processed by the handler, the hosting content script label is tainted with \(e\)’s label.

\[
\Sigma_{cxt}(id) = (\Psi, Tabs_{cxt}(id), \cdots) \\
t_{cxt}(id) = (\cdots, Doc_{cxt}(id), \cdots) \\
Doc_{cxt}(id) = (\cdots, DocCS_{cxt}(id), \cdots) \\
DocCS_{cxt}(id) = (\_, id, \_, \_, \_, eventHandlers :: eh_{cxt}, \ell) \\
eh_{cxt} = (\_., eventType, x, cmd, e :: \mathcal{E}_1, \_, id_e, BlockingFlag, return) \\
labOf(e) \not\subseteq \ell' \\
\text{eh}'_{cxt} = (\_., eventType, x, cmd, \mathcal{E}_1, \_, id_e, BlockingFlag, return) \\
Doc_{cxt}'_{cxt}(id) = DocCS_{cxt}(id)[eh_{cxt} \leftarrow eh'_{cxt}] \\
DocCS'_{cxt}(id) = DocCS_{cxt}(id)[Doc_{cxt}(id) \leftarrow Doc_{cxt}'_{cxt}(id)] \\
Doc_{cxt}'(id) = Doc_{cxt}(id)[DocCS_{cxt}(id) \leftarrow DocCS'_{cxt}(id)] \\
t'_{cxt}(id) = t_{cxt}(id)[Doc_{cxt}(id) \leftarrow Doc_{cxt}'(id)] \\
\Sigma_{cxt}(id) = \Sigma_{cxt}(id)[t_{cxt}(id) \leftarrow t'_{cxt}(id)] \\
\Sigma_{cxt}[\Gamma, skip]|_{id}; \mathcal{E} \xrightarrow{\tau} \Sigma_{cxt}'[\Gamma, skip]|_{id}; \mathcal{E}
\]

EventDequeueCS1
Dequeue an event in Core  In extension cores, after finishing processing of an event, a handler dequeues the next event \( e \) in its event queue. A non-blocking event handler can process an event if the event’s label is lower than the handler’s hosting extension core’s label. A blocking event handler can process an event and generate a new browser state \( \text{ProcBlkEvtState}(\kappa_e, id, e) \) if its label (after necessary floating) is the same as the event’s, where \( \kappa_e \) is \( e \)’s label and \( id \) is a fresh random string. As long as \( e \) is processed by the handler, the hosting extension core’s label is tainted with \( e \)’s label.

If a handler cannot process an event due to label checking, the event will be discarded.

\[
\begin{align*}
\Sigma_{ctx}(id) &= (\Psi, \text{Tabs}, \text{ExtCoreRs}_{ctx}(id), \ldots) \\
\text{ExtCoreRs}_{ctx}(id) &= \text{ExtCoreRs}_{ctx}(id) \\
\text{eh}_{ctx}(e) &= (\cdot, \text{eventType}, x, \text{cmd}, e :: \Sigma_1, \|, id_e, \text{BlockingFlag}, \text{return})
\end{align*}
\]
Dequeue a page event  In page scripts, after finishing processing of an event, a handler dequeues the next event \( e \) in its event queue. There are two types of script handlers: inline handlers and the handlers added using “addEventListener”. Here we model the second type of handlers. If \( e \)'s label is not lower than the hosting page script node's label, \( e \) will be discarded; else, the event handler starts processing \( e \). As long as \( e \) is processed by the handler, the hosting page script node’s label is tainted with \( e \)'s label.

\[
\Sigma_{ctx}(id) = (\Psi, Tabs, ExtCoreR_{ctx}(id), \cdots)
\]
\[
ExtCoreR_{ctx}(id) \in ExtCoreR_{ctx}(id)
\]
\[
ExtCoreR_{ctx}(id) = (id, (\|, -), EventHandlers :: eh_{ctx}, \ell)
\]
\[
eh_{ctx} = (\cdot, eventType, x.cmd, e :: E_1, \|, id_e, blocking, return)
\]
\[
labOf(e) \neq \ell^-
\]
\[
eh'_{ctx} = (\cdot, eventType, x.cmd, E_1, \|, id_e, blocking, return)
\]
\[
ExtCoreR_{ctx}'(id) = ExtCoreR_{ctx}(id)\left[\text{ExtCoreR}_{ctx}(id) \leftarrow ExtCoreR_{ctx}'(id)\right]
\]
\[
\Sigma'_{ctx}(id) = \Sigma_{ctx}(id)\left[\text{ExtCoreR}_{ctx}(id) \leftarrow ExtCoreR_{ctx}'(id)\right]
\]

\[
\Sigma_{ctx}(id) = (\Psi, Tabs, ExtCoreR_{ctx}(id), \cdots)
\]
\[
ExtCoreR_{ctx}(id) \in ExtCoreR_{ctx}(id)
\]
\[
ExtCoreR_{ctx}(id) = (id, (\|, -), EventHandlers :: eh_{ctx}, \ell)
\]
\[
eh_{ctx} = (\cdot, eventType, x.cmd, e :: E_1, \|, id_e, blocking, return)
\]
\[
e = (id_e', \cdot, eventType, return, \cdots, \kappa_e)
\]
\[
\kappa_e = \ell^-
\]
\[
\psi = \text{ProcBlkEvtState}(\kappa_e, id_e, e)
\]
\[
eh'_{ctx} = (\cdot, eventType, x.cmd, E_1, \|, id_e', blocking, some(e, id_e))
\]
\[
ExtCoreR_{ctx}'(id) = ExtCoreR_{ctx}(id)\left[\text{ExtCoreR}_{ctx}(id) \leftarrow eh'_{ctx}\right]
\]
\[
ExtCoreR_{ctx}(id) = (id, (\|, -), EventHandlers :: eh_{ctx}, \ell)
\]
\[
\Sigma'_{ctx}(id) = \Sigma_{ctx}(id)\left[\text{ExtCoreR}_{ctx}(id) \leftarrow ExtCoreR_{ctx}'(id)\right]\left[\Psi = \Psi :: \psi\right]
\]

\[
\Sigma_{ctx}(id) = (\Psi, Tabs_{ctx}(id), \cdots)
\]
\[
l_{ctx}(id) \in Tabs_{ctx}(id)
\]
\[
l_{ctx}(id) = (id, Docеваm(id), url, EventHandlers :: eh_{ctx}(id), \_)
\]
\[
eh_{ctx} = (id, Docеваm(id), url, EventHandlers :: eh_{ctx}(id), \_)
\]
\[
Docеваm(id) \in Docsеваm(id)
\]
\[
Goals{евm}(id) = (\cdot, nodesеваm(id), \cdots)
\]
\[
nodeеваm(id) \in nodesеваm(id)
\]
\[
nodeеваm(id) = (id, \_ \cdots \_ \_ \ell, \|, \ell^*)
\]
\[
l'_{ctx}(id) = l_{ctx}(id)\left[eh_{ctx}(id) \leftarrow eh'_{ctx}(id)\right]
\]
\[
\Sigma'_{ctx}(id) = \Sigma_{ctx}(id)\left[eh_{ctx}(id) \leftarrow eh'_{ctx}(id)\right]
\]
Receiving data
The web server sends header information to the browser. When the header arrives at the browser, the browser generates an internal browser state so the data is processed later.

\[ e = (\_\_, \text{sendToServer}, \_\_ (\text{url}, \text{id}_e), \kappa) \]

\[ \Xi :: (\text{url}, \text{listen}; x. \exp); \Sigma; \mathcal{E} \quad \xrightarrow{\text{sendToServer} (\text{url}, \cdot, \kappa)} \quad \Xi :: (\text{url}, \exp [\text{r} / x]); \Sigma; \mathcal{E} \]

Receiving data
The web server sends header information to the browser. When the header arrives at the browser, the browser generates an internal browser state so the data is processed later.

\[ e = (\_\_, \text{sendToServer}, \_\_ (\text{url}, \text{id}_e), \kappa) \]

\[ \Xi :: (\text{url}, \text{listen}; x. \exp); \Sigma; \mathcal{E} \quad \xrightarrow{\text{sendToServer} (\text{url}, \cdot, \kappa)} \quad \Xi :: (\text{url}, \exp [\text{r} / x]); \Sigma; \mathcal{E} \]

The browser has sent a web request to the server; it has a browser state \( \text{ws} . \text{headerSent} (\kappa, \text{id}_cb, \text{id}_e, \text{url}, \text{info}) \) and is waiting for the header from the server. Upon receiving a headerSent event \( e \), if \( e \) and \( \text{ws} . \text{headerSent} (\kappa, \text{id}_cb, \text{id}_e, \text{url}, \text{info}) \) are paired (through \( \text{info} \)), the browser steps from the \( \text{ws} . \text{headerSent}(\cdot \cdot \cdot) \) state to a headerRecvd(\cdot \cdot \cdot) state, and issues a \text{webRequest.onHeadersReceived} event.

We know that \( \kappa \subseteq \text{labFrom}(\text{url}) \) as we checked labels when the web request was initialized. And by default, \( \kappa' = \text{labFrom}(\text{url}) \) (see rule SERVERSNDDHDR).

\[ \Sigma = (\Psi; \cdot \cdot \cdot); \quad \Psi = \Psi_1 :: \text{ws} . \text{headerSent} (\kappa, \text{id}_cb, \text{id}_e, \text{url}, \text{info}) \]

\[ e = (\text{id}_e, \text{headerSent}, \text{none}, \text{info}, \kappa'); \quad \psi = \text{headerRecvd} (\text{url}, \text{id}_cb, \kappa' \bowtie \kappa) \]

\[ \Sigma; \mathcal{E} :: e \xrightarrow{\psi} \Sigma [\Psi \leftarrow \Psi_1 :: \psi]; \mathcal{E} :: e' \]
The browser receives content and generates an internal state to indicate that the content needs to be processed later.

\[ \Sigma = (\Psi, \ldots) \quad e = (id, contentSent, none, info, \kappa) \quad \psi = contentRecvd(url, info, \kappa) \]

\[ \Sigma; E :: e \xrightarrow{\text{CONTENTRECVED}} \Sigma[\psi \leftarrow \Psi :: \psi]; E \]

### 3.7 Browser State Transitions

The sequence of transitions starts when a web request is made, either because of an update to a tab’s URL; or due to requests made to obtain external resources during DOM tree construction; or because of a DOM write that updates a node and requires contacting remote servers.

#### 3.7.1 Deciding Whether to Send webRequest

Here the browser is going to fetch an object such as a script or an image for a DOM node. The node is assigned with the external object’s URL. The node and a readyToFetch state were created during the DOM tree creation procedure (see CREATEDOC(2)) or added by a script (DOMAPPENDCHILDREN(1)). The readyToFetch state has several arguments and has the form: readyToFetch(\(\kappa, (id_t, id_d, id_{n}, \text{url}_{\text{RES}})\), where \(\kappa\) is the simplified node label, \((id_t, id_d, id_n)\) indicates which node is going to load the object, and \(\text{url}_{\text{RES}}\) is the external object’s URL. If the resource fetching is allowed, the browser implicitly launches a web request call and generates a ws.beforeRequest(\(\kappa, id_{cb}, (id_t, id_d, id_{n}), id_e, info, url\)) state.

\[ \Sigma = (\Psi :: \psi, Tabs :: t, \ldots) \quad \psi = \text{readyToFetch}(\kappa, (id_t, id_d, id_{n}), \text{url}) \]

\[ t = (id_t, Docs :: Doc, url_{1, \ldots, \ell_t}) \quad \text{Doc} = (id_d, \text{url}, \text{nodes}, DocCSs, \chi, \ell_d) \]

\[ \text{node} \in_b \text{nodes} \quad \text{node} = (id_n, \ldots, \ell_n) \quad \text{NetDeclassify}(\ell_n^-) \subseteq \text{labFrom(url)} \]

\[ \psi' = \text{webRequestGet}(\kappa, (id_t, id_d, id_{n}), \text{info, url}) \]

\[ \Sigma' = \Sigma[\psi \leftarrow \psi'] \]

\[ \text{nextStateC}(\Sigma, \text{readyToFetch}(\kappa, id_t, id_d, id_{n}, \text{url})) = \Sigma'; \]

\[ \text{FETCHALLOWED} \]

The object is not allowed to be loaded in a node. We still keep the node, because it may have sub-nodes.

\[ \Sigma = (\Psi :: \psi, Tabs :: t, \ldots) \]

\[ \psi = \text{readyToFetch}(\kappa, (id_t, id_d, id_{n}), \text{url}_{\text{RES}}) \quad t = (id_t, Docs :: Doc, url_{1, \ldots, \ell_t}) \]

\[ \text{Doc} = (id_d, \text{url}, \text{nodes}, DocCSs, \chi, \ell_d) \quad \text{node} \in_b \text{nodes} \]

\[ \text{node} = (id_n, \ldots, \ell_n) \quad \text{NetDeclassify}(\ell_n^-) \not\subseteq \text{labFrom(url)} \]

\[ \Sigma' = \Sigma[\psi \leftarrow \Psi] \]

\[ \text{nextStateC}(\Sigma, \text{readyToFetch}(\kappa, id_t, id_d, id_{p}, \text{url}_{\text{RES}})) = \Sigma'; e = \cdot \]

\[ \text{FETCHBLOCKED} \]

Now the system has a readyToFetchDoc state with arguments (\(\kappa, id_t, \ldots, url\)). It means the browser is going to load a new top-level document to a tab. \(\ell_t\) is the tab’s label. \(\kappa\) is the readyToFetchDoc state’s label. \(url\) is the top-level document’s URL. Given \(\ell_t, \kappa, \text{and url, computeLabel}\) works as follows: if \(\ell_t \Rightarrow \text{labFrom(url)}\), it outputs \(\ell_t, \omega_M \text{labFrom(url)}\); else, it outputs \(\emptyset\). We don’t check whether \(\kappa \subseteq \text{labOf(url)}\), as \(\kappa\) comes from \(\ell_t\), and \(\kappa\) could be not lower than \(\text{labFrom(url)}\).

If computeLabel’s output is not equal to \(\emptyset\), then the system will allow the top-level document to be loaded to the tab. A new blank document will be created and added to the tab. The system will transfer from the readyToCreateDoc state to a ws.beforeRequest state.
For blocking handlers, we will restrict that only the handler/core with the same label as the event/state can return a value. So we don’t need to check the label in nextState.

3.7.2 Web State Transitions
For web requests for loading external objects/pages, we check whether they can go out according to the rules in Section 3.7.1. For web requests issued by calling HTTP WebRequest APIs, we check whether they can go out in the HTTPWebRequest asyAPICall rules. So given a web request related browser state \( ws \) \( * (\kappa, \cdots, url, \cdot) \) from an entity with label \( \ell \), by default, we have \( \ell \Rightarrow labFrom(url) \). However, it is not necessary to require that \( \kappa \subseteq labFrom(url) \).

**Before the request is sent** \( ws \).beforeRequest(\( \cdots \)) is a browser state related to a blocking event webRequest.onBeforeRequest(\( \cdots \)). \( updates \) is the selected output from all the blocking handlers for the event. The browser decides which is the next step based on \( updates \).

\[
\Sigma = (\Psi :: \psi, \cdots) \quad \psi' = ws\cdot beforeRequest(\kappa, *, (id_t, id_d, id_n), id_e, info, urlRES)
\]

\[
fresh(id_e) \quad info_1 = (id_e, info)
\]

\[
e = (id_e, webRequest\cdot onBeforeRequest, none, info_1, \kappa) \quad \Sigma' = \Sigma[\psi \leftarrow \psi']
\]

\[
nextStateC(\Sigma', webRequest\cdot onBeforeRequestGet(\kappa, *, (id_t, id_d, id_n), info, urlRES)) = \Sigma'; e
\]

\[
updates = void or noChange
\]

\[
fresh(id_e') \quad \psi' = ws\cdot beforeSendHeader(\kappa, \cdot, (id_t, id_d, id_n), id_e', info)
\]

\[
e = (id_e', webRequest\cdot onBeforeSendHeaders, none, info, \kappa)
\]

\[
nextState(ws\cdot beforeRequest(\kappa, id_cb, (id_t, id_d, id_n), id_e, url, info, updates)) = \psi', e
\]

\[
updates = Blocked(\text{redirect, url}_1) \quad info_2 = updateInfo(info, updates)
\]

\[
fresh(id_e') \quad \psi' = ws\cdot beforeRequest\cdot redirect(\kappa, id_cb, (id_t, id_d, id_n), id_e', url_1, info_2)
\]

\[
e = (id_e', webRequest\cdot onBeforeRedirect, none, info_2, \kappa)
\]

\[
nextState(ws\cdot beforeRequest(\kappa, id_cb, (id_t, id_d, id_n), id_e, url, info, updates)) = \psi', e
\]

\[
updates = Blocked(\text{cancel}) \quad id_{cb} = \cdot \quad info_2 = updateInfo(info, updates)
\]

\[
fresh(id_e') \quad \psi' = ws\cdot failed(\kappa, id_{cb}, (id_t, id_d, id_n), id_e', url, info_2)
\]

\[
e = (id_e', webRequest\cdot onErrorOccurred, none, info_2, \kappa)
\]

\[
nextState(ws\cdot beforeRequest(\kappa, id_{cb}, (id_t, id_d, id_n), id_e, url, info, updates)) = \psi', e
\]

\[
updates = Blocked(\text{cancel}) \quad id_{cb} \neq \cdot \quad id_{cb} = \cdot
\]

\[
fresh(id_e') \quad \psi' = ws\cdot failed(\kappa, id_{cb}, (id_t, id_d, id_n), id_e', url, info_2)
\]

\[
e' = (id_e', webRequest\cdot onErrorOccurred, none, info_2, \kappa)
\]

\[
nextState(ws\cdot beforeRequest(\kappa, id_{cb}, (id_t, id_d, id_n), id_e, url, info, updates)) = \psi', e''
\]

\[
fresh(id_e') \quad \psi' = ws\cdot beforeRequest(\kappa, id_{cb}, (id_t, id_d, id_n), id_e', url, info)
\]

\[
e = (id_e', webRequest\cdot onBeforeRequest, none, info, \kappa)
\]

\[
nextState(ws\cdot beforeRequest\cdot redirect(\kappa, id_{cb}, (id_t, id_d, id_n), id_e, url, info, void)) = \psi', e
\]

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Before the header is sent  The state that relates to the blocking event webRequest.onBeforeSendHeaders is ws.beforeSendHeader. Depending on whether there are blocking event handlers, and the result returned by these handlers, the nextState function advances to different states. Here, we also generate an external event denoting that data is send across the network.

\[
\text{updates} = \text{void} \lor \text{noChange}
\]

\[
fresh(id') \quad \psi' = \text{ws.headerSent}(\kappa, id_cb, (id_t, id_d, id_n), id_e', url, info)
\]

\[
e = (id_e', \text{webRequest.onSendHeaders}, \text{none}, info, \kappa) \quad e' = (\text{sendToServer}, (url, id_e'), \kappa')
\]

\[
\text{nextState}(\text{ws.beforeSendHeader}(\kappa, id_cb, (id_t, id_d, id_n), id_e, url, info), \text{updates}) = \psi', e :: e' \quad \text{NS-Ws-BSH(1)}
\]

The following rule applies when the event handler blocks the header. The blocking handler can rewrite the header.

\[
\text{updates} = \text{Blocked}(\text{newHeader}, \text{header}) \quad \text{info}' = \text{updateInfo}(\text{info}, \text{updates})
\]

\[
fresh(id') \quad \psi' = \text{ws.headerSent}(\kappa, id_cb, (id_t, id_d, id_n), id_e', url, \text{info'})
\]

\[
e = (id_e', \text{webRequest.onSendHeaders}, \text{none}, \text{info'}, \kappa) \quad e' = (\text{sendToServer}, \text{w}, \kappa')
\]

\[
\text{nextState}(\text{ws.beforeSendHeader}(\kappa, id_cb, (id_t, id_d, id_n), id_e, url, \text{info}), \text{updates}) = \psi', e :: e' \quad \text{NS-Ws-BSH(2)}
\]

The following rule applies when one of the event handlers cancels the web request.

\[
\text{updates} = \text{Blocked}(\text{Cancel}) \quad \text{id}_c = \cdot
\]

\[
fresh(id') \quad \psi' = \text{ws.failed}(\kappa, id_cb, (id_t, id_d, id_n), id_e', url, \text{info'})
\]

\[
e = (id_e', \text{webRequest.onErrorOccurred}, \text{none}, \text{info'}, \kappa)
\]

\[
\text{nextState}(\text{ws.beforeSendHeader}(\kappa, id_cb, (id_t, id_d, id_n), id_e, url, \text{info}), \text{updates}) = \psi', e \quad \text{NS-Ws-BSH(3A)}
\]

Receiving header  After header is sent, the browser will receive a header from the server. The following two rules are the first place the header is received.

\[
fresh(id_e') \quad \psi' = \text{ws.headerReceived}(\kappa, id_cb, (id_t, id_d, id_n), id_e', url, \text{info'})
\]

\[
e = (id_e', \text{webRequest.onHeadersReceived}, \text{none}, \text{info'}, \kappa)
\]

\[
\text{nextState}(\text{headerRecvd}(url, id_t, id_d, id_n, \kappa), \cdot) = \psi', e \quad \text{NS-Ws-HS}
\]

Processing header  Once the header is received, the browser transitions to a blocking state. updates comes from the blocking handlers.

\[
\psi' = \text{ws.headerRecvUpdated}(\kappa, id_cb, (id_t, id_d, id_n), id_e, url, \text{info}, \text{updates})
\]

\[
\text{nextState}(\text{ws.headerReceived}(\kappa, id_cb, (id_t, id_d, id_n), id_e, url, \text{info}), \text{updates}) = \psi',
\]

We allow a blocking event handler to update the header. In the following rule, the web request is for loading an external object (not a page). The header does not contain any CSP. However, the header may contain commands for
setting cookies. info and updates contain cookie setting commands from the original header and the blocking event handlers respectively.

\[\Sigma = (\Psi, \ldots)\]
\[\Psi = \Psi'':: \text{ws.headerRecvUpdated}(\kappa, id_{cb}, (id_{t}, id_{d}, id_{n}), id_{e}, url, info, updates)\]
\[\text{updates} = \text{void} \lor \text{noChange} \lor \text{Blocked}(\text{newHdr}, \text{header})\]
\[\text{info} = \text{updateInfo(info, updates)}\]
\[\Psi' = \text{processCookieCmds}(\text{info, updates})\]
\[\text{header is for an object}\]
\[\psi' = \text{ws.responseStarted}(\kappa, id_{cb}, (id_{t}, id_{d}, id_{n}), id_{e}', url, info')\]
\[\psi' = \text{getCSP(info, updates)}\]
\[\chi' = \text{computeNewLabel}()\]
\[\text{nextStateC}(\Sigma, \text{ws.headerRecvUpdated}(\kappa, id_{cb}, (id_{t}, id_{d}, id_{n}), id_{e}, url, info, updates)) = \Sigma', e\]

If the header is for a document, we extract the CSP from the header, and recompute the label for the document. Note that the CSP is an additional layer of policy applied on top of the policies represented by the original document label \(\ell_d\). The CSP can only tighten the existing constraints of \(\ell_d\). We leave this function definition abstract. The generalized CSP could be augmented to include additional information as to how to restrict the label of the doc.

\[\Sigma = (\Psi, \text{Tabs}, \ldots)\]
\[\Psi = \Psi'':: \text{ws.headerRecvUpdated}(\kappa, id_{cb}, (id_{t}, id_{d}, id_{n}), id_{e}, url, info, updates)\]
\[\text{Tabs} = \text{Tabs}'':: t \quad t = (id_{t}, \text{Docs} :: \text{Doc}_{\ldots, \ldots, \ldots})\]
\[\text{Doc} = (id_{d}, \ldots, \ldots, \chi, \ell_d)\]
\[\text{updates} = \text{void} \lor \text{noChange} \lor \text{Blocked}(\text{newHdr}, \text{header})\]
\[\text{header is for a doc}\]
\[\text{info} = \text{updateInfo(info, updates)}\]
\[\psi' = \text{ws.responseStarted}(\ell_d', id_{cb}, (id_{t}, id_{d}, id_{n}), id_{e}', url, info')\]
\[\chi' = \text{getCSP(info, updates)}\]
\[\Psi' = \text{computeNewLabel}(\chi', \ell_d)\]
\[\text{nextStateC}(\Sigma, \text{ws.headerRecvUpdated}(\kappa, id_{cb}, (id_{t}, id_{d}, id_{n}), id_{e}, url, info, updates)) = \psi', e\]

The browser enters a failed state if the CSP blocks everything including the content from the to-be-fetched doc itself. This situation is not likely to happen if by default any CSP will support its host page’s URL.

\[\Sigma = (\Psi, \text{Tabs}, \ldots)\]
\[\Psi = \Psi'':: \text{ws.headerReceived}(\kappa, id_{cb}, (id_{t}, id_{d}, id_{n}), id_{e}, url, info).\text{updates}\]
\[\text{Tabs} = \text{Tabs}'':: t \quad t = (id_{t}, \text{Docs} :: \text{Doc}_{\ldots, \ldots, \ldots})\]
\[\text{Doc} = (id_{d}, \ldots, \ldots, \chi, \ell_d)\]
\[\text{updates} = \text{void} \lor \text{noChange} \lor \text{Blocked}(\text{newHdr}, \text{header})\]
\[\text{header is for a doc}\]
\[\text{info} = \text{updateInfo(info, updates)}\]
\[\chi' = \text{getCSP(info, updates)}\]
\[\psi' = \text{ws.failed}(\kappa, id_{cb}, (id_{t}, id_{d}, id_{n}), id_{e}', url, info_2)\]
\[\psi' = \Psi'':: \psi' :: \Psi_1\]
\[\text{nextStateC}(\Sigma, \text{ws.headerRecvUpdated}(\kappa, id_{cb}, (id_{t}, id_{d}, id_{n}), id_{e}, url, info, updates)) = \psi', e\]
\[ \Sigma = (\Psi, \text{Tabs}, \ldots) \]
\[ \Psi = \Psi_1 \cdot : = \text{ws.headerReceived}(\kappa, id_{cb}, (id_t, id_d, id_n), id_e, url, info).\text{updates} \]
\[ \text{Tabs} = \text{Tabs}'' = t = (id_t, \text{Docs} :: \text{Doc}, \ldots \ldots) \quad \text{Doc} = (id_d, \ldots \ldots, \chi, \ell_d) \]
\[ \text{updates} = \emptyset \lor \text{noChange} \lor \text{Blocked}(\text{newHdr}, \text{header}) \quad \text{header is for a doc} \]
\[ \Psi_1 = \text{processCookieCmds}(\kappa, \text{info}, \text{updates}) \quad \text{info} = \text{updateInfo}(\text{info}, \text{updates}) \]
\[ \chi' = \text{getCSP}(\text{info}, \text{updates}) \quad \emptyset = \text{computeNewLabel}(\chi', \ell_d) \]
\[ \text{fresh}(id_e') \quad \text{fresh}(id_e'') \quad \psi' = \text{ws.failed}(\kappa, id_{cb}, (id_t, id_d, id_n), id_e', url, info_2) \]
\[ \Psi' = \Psi'' : : \Psi_1 \quad \Sigma' = \Sigma[\Psi \leftarrow \Psi'] \]
\[ e = (id_e', \text{webRequest.onErrorOccurred}, \text{none}, \text{info}_2, \kappa) \quad e' = (id_e'', id_{cb}, \text{none}, \text{info}_2, \kappa) \]
\[ \text{nextStateC}(\Sigma, \text{ws.headerRecvUpdated}(\kappa, id_{cb}, (id_t, id_d, id_n), id_e, url, info, \text{updates})) = \psi', e \,::\, e' \quad \text{NS-Ws-HR-Upd(4)} \]

**Content arriving** When the browser receives the content from the server, the web request is completed. The browser goes to the next state. It is a afterFetchedDoc state if the web request loads a page. Else, it is a afterFetched state.

\[ \Sigma = (\Psi, \ldots) \]
\[ \Psi = \Psi_1 :: : \text{contentRecved}(\text{url}, \text{content}, \kappa) :: \text{ws.responseTextStarted}(\kappa_1, id_{cb}, (id_t, id_d, id_n), id_e, url, info) \]
\[ \text{fresh}(id_{e''}) \]
\[ \psi' = \text{ws.completed}(\kappa \cup M \cup \kappa_1, id_{cb}, (id_t, id_d, id_n), id_{e''}, url, info', \text{content}) \quad id_{cb} = \cdot \]
\[ e = (id_{e''}, \text{webRequest.onCompleted}, \text{none}, \text{info'}, \kappa \cup M \cup \kappa_1) \]
\[ \Sigma' = \Sigma[\Psi \leftarrow \Psi_1 :: \psi'] \]
\[ \text{nextStateC}(\Sigma, \text{ws.responseTextStarted}(\kappa_1, id_{cb}, (id_t, id_d, id_n), id_e, url, info, \cdot), \cdot) = \Sigma', e \quad \text{NS-Ws-RS(1)} \]

**Content Loading**

Content fetched from server is loaded to a node. The node is not a script node.
that are set to run in this phase.

There are three phases,

\[ \text{Create the DOM tree} \quad \text{Next, the browser creates the DOM tree and injects content scripts. DOM tree creation contains three phases, DocBegin, DocEnd, and DocIdl. At each phase, the browser only injects the content scripts that are set to run in this phase.} \]

\[ \sum = (\Psi :: \psi, \text{Tabs, Exts, ExtCoreRs}, \cdots) \]
\[ \text{Tabs} = t :: \text{Tabs}_1 \quad \text{\( t = (\text{id}_t, \text{Docs} :: \text{Doc}, \text{url}_1, \ldots, \ell_{\text{tab}}) \)} \]
\[ \psi = \text{afterFetched}(\kappa, \text{id}_t, \text{id}_d, \text{id}_n, \text{content}) \quad \text{Doc} = (\text{id}_d, \text{nodes}, \cdots) \]
\[ \text{node} \in \text{nodes} \quad \text{node} = (\text{id}_n, \text{attributes} \cdot \cdot \cdot, \text{content}_n, \ell_n) \quad \text{type} \in \text{attributes} \]
\[ \text{type} \neq \text{script} \quad \ell'_n = \kappa \triangleright \text{int} \quad \ell_n \quad \text{node}' = \text{node}[\text{content}_n \leftarrow \text{content}, \ell_n \leftarrow \ell'_n] \]
\[ \text{nodes}' = \text{nodes}[\text{node} \leftarrow \text{node}'] \quad \text{Doc} = \text{Doc}[\text{nodes} \leftarrow \text{nodes}'] \]
\[ \psi' = \cdot \quad t' = t[D\text{oc} \leftarrow \text{Doc}'] \quad \sum' = \sum[t \leftarrow t'][\psi \leftarrow \psi'] \]

nextStateC\( (\sum, \text{afterFetched}(\kappa, \text{id}_t, \text{id}_d, \text{id}_n, \text{content})) = \sum' : \)

A script is loaded to a node. The browser extracts event handlers from the script.

\[ \sum = (\Psi :: \psi, \text{Tabs, Exts, ExtCoreRs}, \cdots) \]
\[ \text{Tabs} = t :: \text{Tabs}_1 \quad \text{\( t = (\text{id}_t, \text{Docs} :: \text{Doc}, \text{url}_1, \ldots, \ell_{\text{tab}}) \)} \]
\[ \psi = \text{afterFetched}(\kappa, \text{id}_t, \text{id}_d, \text{id}_n, \text{content}) \quad \text{Doc} = (\text{id}_d, \text{nodes}, \cdots) \]
\[ \text{node} \in \text{nodes} \quad \text{node} = (\text{id}_n, \text{attributes} \cdot \cdot \cdot, \text{content}_n, \ell_n) \quad \text{type} \in \text{attributes} \]
\[ \text{type} = \text{script} \quad \ell'_n = \kappa \triangleright \text{int} \quad \ell_n \quad \text{node}' = \text{node}[\text{content}_n \leftarrow \text{content}, \ell_n \leftarrow \ell'_n] \]
\[ \text{nodes}' = \text{nodes}[\text{node} \leftarrow \text{node}'] \quad \text{Doc} = \text{Doc}[\text{nodes} \leftarrow \text{nodes}'] \]
\[ \text{EventHandlers}' = \text{registerHandlers}(\text{EventHandlers}, \text{content}) \]
\[ \psi' = \cdot \quad t' = t[D\text{oc} \leftarrow \text{Doc}'][\text{\{EventHandlers} = \text{\text{EventHandlers}'\} ] \]
\[ \sum' = \sum[t \leftarrow t'][\psi \leftarrow \psi'] \]
\[ \text{fresh}(\text{id}_e) \quad e = (\text{id}_e, \text{DOM.scriptLoaded}, (\text{id}_t, \text{id}_d, \text{id}_n), \ell'_n) \]

nextStateC\( (\sum, \text{afterFetched}(\kappa, \text{id}_t, \text{id}_d, \text{id}_n, \text{content})) = \sum' : \)

After fetching the content for a page, the browser is ready to create the page’s DOM tree.

\[ \text{fresh}(\text{id}) \quad \psi' = \text{readyToCreateDoc}(\text{id}_t, \text{id}_d, \text{id}, \text{content}, \kappa) \]
\[ e = (\text{id}, \text{webNavigation.onCommitted}, \text{none}, \text{info}, \kappa) \]
\[ \text{nextState}(\sum, \text{afterFetchedDoc}(\kappa, \text{id}_t, \text{id}_d, \text{id}_n, \text{content})) = \psi' ; e \]

Create the DOM tree

In \text{CreateDoc}(2), a DOM tree is constructed as the browser renders a page. A node could load a single piece of external content (e.g., an image or a text file) or an iframed page. When a node that requires a single piece of external content is created, a corresponding \text{readyToFetch} state is generated as well. The node’s label and the state’s label are computed based on the node’s parent’s label. When an iframe node is created, the system will generate a corresponding \text{readyToFetchDoc} state. The node’s label is computed based on its parent’s label and the iframe policy
set by the parent node. The readyToFetchDoc state’s label is computed merely based on the node’s label. After generating the DOM nodes, and the readyToFetch and readyToFetchDoc states, the document’s status proceeds from DocBegin to DocEnd without loading external objects and subpages.

\[
\Sigma = (\Psi, \text{Tabs} :: t, \text{Ext} \text{Core} \text{Rs}, \cdots) \quad \Psi = \Psi_1 :: \psi
\]

\[
\psi = \text{DocBegin}(\kappa, \text{id}_t, \text{id}_d, \text{content}) \quad (\Psi_2, t') = \text{domTreeCreation}(\text{content}, t)
\]

\[
t' = (\text{id}_t, \text{Docs} :: \text{Doc} \cdots) \quad \text{Doc} = (\text{id}_d, \text{url}, \text{nodes}, \text{DocCSs}, \chi, \ell)
\]

\[
\psi_1 = \text{DocEnd}(\kappa, \text{id}_t, \text{id}_d) \quad \text{DocCS}_1 = \text{injectCSAll}(\text{Exts}, \text{progInjCSs}, \text{id}_t, \text{id}_d, \text{DocEnd})
\]

\[
\text{Doc}' = \text{Doc}[\text{DocCSs} \leftarrow \text{DocCSs} :: \text{DocCS}_1]
\]

\[
t_2 = t'[\text{Doc} \leftarrow \text{Doc}'] \quad \Sigma' = \Sigma[t \leftarrow t_2][\Psi \leftarrow \Psi_1 :: \psi_1 :: \Psi_2]
\]

\[
\text{nextStateC(} (\Sigma, \text{DocBegin}(\kappa, \text{id}_t, \text{id}_d, \text{content})) = \Sigma';
\]

\[
\text{Content Script Injection} \quad \text{When document state changes, both the scripts in the extensions and programatically injected scripts get a chance to be injected to the page. injectCSExts(Exts, id_t, id_d, docState) extracts the content scripts that can be executed in the page with tab ID id_t and Doc ID id_d from extensions Exts. If an extension is active, the content scripts to be injected are extracted from the extension’s static content scripts. If an extension is inactive, none of its content scripts will be injected to the page.}
\]

\[
\text{injectCSAll(Exts, progInjCSs, id_t, id_d, docState) = DocCS}_1 :: \text{DocCS}_2
\]

\[
\text{injectCSExts(\cdot, id_t, id_d, docState)} = \cdot
\]

\[
\text{injectCSExts(Exts, id_t, id_d, docState)} = \text{DocCS}_1 :: \text{DocCS}_2
\]

\[
\text{injectCSExts(Exts :: Ext, id_t, id_d, docState) = DocCS}_1 :: \text{DocCS}_2
\]

\[
\text{Ext = (\cdot, \cdot, ExtCSs, \cdot, \text{active}, \ell) \quad DocCSs = injectCSs(ExtCSs, id_t, id_d, docState)}
\]

\[
\text{injectCSExt(Ext, id_t, id_d, docState)} = \text{DocCSs}
\]

\[
\text{Ext = (\cdot, \cdot, ExtCSs, \cdot, \text{inactive}, \ell)} \quad \text{injectCSExt-inactive}
\]
and id

the value of a specific node property

pointer, and ℓ

ℓ

label for the content stored in the node. In the following, a node contains four labels in its attribute field:

inserting, deleting, and moving node pointers. We distinguish between labels related to the structure of the DOM tree

document

DomGetNodePointer

Scripts can access DOM nodes in the same document. Scripts can refer to one or a list

DOM node details

Scripts can not only read and write DOM nodes but also change the tree structure of DOM by

3.8 Rules for Accessing DOM

3.8.1 Rules for Accessing DOM

DOM node details Scripts can not only read and write DOM nodes but also change the tree structure of DOM by

inserting, deleting, and moving node pointers. We distinguish between labels related to the structure of the DOM tree

and the label for the content stored in the node. In the following, a node contains four labels in its attribute field: ℓ

parent is the label for parent point, ℓ

children the label for the children points, ℓ

pre the label for the previous sibling pointer, and ℓ

succ the label for the succeeding sibling pointer. For a script to change a node’s parent pointer, the script’s label must be lower or equal to the target node’s ℓ

parent.

Node node ::= (id, attributes, nodes, content, ℓ)

Attributes attributes ::= (type, url, ℓ

parent, ℓ

children, ℓ

pre, ℓ

succ, ···)

DomGetNodePointer Scripts can access DOM nodes in the same document. Scripts can refer to one or a list

of elements by attributes (e.g., node ID and tag) through the document.getElementsByTagName API. For example, with “var

myList = document.getElementsByTagName(“p”))”, myList refers to the pointers of the nodes with tag “p”. To get

the value of a specific node property prop of a node, one can use a command like “value = myList[0].prop”, where

myList[0] is the pointer to the target node.

In this rule, we model the document.getElementsByTagName APIs with domAPI DomGetNodePointer(id_t, id_d, query). id_t

and id_d indicate to which tab and doc the caller script belongs. Different document.getElementsByTagName APIs match to
different queries. E.g., for “var myList = document.getElementsByTagName("p");”, query should be “TagName, p”. pointersOf(nodes) denotes the pointers of nodes.

A script could attempt to leak secrets by affecting the return results of such queries. For instance, if a secret script deleted a node with tag “p”, an attacker that used the API to return all pointers to nodes with tag “p” can observe the elements returned and know whether the first script has deleted the element. Mitigate this leak, we assume this is a lable assigned to each query. When the return results change, the label of the query will reflect that change. For instance, there is a global label for elements with tag “p”. When one program with label l₁ deletes an element with tag “p”, then the label for the query is updated to be tainted by the label l₁. In practice, this data structure needs to be build and maintained by the browser runtime.

If the caller’s label is lower than the label of the query, the system returns the matching nodes’ pointers. The caller’s label gets tainted by the matching nodes’ labels. Otherwise, the execution gets stuck.

\[
\begin{align*}
\Sigma_{ctx}(id) &= (\Psi, Tabs :: t_{ctx}(id), \ldots) \\
\ell &= ctxOfl(\Sigma_{ctx}) \Gamma, let \ x = domAPI.getNodePointer(id, id, query) \ in \ cmd \mid id \ | id) \\
\kappa &= \ell' \\
t &= (id, Docs :: Doc, \ldots) \\
Doc &= (id, \ldots) \quad \kappa_Q = labOFL(query, Doc) \quad \kappa_Q = \subseteq \kappa \\
\quad \text{nodes}_1 = QueryNodes(query, Doc) \quad \Sigma_{ctx}(id) = update(\Sigma_{ctx}(id), \kappa_Q \supseteq \kappa) \\
\quad \text{call}(domAPI.getNodePointer, (id, id, query), pointersOf(nodes_1), \kappa_Q) \\
\Sigma_{ctx}' \mid \Gamma, let \ x = domAPI.getNodePointer(id, id, query) \ in \ cmd \mid id \\
\quad \text{DOMGetNodePointer}
\end{align*}
\]

\[
\begin{align*}
\Sigma_{ctx}(id) &= (\Psi, Tabs :: t_{ctx}(id), \ldots) \\
\ell &= ctxOfl(\Sigma_{ctx}) \Gamma, let \ x = domAPI.getNodePointer(id, id, query) \ in \ cmd \mid id \ | id) \\
\kappa &= \ell' \\
t &= (id, Docs :: Doc, \ldots) \\
Doc &= (id, \ldots) \quad \kappa_Q = labOFL(query, Doc) \quad \kappa_Q = \subseteq \kappa \\
\quad \Sigma_{ctx} \mid \Gamma, let \ x = domAPI.getNodePointer(id, id, query) \ in \ cmd \mid id &\rightarrow \text{stuck} \quad \text{DOMGetNodePointer}\$
\]

\text{DomNodeRead} \quad \text{Given a pointer to a node, a property value of the node is read through a command like “value = myList[0].prop”. name is the property name. The system returns the value if the node’s label is lower than \( \kappa \). The caller’s label gets tainted by the node’s label. Or else, the system gets stuck.}

\[
\begin{align*}
\Sigma_{ctx}(id) &= (\Psi, Tabs :: t_{ctx}(id), \ldots) \\
\ell &= ctxOfl(\Sigma_{ctx}) \Gamma, let \ x = domAPI.readNode(id, id, id, name) \ in \ cmd \mid id \mid id) \\
\kappa &= \ell' \\
t &= (id, Docs :: Doc, \ldots) \\
Doc &= (id, \ldots) \quad \text{node} \in \ Doc \quad \text{node} = (id, \ldots, \ell) \quad \ell \subseteq \kappa \\
\quad \text{result} = getPropertyValue(node, name) \quad \Sigma_{ctx}'(id) = update(\Sigma_{ctx}(id), \ell \supseteq \kappa) \\
\quad \text{call}(domAPI.readNode, (id, id, id, name), result, \ell') \quad \Sigma_{ctx}' \mid \Gamma, let \ x = domAPI.readNode(id, id, id, name) \ in \ cmd \mid id \mid id \mid id) &\rightarrow \text{DOMNodeRead}
\end{align*}
\]

\text{DOMNodeWrite(1)} \quad \text{A script is allowed to update the content of a node if its label is lower than the node’s label. In this rule, the script updates the whole node, and can assign the node with a new label which should be lower than the script’s label. DomNodeWrite API does not return any value.}

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\[ \Sigma_{ctx}(id) = (\Psi, \text{Tabs} :: t_{ctx}(id), \cdots) \]
\[ \ell = \text{ctxOfId}(\Sigma_{ctx}, t_{ctx}(id), \text{domAPI}.\text{writeNode}(id_{t}, \ell_{id}, \ell_{n_{t}}, \text{content'}, \kappa_{1}) \mid id, id) \quad \kappa = \ell' \]
\[ t = (id_{t}, \cdots, \text{Docs} :: Doc, \cdots) \]
\[ \text{Doc} = (id_{t}, \ell_{node}, \cdots, \ell_{node}) \quad \text{node} \in \text{nodes} \quad \text{node} = (id_{n}, \cdots, \ell_{node}) \]
\[ \kappa \subseteq \ell_{node} \quad \ell' = (id_{n}, \cdots, \ell_{node}) \]
\[ \text{Doc}' = \text{Doc}[\text{node} = \text{node}'] \quad \ell' = \ell' \text{[Doc} \text{Doc}] \]
\[ \Sigma_{ctx}(id)' = \Sigma_{ctx}(id)[t \leftarrow t'] \quad \text{DOMNODEWRITE(1)} \]

\[ \Sigma_{ctx}(id) = (\Psi, \text{Tabs} :: t_{ctx}(id), \cdots) \]
\[ \ell = \text{ctxOfId}(\Sigma_{ctx}, t_{ctx}(id), \text{domAPI}.\text{writeNode}(id_{t}, \ell_{id}, \ell_{n_{t}}, \text{content'}, \kappa_{1}) \mid id, id) \quad \kappa = \ell' \]
\[ t = (id_{t}, \cdots, \text{Docs} :: Doc, \cdots) \quad \text{Doc} = (id_{t}, \cdots, \text{nodes}, \cdots) \]
\[ (\exists \text{node} \in \text{nodes} \quad \text{node} = (id_{n}, \cdots)) \quad \text{or} \ (\exists \text{node} \in \text{nodes} \quad \text{node} = (id_{n}, \cdots, \ell_{node}) \text{and} \ k \not\subseteq \ell_{node}) \]
\[ \Sigma_{ctx}(id) = \text{DOMNODEWRITE(2)} \]
\[ \Sigma_{ctx}(id) = (\Psi, \text{Tabs} :: t_{ctx}(id), \cdots) \]
\[ \ell = \text{ctxOfId}(\Sigma_{ctx}, \Gamma, \text{domAPI}.\text{getChildren}(id_{t}, \ell_{id}, \ell_{n_{t}}) \text{in cmd} \mid id, id) \]
\[ \kappa = \ell'' \quad t = (id_{t}, \cdots, \text{Docs} :: \text{Doc}, \cdots) \]
\[ \text{Doc} = (id_{t}, \cdots) \quad \text{node} \in \text{Doc} \quad \text{node} = (id_{n}, \cdots, \ell_{children}, \cdots, \cdots, \ell_{n}) \]
\[ \ell_{children} \subseteq k \quad k = \ell_{children} \quad \Sigma_{ctx}(id) = \text{DOMGETCHILDREN} \]
\[ \Sigma_{ctx}(id) = (\Psi, \text{Tabs} :: t_{ctx}(id), \cdots) \]
\[ \ell = \text{ctxOfId}(\Sigma_{ctx}, \Gamma, \text{let} \ x = \text{domAPI}.\text{getParent}(id_{t}, \ell_{id}, \ell_{n_{t}}) \text{in cmd} \mid id, id) \]
\[ \kappa = \ell'' \quad t = (id_{t}, \cdots, \text{Docs} :: \text{Doc}, \cdots) \quad \text{Doc} = (id_{t}, \cdots) \quad \text{node} \in \text{Doc} \quad \text{node} = (id_{n}, \cdots, \ell_{parent}, \cdots, \cdots, \ell_{n}) \]
\[ \ell_{parent} \subseteq k \quad p = \text{parentOf}(id, \ell_{parent}) \quad \Sigma_{ctx}(id) = \text{DOMGETPARENT} \]

**DOMNODEWRITE(2)**  A script fails to write something to a node by assignment. Label check fails, or the target node does not exist. DomNODEWRITE API does not return any value.

**DOMGETCHILDREN**  This API returns the set of pointers of the children of a node. The caller’s label must be lower than or equal to the child point label of the node; otherwise, the program is stuck.

**DOMGETPARENT**  This API returns a node’s parent pointer, if the caller’s label is lower than or equal to the node’s parent pointer label. Otherwise, the execution gets stuck.
**DOMGetPreSibling**  Get a node's previous sibling.

\[
\text{DOMGetPreSibling} \quad \Sigma_{ctx}(id) = (\Psi, \text{Tabs} :: t_{ctx}(id), \ldots)
\]
\[
\ell = \text{ctxOfId}(\Sigma_{ctx}) \Gamma, \text{let } x = \text{domAPI.getPrePreviousSibling}(id_1, id_d, id_n) \text{ in } cmd \| id, id \n\]
\[
\kappa = \ell \quad t = (id, Docs :: Doc :: Doc, \ldots) \quad Doc = (id_d, \ldots)
\]
\[
\text{node} \in \text{Doc} \quad \text{node} = (id_n, (\ldots, \ell_{\text{pre}}, \ldots), \ell_n) \quad \ell_{\text{pre}} \subseteq \kappa \quad p = \text{preSiblingOf}(id_n, \text{Doc})
\]
\[
\Sigma_{ctx}'(id) = \text{update}(\Sigma_{ctx}(id), \ell_{\text{pre}} \triangleright_{\text{ref}} \ell)
\]
\[
\Sigma_{ctx}' \| \Gamma, \text{let } x = \text{domAPI.getPrePreviousSibling}(id_1, id_d, id_n) \text{ in } cmd \| id
\]
\[
\text{call}(\text{domAPI.getPreviousSibling}, \langle id_1, id_d, id_n, p, \ell_{\text{pre}} \rangle) \quad \Sigma_{ctx}' \| \Gamma, cmd[p/x] \| id;
\]

**DOMAppendChildren**  Append a child node to a node \text{node}. \text{node}_1 is the to-be-appended node. \text{node}_1 has a label \ell_1 which can be lower than \kappa. When the \text{domAPI.appendChild} API call is issued, in the rule \text{FIREAPICALL-S2}, we make sure that \text{labOf}(\text{node}_1) is lower than \kappa.

**DOMAppendChildren:** Successfully appends \text{node}_1 to \text{node}. There are three cases: a) the node will not load contents from a server; b) the node will load an external object, for example, an image; c) the node will load a page into an iframe. For case 1b, a \text{readyToFetch} state will be generated. For case 1c, a \text{readyToFetchDoc} state will be generated.

\[
\text{DOMAppendChildren(A)}
\quad \Sigma_{ctx}(id) = (\Psi, \text{Tabs} :: t_{ctx}(id), \ldots)
\quad \ell_1 = \text{ctxOfId}(\Sigma_{ctx}) \| \Gamma, \text{let } x = \text{domAPI.appendChild}(id_1, id_d, id_n, \text{node}_1, \ell_1) \text{ in } cmd \| id, id
\quad \kappa = \ell_1 \quad t = (id_1, \ldots, Docs :: Doc, \ldots)
\quad Doc = (id_d, \ldots, \text{nodes}, \ldots) \quad \text{node} \in \text{nodes} \quad \text{node} = (id_1, (\ldots, \ell_{\text{children}}, \ldots), \text{nodes}_1, \ldots, \ell_n)
\quad \text{node}_1 = (id_1, (\ldots, \ell_{\text{parent}}, \ell_{\text{pre}}, \ldots), \ell_1) \quad \#url \in \text{attributes}
\quad \kappa \subseteq \ell_{\text{children}} \quad \kappa \subseteq \ell_{\text{parent}} \quad \kappa \subseteq \ell_{\text{pre}} \quad \ell_{\text{succ}} = \text{nextSiblingOf}(\text{last}(\text{nodes}_1)) \quad \kappa \subseteq \ell_{\text{succ}}
\quad \text{Doc}' = \text{Doc}[\text{node} \leftarrow \text{append}(\text{node}, \text{node}_1)] \quad t' = t[\text{Doc} \leftarrow \text{Doc}'] \quad \Sigma_{ctx}'(id) = \Sigma_{ctx}(id)[t \leftarrow t']
\]
\[
\Sigma_{ctx}' \| \Gamma, \text{let } x = \text{domAPI.appendChild}(id_1, id_d, id_n, \text{node}_1, \ell_1) \text{ in } cmd \| id
\quad \text{call}(\text{domAPI.appendChild}, \langle id_1, id_d, id_n, \text{node}_1, \ell_1 \rangle, \text{pointersOf}(\text{node}_1), \kappa) \quad \Sigma_{ctx}' \| \Gamma, cmd[\text{pointersOf}(\text{node}_1)/x] \| id;
\]

**DOMAppendChildren(B)**
\[
\Sigma_{ctx}(id) = (\Psi, \text{Tabs} :: t_{ctx}(id), \ldots)
\quad \ell = \text{ctxOfId}(\Sigma_{ctx}) \| \Gamma, \text{let } x = \text{domAPI.appendChild}(id_1, id_d, id_n, \text{node}_1, \ell_1) \text{ in } cmd \| id, id
\quad \kappa = \ell_1 \quad t = (id_1, \ldots, Docs :: Doc, \ldots)
\quad Doc = (id_d, \ldots, \text{nodes}, \ldots) \quad \text{node} \in \text{nodes} \quad \text{node} = (id_1, (\ldots, \ell_{\text{children}}, \ldots), \text{nodes}_1, \ldots, \ell_n)
\quad \text{node}_1 = (id_1, (\ldots, \ell_{\text{parent}}, \ell_{\text{pre}}, \ldots), \ell_1) \quad \#url \in \text{attributes} \quad \#\text{doc} \notin \text{attributes}
\quad \psi_1 = \text{readyToApply}(\kappa, \langle id, id_d, id_n, \text{url} \rangle) \quad \kappa \subseteq \ell_{\text{children}} \quad \kappa \subseteq \ell_{\text{parent}} \quad \kappa \subseteq \ell_{\text{pre}}
\quad \ell_{\text{succ}} = \text{nextSiblingOf}(\text{last}(\text{nodes}_1)) \quad \kappa \subseteq \ell_{\text{succ}} \quad \text{Doc}' = \text{Doc}[\text{node} \leftarrow \text{append}(\text{node}, \text{node}_1)]
\quad t' = t[\text{Doc} \leftarrow \text{Doc}'] \quad \Sigma_{ctx}'(id) = \Sigma_{ctx}(id)[\Psi \leftarrow \psi_1][t \leftarrow t']
\]
\[
\Sigma_{ctx}' \| \Gamma, \text{let } x = \text{domAPI.appendChild}(id_1, id_d, id_n, \text{node}_1, \ell_1) \text{ in } cmd \| id
\quad \text{call}(\text{domAPI.appendChild}, \langle id_1, id_d, id_n, \text{node}_1, \ell_1 \rangle, \text{pointersOf}(\text{node}_1), \kappa) \quad \Sigma_{ctx}' \| \Gamma, cmd[\text{pointersOf}(\text{node}_1)/x] \| id;
\]
3.8.2 Rules for Accessing Bookmarks

In order to access bookmarks, a DOM API function, `appendChild`, can be used to add a child node to a node. The function `appendChild` can be called with the following parameters:

\[
\Sigma_{ctx}(id) = (\Psi, \text{Tabs} :: t_{ctx}(id), \cdots)
\]

let \( \ell = \text{ctxOfId}(\Sigma_{ctx}(id)) \) \( \Gamma \), let \( x = \text{domAPI} \cdot \text{appendChild}(id_1, id_d, id_n, node_1, \ell_1) \) in \( \text{cmd} \mid id, id \)

\[\kappa = \ell_1 \quad t = (id_1, \cdots, Docs :: Doc, \cdots) \quad \text{Doc} = (id_d, \cdots, nodes, \cdots) \]

node \( \in \) nodes  node = (id_n, (\cdots, \ell_{\text{children}}, \cdots), nodes_1, \cdots, \ell_n)  node_1 = (id_1, (\cdots, \ell_{\text{parent}}, \ell_{\text{pre}}, \cdots), \ell_1) \quad \text{url} \in \) attributes

\[\text{“doc”} \in \text{attributes} \quad \psi_1 = \text{readyToFetchDoc}(\kappa, id_1, id_d, id_1, \text{url}) \]

\[\ell = \ell_{\text{children}}^* \quad \kappa \subseteq \ell_{\text{parent}}^* \quad \ell_{\text{pre}}^* \quad \ell_{\text{suc}} = \text{nextSiblingOf}((\text{last}(\text{nodes}_1))) \]

\[\ell' = t'[\text{Doc} \leftarrow \text{Doc}'] \quad \Sigma'_{ctx}(id) = \Sigma_{ctx}(id)[\psi \leftarrow \psi_1][t \leftarrow t']
\]

\[\text{DOMappendChild}(c)
\]

**DomRemoveChild** A script can remove the child node from a node if all labels that need to be updated after the node is removed are lower than or equal to the script's label. That is, the labels of the parent, children, pre-sibling, and next-sibling allow it. Finally, we need to update the query set labels that are affected by the removal of the node. Function `updateQ(Doc, \kappa, node_c)` taints all the labels for queries that are affected by the removal of `node_c`. For instance, if the node removed has a tag “p”, then the label for the query “p” needs to be updated.

\[
\Sigma_{ctx}(id) = (\Psi, \text{Tabs} :: t_{ctx}(id), \cdots)
\]

let \( \ell = \text{ctxOfId}(\Sigma_{ctx}(id)) \) \( \Gamma \), let \( x = \text{domAPI} \cdot \text{removeChild}(id_e, id_d, id_n, node_1, \ell_1) \) in \( \text{cmd} \mid id \)

\[\kappa = \ell_1 \quad t = (id_1, \cdots, Docs :: Doc, \cdots) \quad \text{Doc} = (id_d, \cdots, nodes, \cdots) \quad \text{node} \in \) nodes

node = (id_n, (\cdots, \ell_{\text{children}}, \cdots), nodes_1, \cdots, \ell_n)  node_1 = (id_1, (\cdots, \ell_{\text{parent}}, \ell_{\text{pre}}, \cdots), \ell_1) \quad \text{url} \in \) attributes

\[\text{“doc”} \in \text{attributes} \quad \psi_1 = \text{readyToFetchDoc}(\kappa, id_1, id_d, id_1, \text{url}) \]

\[\ell = \ell_{\text{children}}^* \quad \kappa \subseteq \ell_{\text{parent}}^* \quad \kappa \subseteq \ell_{\text{pre}}^* \quad \ell_{\text{suc}} = \text{nextSiblingOf}((\text{last}(\text{nodes}_1))) \]

\[\ell' = t'[\text{Doc} \leftarrow \text{Doc}'] \quad \Sigma'_{ctx}(id) = \Sigma_{ctx}(id)[\psi \leftarrow \psi_1][t \leftarrow t']
\]

\[\text{DOMRemoveChild}(c)
\]

3.8.2 Rules for Accessing Bookmarks

We adopt multi-level bookmarks. There are 11 methods in the Bookmark API. The first six rules only query the bookmarks by using bookmarkQuery function. The last five rules update the bookmarks using bookmarkWrite function.

**Query bookmarks** First we define an auxiliary function `selectBookmark` to select a bookmark from the set of bookmarks `MBookmarks` based on labels. The selection criteria include: 1) the label should be lower than \( \kappa \); and 2) it is the latest updated one among the `MBookmarks` with lower label than \( \kappa \)(or anything else depending on the implementation). The function `selectBookmark` returns a bookmark that satifies the above conditions. If no matching bookmarks can be found, the function returns NONE.

\[\text{MBookmarks}_1 = (\text{bookmarks}, \kappa_1) \quad \text{MBookmarks}_1 \in \text{MBookmarks} \quad \kappa_1 \subseteq \kappa
\]

\[\forall \text{MBookmarks} \in \text{MBookmarks} \quad s.t. \text{labOf(MBookmarks) } \subseteq \kappa
\]

\[\text{laterUpdated(MBookmarks}_1, \text{MBookmarks}) = \text{true}
\]

\[\text{bookmarks} = \text{selectBookmark(MBookmarks, } \kappa)\]
**BookmarkGet**: Get a set of bookmark items based on their IDs. Given \(MBookmarks\) and \(\kappa\), we first select a bookmark using \(selectBookmark\), then, we query the returned bookmark. The query result is placed in an event that will eventually trigger the callback function for processing the query result.

\[
\Sigma = (\Psi, \ldots, MBookmarks, \ldots) \quad \Psi = \Psi' :: \text{chrome.bookmarks.get}(\kappa, id_{cb}, ids) \\
bookmarks = \text{selectBookmark}(MBookmarks, \kappa) \\
result = \text{bookmarkQuery}(bookmarks, \text{chrome.bookmarks.get}, \text{ids}) \\
fresh(id_e) \quad e = (id_e, id_{cb}, \text{none}, \text{result}, \kappa) \quad \Sigma' = \Sigma[\Psi \leftarrow \Psi'] \\
extStateC(\Sigma, \text{chrome.bookmarks.get}(\kappa, id_{cb}, ids)) = \Sigma'; e
\]

**BookmarkGet**

The rules **BookmarkGetChildren**, **BookmarkGetRecent**, **BookmarkGetTree**, **BookmarkGetSubTree** and **BookmarkSearch** are similar to **BookmarkGet**.

**BookmarkGetChildren**: Given an ID, get a bookmark item’s children.

\[
\Sigma = (\Psi, \ldots, MBookmarks, \ldots) \\
\Psi = \Psi' :: \text{chrome.bookmarks.getChildren}(\kappa, id_{cb}, id) \\
bookmarks = \text{selectBookmark}(MBookmarks, \kappa) \\
result = \text{bookmarkQuery}(bookmarks, \text{chrome.bookmarks.getChildren}, id) \\
fresh(id_e) \quad e = (id_e, id_{cb}, \text{none}, \text{result}, \kappa) \quad \Sigma' = \Sigma[\Psi \leftarrow \Psi'] \\
extStateC(\Sigma, \text{chrome.bookmarks.getChildren}(\kappa, id_{cb}, id)) = \Sigma'; e
\]

**BookmarkGetChildren**

**BookmarkGetRecent**: Retrieves the recently added bookmarks. Returns at most \(number\) bookmark items.

\[
\Sigma = (\Psi, \ldots, MBookmarks, \ldots) \\
\Psi = \Psi' :: \text{chrome.bookmarks.getRecent}(\kappa, id_{cb}, number) \\
bookmarks = \text{selectBookmark}(MBookmarks, \kappa) \\
result = \text{bookmarkQuery}(bookmarks, \text{chrome.bookmarks.getRecent}, number) \\
fresh(id_e) \quad e = (id_e, id_{cb}, \text{none}, \text{result}, \kappa) \quad \Sigma' = \Sigma[\Psi \leftarrow \Psi'] \\
extStateC(\Sigma, \text{chrome.bookmarks.getRecent}(\kappa, id_{cb}, number)) = \Sigma'; e
\]

**BookmarkGetRecent**

**BookmarkGetTree**: Retrieves the entire bookmarks hierarchy.

\[
\Sigma = (\Psi, \ldots, MBookmarks, \ldots) \quad \Psi = \Psi' :: \text{chrome.bookmarks.getTree}(\kappa, id_{cb}) \\
bookmarks = \text{selectBookmark}(MBookmarks, \kappa) \\
result = \text{bookmarkQuery}(bookmarks, \text{chrome.bookmarks.getTree}) \\
fresh(id_e) \quad e = (id_e, id_{cb}, \text{none}, \text{result}, \kappa) \quad \Sigma' = \Sigma[\Psi \leftarrow \Psi'] \\
extStateC(\Sigma, \text{chrome.bookmarks.getTree}(\kappa, id_{cb})) = \Sigma'; e
\]

**BookmarkGetTree**

**BookmarkGetSubTree**: Retrieves the subtrees of bookmark node with ID \(id\).
\[ \Sigma = (\Psi, \ldots, MBookmarks, \ldots) \]
\[ \Psi = \Psi' :: \text{chrome.bookmarks.getSubTree}(\kappa, \text{id}_{cb}, \text{id}) \]
\[ \text{bookmarks} = \text{selectBookmark}(MBookmarks, \kappa) \]
\[ \text{result} = \text{bookmarkQuery}(\text{bookmarks}, \text{chrome.bookmarks.getSubTree}, \text{id}) \]
\[ \text{fresh}(\text{id}_c) \quad e = (\text{id}_c, \text{id}_{cb}, \text{none}, \text{result}, \kappa) \quad \Sigma' = \Sigma[\Psi \leftarrow \Psi'] \]
\[ \text{nextStateC}(\Sigma, \text{chrome.bookmarks.getSubTree}(\kappa, \text{id}_{cb}, \text{id})) = \Sigma'; e \]

**BookmarkSearch**: Searches for BookmarkTreeNodes that match with a given query.

\[ \Sigma = (\Psi, \ldots, MBookmarks, \ldots) \quad \Psi = \Psi' :: \text{chrome.bookmarks.search}(\kappa, \text{id}_{cb}, \text{query}) \]
\[ \text{bookmarks} = \text{selectBookmark}(MBookmarks, \kappa) \]
\[ \text{result} = \text{bookmarkQuery}(\text{bookmarks}, \text{chrome.bookmarks.search}, \text{query}) \]
\[ \text{fresh}(\text{id}_c) \quad e = (\text{id}_c, \text{id}_{cb}, \text{none}, \text{result}, \kappa) \quad \Sigma' = \Sigma[\Psi \leftarrow \Psi'] \]
\[ \text{nextStateC}(\Sigma, \text{chrome.bookmarks.search}(\kappa, \text{id}_{cb}, \text{query})) = \Sigma'; e \]

**Update bookmarks** The APIs that update bookmarks will only update one of the bookmark trees in the multi-level bookmarks. If API caller’s simple label exactly matches one bookmark tree, then that bookmark tree will be updated. Otherwise, the selectBookmark will be called to select the closest one to be updated.

**BookmarkCreate(1)**: Add a new bookmark item under a directory with ID \( \text{id}_{parent} \). \( \text{positionIndex} \) is the new item’s position index. \( \text{title} \) is the bookmark item title. \( \text{url} \) is the URL. There is a copy of MBookmark \( MBookmarks \) in \( MBookmarks \) with the same label as the caller’s label. In this case, we directly update MBookmark. If MBookmark does not contain a directory with ID \( \text{id}_{parent} \), we set \( \text{result} \) as void; else, \( \text{result} \) contains \( \text{id}_{parent}, \text{positionIndex}, \text{title}, \text{url} \).

\[ \Sigma = (\Psi, \ldots, MBookmarks, \ldots) \]
\[ \Psi = \Psi' :: \text{chrome.bookmarks.create}(\kappa, \text{id}_{cb}, (\text{id}_{parent}, \text{positionIndex}, \text{title}, \text{url})) \]
\[ MBookmarks = MBookmarks'' :: (\text{bookmarks}, \kappa) \]
\[ (\text{bookmarks}', \text{result}) = \text{bookmarkWrite}(\text{bookmarks}, \text{chrome.bookmarks.create}, (\text{id}_{parent}, \text{positionIndex}, \text{title}, \text{url})) \]
\[ \text{fresh}(\text{id}_c) \quad e = (\text{id}_c, \text{id}_{cb}, \text{none}, \text{result}, \kappa) \quad MBookmarks' = MBookmarks'' :: (\text{bookmark}', \kappa) \]
\[ \Sigma' = \Sigma[\Psi \leftarrow \Psi'][MBookmarks \leftarrow MBookmarks'] \]
\[ \text{nextStateC}(\Sigma, \text{chrome.bookmarks.create}(\kappa, \text{id}_{cb}, (\text{id}_{parent}, \text{positionIndex}, \text{title}, \text{url}))) = \Sigma'; e \]

**BookmarkCreate(2)**: There does not exist a MBookmark with label \( \kappa \). We select a MBookmark \( MBookmarks \) through selectBookmark(MBookmarks, \kappa), and then generate a new MBookmark \( MBookmarks' \) from \( MBookmarks \), by replacing its label with \( \kappa \). Then we add a new bookmark item to \( MBookmarks' \). The result of the write operation will be returned through \( \text{result} \).
$\Sigma = (\Psi, \ldots, MBookmarks, \ldots)$

$\Psi = \Psi' :: \text{chrome.bookmarks.create}(\kappa, \text{id}_{cb}, (\text{id}_{parent}, \text{positionIndex}, \text{title}, \text{url}))$

$\nexists \text{MBookmark} \in \text{MBookmarks} \text{ s.t. labOf(} \text{MBookmark} \text{)} = \kappa$

$\text{bookmarks}_1 = \text{selectBookmark}(\text{MBookmarks}, \kappa)$

$(\text{bookmarks}_1', \text{result}) = \text{bookmarkWrite}(\text{bookmarks}_1, \text{chrome.bookmarks.create},$

$(\text{id}_{parent}, \text{positionIndex}, \text{title}, \text{url}))$

$\text{fresh}(\text{id}_e)$

$e = (\text{id}_e, \text{id}_{cb}, \text{none}, \text{result}, \kappa) \quad \text{MBookmarks}' = \text{MBookmarks} :: (\text{bookmarks}_1', \kappa)$

$\Sigma' = \Sigma[\Psi \leftarrow \Psi'][\text{MBookmarks} \leftarrow \text{MBookmarks}']$

$\text{nextStateC}(\Sigma, \text{chrome.bookmarks.create}(\kappa, \text{id}_{cb}, (\text{id}_{parent}, \text{positionIndex}, \text{title}, \text{url}))) = \Sigma'; e$

The rules \text{BookmarkMove}(1), \text{BookmarkUpdate}(1), \text{BookmarkRemove}(1), \text{BookmarkRemoveTree}(1) are similar to the rule \text{BookmarkCreate}(1).

The rules \text{BookmarkMove}(2), \text{BookmarkUpdate}(2), \text{BookmarkRemove}(2), \text{BookmarkRemoveTree}(2) are similar to the rule \text{BookmarkCreate}(2).

\text{BookmarkMove}:\text{ Moves the specified BookmarkTreeNode to the provided location.}

$\Sigma = (\Psi, \ldots, MBookmarks, \ldots)$

$\Psi = \Psi' :: \text{chrome.bookmarks.move}(\kappa, \text{id}_{cb}, (\text{id}, \text{id}_{parent}, \text{positionIndex}))$

$\text{MBookmarks} = \text{MBookmarks}'' :: (\text{bookmarks}, \kappa)$

$(\text{bookmarks}', \text{result}) = \text{bookmarkWrite}(\text{bookmarks}, \text{chrome.bookmarks.move},$

$(\kappa, \text{id}_{cb}, (\text{id}, \text{id}_{parent}, \text{positionIndex})))$

$\text{fresh}(\text{id}_e)$

$e = (\text{id}_e, \text{id}_{cb}, \text{none}, \text{result}, \kappa) \quad \text{MBookmarks}' = \text{MBookmarks}'' :: (\text{bookmarks}', \kappa)$

$\Sigma' = \Sigma[\Psi \leftarrow \Psi'][\text{MBookmarks} \leftarrow \text{MBookmarks}']$

$\text{nextStateC}(\Sigma, \text{chrome.bookmarks.move}(\kappa, \text{id}_{cb}, (\text{id}, \text{id}_{parent}, \text{positionIndex}))) = \Sigma'; e$

\text{BookmarkMove}(1)

$\Sigma = (\Psi, \ldots, MBookmarks, \ldots)$

$\Psi = \Psi' :: \text{chrome.bookmarks.move}(\kappa, \text{id}_{cb}, (\text{id}, \text{id}_{parent}, \text{positionIndex}))$

$\nexists \text{MBookmark} \in \text{MBookmarks} \text{ s.t. labOf(} \text{MBookmark} \text{)} = \kappa$

$\text{bookmarks}_1 = \text{selectBookmark}(\text{MBookmarks}, \kappa)$

$(\text{bookmarks}_1', \text{result}) = \text{bookmarkWrite}(\text{bookmarks}_1, \text{chrome.bookmarks.move},$

$(\kappa, \text{id}_{cb}, (\text{id}, \text{id}_{parent}, \text{positionIndex})))$

$\text{fresh}(\text{id}_e)$

$e = (\text{id}_e, \text{id}_{cb}, \text{none}, \text{result}, \kappa) \quad \text{MBookmarks}' = \text{MBookmarks} :: (\text{bookmarks}_1', \kappa)$

$\Sigma' = \Sigma[\Psi \leftarrow \Psi'][\text{MBookmarks} \leftarrow \text{MBookmarks}']$

$\text{nextStateC}(\Sigma, \text{chrome.bookmarks.move}(\kappa, \text{id}_{cb}, (\text{id}, \text{id}_{parent}, \text{positionIndex}))) = \Sigma'; e$

\text{BookmarkMove}(2)

\text{BookmarkUpdate}: \text{ Updates the properties of a bookmark or folder. Specify only the properties that you want to change; unspecified properties will be left unchanged. Note: Currently, only 'title' and 'url' are supported.}
The **chrome.bookmarks.remove** API removes a bookmark or an empty bookmark folder.

The **chrome.bookmarks.removeTree** API recursively removes a bookmark folder.
3.8.3 Rules for Accessing Cookies

The cookies can be set by server through the HTTP response header. In each web request, the browser sends all the cookies in the same domain to the web server, no matter whether the cookies were set by the server or client-side scripts. The httpOnly cookies cannot be accessed by client-side scripts including page scripts, extensions etc. A cookie for domain url always has a label $\kappa = \text{labFrom}(\text{url})$.

CookieWebsiteSet(1): An web site updates an existing cookie item’s value. We don’t need label checking here because $\kappa = \text{labFrom}(\text{url})$ and $\text{labFrom}(\text{url})$ is the cookie’s label.

$$
\Sigma = (\Psi, \ldots, \text{Cookies}, \ldots) \quad \Psi = \Psi' :: \text{website.cookieSet}(\kappa, \text{id}_c, \text{name, value, url}) \quad \text{Cookie} \in \text{Cookies} \\
\text{Cookie} = (\text{name, value}, \text{url, } \kappa) \quad \text{Cookie}' = \text{Cookie}[\text{value} \leftarrow \text{value}] \\
\text{Cookies}' = \text{Cookies} \ni \text{Cookie} \leftarrow \text{Cookie}' \quad \Sigma' = \Sigma[\Psi \leftarrow \Psi'][\text{Cookies} \leftarrow \text{Cookies}'] \\
\text{fresh}(\text{id}_c) \quad e = (\text{id}_c, \text{id}_c, \text{none, result, } \kappa) \quad \text{nextStateC}(\Sigma, \text{website.cookieSet}(\kappa, \text{id}_c, (\text{name, value, url}))) = \Sigma'; e
$$

CookieWebsiteSet(2): An web site sets a new cookie item.

$$
\Sigma = (\Psi, \ldots, \text{Cookies}, \ldots) \quad \Psi = \Psi' :: \text{website.cookieSet}(\kappa, \text{id}_c, (\text{name, value, url})) \\
\exists \text{Cookie} \in \text{Cookies} \ni \text{Cookie} = (\text{name, value}, \text{url, } \cdot) \quad \text{Cookie} = (\text{name, value}, \text{url, } \kappa) \\
\text{Cookies}' = \text{Cookies} \ni \text{Cookie} \quad \Sigma' = \Sigma[\Psi \leftarrow \Psi'][\text{Cookies} \leftarrow \text{Cookies}'] \\
\text{fresh}(\text{id}_c) \quad e = (\text{id}_c, \text{id}_c, \text{none, info(\text{Cookie}), } \kappa) \quad \text{nextStateC}(\Sigma, \text{website.cookieSet}(\kappa, \text{id}_c, (\text{name, value, url}))) = \Sigma'; e
$$
CookieWebsiteGet(1): In each HTTP web request header, the cookies that belong to the same domain are attached. By default, \( \text{labFrom}(url) \subseteq \kappa \). There is no callback function for “get cookie” commands in HTTP headers. Seems this rule is useless.

\[
\Sigma = (\Psi, \cdots, \text{Cookies}, \cdots) \quad \Psi = \Psi' :: \text{website.cookieGet}(\kappa, url) \\
\text{Cookies} = \text{Cookies}_1 :: \text{Cookies}_2 \\
\forall \text{Cookie} \in \text{Cookies}_1, \text{Cookie} = (\cdot, \cdot, url, \cdot) \\
\n\text{nextStateC}(\Sigma, \text{website.cookieGet}(\kappa, url)) = \Sigma'; e \quad \text{COOKIEWEBSITEGET(1)}
\]


\[
\Sigma = (\Psi, \cdots, \text{Cookies}, \cdots) \\
\Psi = \Psi' :: \text{domAPI.cookieSet}(\kappa, id_{cb}, (name, value, url)) \\
\text{Cookie} \in \text{Cookies} \\
\text{Cookie} = (\text{name}, \text{value}, \text{url}, \kappa_c) \quad \kappa \subseteq \kappa_c \\
\text{Cookie}' = \text{Cookie}[\text{value}, \cdot = \text{value}] \\
\text{Cookies}' = \text{Cookies}(\text{Cookie} \leftarrow \text{Cookie}') \\
\text{nextStateC}(\Sigma, \text{domAPI.cookieSet}(\kappa, id_{cb}, (name, value, url))) = \Sigma'; e \quad \text{COOKIESCRIPTSET(1)}
\]

CookieScriptSet(2): The label checking fails. The target cookie keeps unchanged.

\[
\Sigma = (\Psi, \cdots, \text{Cookies}, \cdots) \\
\Psi = \Psi' :: \text{domAPI.cookieSet}(\kappa, id_{cb}, (name, value, url)) \\
\text{Cookie} \in \text{Cookies} \\
\text{nextStateC}(\Sigma, \text{domAPI.cookieSet}(\kappa, id_{cb}, (name, value, url))) = \Sigma'; e \quad \text{COOKIESCRIPTSET(2)}
\]

CookieScriptSet(3): A script creates a new cookie item.

\[
\Sigma = (\Psi, \cdots, \text{Cookies}, \cdots) \\
\Psi = \Psi' :: \text{domAPI.cookieSet}(\kappa, id_{cb}, (name, value, url)) \\
\text{Cookie} \in \text{Cookies} \\
\text{nextStateC}(\Sigma, \text{domAPI.cookieSet}(\kappa, id_{cb}, (name, value, url))) = \Sigma'; e \quad \text{COOKIESCRIPTSET(3)}
\]

CookieScriptSet(4): A script fails to create a new cookie item.

\[
\Sigma = (\Psi, \cdots, \text{Cookies}, \cdots) \\
\Psi = \Psi' :: \text{domAPI.cookieSet}(\kappa, id_{cb}, (name, value, url)) \\
\text{nextStateC}(\Sigma, \text{domAPI.cookieSet}(\kappa, id_{cb}, (name, value, url))) = \Sigma'; e \quad \text{COOKIESCRIPTSET(4)}
\]
CookieScriptGet(1) Get a cookie.

\[
\Sigma = (\Psi, \ldots, \text{Cookies,} \ldots) \quad \Psi = \Psi' :: \text{domAPI.cookieGet}(\kappa, id_{cb}, (name, url))
\]
\[
\text{Cookie} \in \text{Cookies} \quad \text{Cookie} = (\text{name, value, url, } \kappa_c)
\]
\[
\kappa_c \subseteq \kappa \\
\Sigma' = \Sigma[\Psi \leftarrow \Psi']
\]
\[
fresh(id_e) \quad e = (id_e, id_{cb}, \text{none, Cookie, } \kappa)
\]
\[
\text{nextStateC}(\Sigma, \text{domAPI.cookieGet}(\kappa, id_{cb}, (name, url))) = \Sigma'; e
\]

CookieScriptGet(2) Fail to get a cookie as the target cookie does not exist.

\[
\Sigma = (\Psi, \ldots, \text{Cookies,} \ldots) \quad \Psi = \Psi' :: \text{domAPI.cookieGet}(\kappa, id_{cb}, (name, url))
\]
\[
\exists \text{Cookie} \in \text{Cookies} \text{ s.t. } \text{Cookie} = (\text{name, } _, \text{url, } _) \\
\Sigma' = \Sigma[\Psi \leftarrow \Psi']
\]
\[
\text{nextStateC}(\Sigma, \text{domAPI.cookieGet}(\kappa, id_{cb}, (name, url))) = \Sigma';
\]

CookieScriptGet(3) Fail to get a cookie due to the label checking.

\[
\Sigma = (\Psi, \ldots, \text{Cookies,} \ldots) \quad \Psi = \Psi' :: \text{domAPI.cookieGet}(\kappa, id_{cb}, (name, url))
\]
\[
\text{Cookie} \in \text{Cookies} \quad \text{Cookie} = (\text{name, value, url, } \kappa_c) \\
\kappa_c \nsubseteq \kappa \\
\Sigma' = \Sigma[\Psi \leftarrow \Psi']
\]
\[
\text{nextStateC}(\Sigma, \text{domAPI.cookieGet}(\kappa, id_{cb}, (name, url))) = \Sigma';
\]

CookieCoreGet Extension core gets a cookie by (url, name, storeID). The browser return the cookie. Similar to COOKIESCRIPTRULES.

CookieCoreSet Extension core set cookie with url, name. The rules are similar to COOKIESCRIPTRULES rules.

CookieCoreGetAll Extension core gets a cookie with the parameters. The browser return the cookie, taint the label the extension core with the label of the cookies.

\[
\Sigma = (\Psi, \ldots, \text{Cookies,} \ldots) \quad \Psi = \Psi' :: \text{chrome.cookies.getAll}(\kappa, id_{cb}, \text{filter})
\]
\[
\forall \text{Cookie} \in \text{Cookies, Cookie} = (_{\ldots,} \kappa_c) \\
\text{if matchFilter(} \text{Cookie, } \text{filter} = \text{true} \land \kappa_c \nsubseteq \kappa
\]
\[
\text{Add Cookie to Cookies_results} \\
\Sigma' = \Sigma[\Psi \leftarrow \Psi']
\]
\[
fresh(id_e) \quad e = (id_e, id_{cb}, \text{none, Cookies_results, } \kappa)
\]
\[
\text{nextStateC}(\Sigma, \text{chrome.cookies.getAll}(\kappa, id_{cb}, \text{filter})) = \Sigma'; e
\]

CookieCoreRemove(1) Extension core removes a cookie with name and url. The callback function can access the removed cookie.

\[
\Sigma = (\Psi, \ldots, \text{Cookies,} \ldots) \quad \Psi = \Psi' :: \text{chrome.cookies.remove}(\kappa, id_{cb}, (name, url))
\]
\[
\text{Cookies} = \text{Cookies}' :: \text{Cookie} \\
\text{Cookie} = (\text{name, } _, \text{url, } \kappa_c) \\
\kappa \nsubseteq \kappa_c \\
\Sigma' = \Sigma[\Psi \leftarrow \Psi'][\text{Cookies} \leftarrow \text{Cookies'}]
\]
\[
fresh(id_e) \quad e = (id_e, id_{cb}, \text{none, Cookie, } \kappa_c)
\]
\[
\text{nextStateC}(\Sigma, \text{chrome.cookies.remove}(\kappa, id_{cb}, (name, url))) = \Sigma'; e
\]

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CookieCoreRemove(2)  The target cookie does not exist.

$$\Sigma = (\Psi, \ldots, \text{Cookies}, \ldots) \quad \Psi = \Psi' :: \text{chrome.cookies.remove}(\kappa, \text{id}_{cb}, (\text{name}, \text{url}))$$

$$\not\exists \text{Cookie} \in \text{Cookies} \text{ s.t. } \text{Cookie} = (\text{name}, \ldots, \text{url}, \ldots) \quad \Sigma' = \Sigma[\Psi \leftarrow \Psi']$$

$$\text{nextStateC}(\Sigma', \text{chrome.cookies.remove}(\kappa, \text{id}_{cb}, (\text{name}, \text{url}))) = \Sigma';$$

CookieCoreRemove(3)  Extension core fails to remove a cookie with name and url due to the label checking.

$$\Sigma = (\Psi, \ldots, \text{Cookies}, \ldots) \quad \Psi = \Psi' :: \text{chrome.cookies.remove}(\kappa, \text{id}_{cb}, (\text{name}, \text{url}))$$

$$\exists \text{Cookie} := \text{Cookies} \quad \kappa \not\subseteq \kappa_c \quad \Sigma' = \Sigma[\Psi \leftarrow \Psi']$$

$$\text{nextStateC}(\Sigma', \text{chrome.cookies.remove}(\kappa, \text{id}_{cb}, (\text{name}, \text{url}))) = \Sigma';$$

3.8.4 Rules for Accessing History

historySearch  Searches the history for the last visit time of each page matching the query.

$$\Sigma = (\Psi, \ldots, \text{histories}, \ldots)$$

$$\Psi = \Psi' :: \text{chrome.history.search}(\kappa, \text{id}_{cb}, \text{query}) \quad \text{histories} = \text{histories}_1 :: \text{histories}_2$$

$$\forall \text{history} \in \text{histories}_1, \text{history} = (\text{id}, \text{url}, \text{name}, \text{visitTime}, \text{visitType}, \kappa_h)$$

$$\text{matchQuery}(\text{history}, \text{query}) = \text{true}$$

$$\kappa_h \subseteq \kappa$$

$$\not\exists \text{history}' \in \text{histories}, \text{history}' = (\text{id}', \text{url}, \text{name}, \text{visitTime}', \text{visitType}', \kappa_h'), \text{history}' \neq \text{history}'$$

$$\text{s.t. } \text{visitTime}' \text{ is later than } \text{visitTime} \land \kappa_h' \subseteq \kappa$$

$$\forall \text{history} \in \text{histories}_2, \text{history} = (\text{id}, \text{url}, \text{name}, \text{visitTime}, \text{visitType}, \kappa_h)$$

$$\text{matchQuery}(\text{history}, \text{query}) = \text{true}$$

$$\kappa_h \subseteq \kappa$$

$$\exists \text{history}' \in \text{histories}_1, \text{history}' = (\text{id}', \text{url}, \text{name}, \text{visitTime}', \text{visitType}', \kappa_h'),$$

$$\text{s.t. } \text{visitTime}' \text{ is later than } \text{visitTime} \land \kappa_h' \subseteq \kappa$$

$$\Sigma' = \Sigma[\Psi \leftarrow \Psi'] \quad \text{fresh}(\text{id}_e) \quad e = (\text{id}_e, \text{id}_{cb}, \text{none}, \text{histories}_1, \kappa)$$

$$\text{nextStateC}(\Sigma, \text{chrome.history.search}(\kappa, \text{id}_{cb}, \text{query})) = \Sigma'; e$$

If the user visit a page for n times, the browser will generate n history items with the same url and name. For each page, we put its latest history item into histories1, the rests are in histories2. Line 3-7 say that any item in histories1 is fresher than any other record for the same page. Line 8-12 are to ensure that histories1 contains all pages’s latest history record items.

historyGetVisits:  Retrieves information about visits to a URL.

$$\Sigma = (\Psi, \ldots, \text{histories}, \ldots)$$

$$\Psi = \Psi' :: \text{chrome.history.getVisits}(\kappa, \text{id}_{cb}, \text{url}) \quad \text{histories} = \text{histories}_1 :: \text{histories}_2$$

$$\forall \text{history} \in \text{histories}_1$$

$$\text{history} = (\ldots, \text{url}, \ldots, \ldots, \kappa_h)$$

$$\kappa_h \subseteq \kappa$$

$$\not\exists \text{history} \in \text{histories}_2, \text{s.t. } \text{history} = (\ldots, \text{url}, \ldots, \ldots, \kappa_h) \land \kappa_h \subseteq \kappa$$

$$\Sigma' = \Sigma[\Psi \leftarrow \Psi'] \quad \text{fresh}(\text{id}_e) \quad e = (\text{id}_e, \text{id}_{cb}, \text{none}, \text{histories}_1, \kappa)$$

$$\text{nextStateC}(\Sigma, \text{chrome.history.getVisits}(\kappa, \text{id}_{cb}, \text{url})) = \Sigma'; e$$
**historyAddUrl:** Adds a URL to the history at the current time.

\[
\Sigma = (\Psi, \ldots, \text{histories}, \ldots)
\]
\[
\Psi = \Psi' :: \text{chrome.history.addUrl}(\kappa, \text{id}_{cb}, (\text{name}, \text{url}, \text{visitTime}, \text{visitType}))
\]
\[
\text{histories}' = \text{histories} :: \text{history}
\]
\[
fresh(id) \quad \text{history} = (id, \text{url}, \text{name}, \text{visitTime}, \text{visitType}, \kappa)
\]
\[
\Sigma' = \Sigma[\Psi \leftarrow \Psi'][\text{histories} \leftarrow \text{histories}'] \quad fresh(id_e) \quad e = (id_e, \text{id}_{cb}, \text{none}, \text{history}, \kappa)
\]
\[
\text{nextStateC}(\Sigma, \text{chrome.history.addUrl}(\kappa, \text{id}_{cb}, (\text{name}, \text{url}, \text{visitTime}, \text{visitType}))) = \Sigma'; e
\]

**historyDeleteUrl:** Removes all occurrences of the given URL from the history. We delete all the matching items which has a label higher than \(\kappa\). In the callback event, we return void instead of the deleted high history items.

\[
\Sigma = (\Psi, \ldots, \text{histories}, \ldots)
\]
\[
\Psi = \Psi' :: \text{chrome.history.deleteUrl}(\kappa, \text{id}_{cb}, \text{url}) \quad \text{histories} = \text{histories}_1 :: \text{histories}_2
\]
\[
\forall \text{history} \in \text{histories}_1
\]
\[
\text{history} = (\ldots, \text{url}, \ldots, \ldots, \kappa_h)
\]
\[
\kappa \sqsubseteq \kappa_h
\]
\[
\exists \text{history} \in \text{histories}_2, \text{s.t.} \text{history} = (\ldots, \text{url}, \ldots, \ldots, \kappa_h) \wedge \kappa \sqsubseteq \kappa_h
\]
\[
\Sigma' = \Sigma[\Psi \leftarrow \Psi'][\text{histories} \leftarrow \text{histories}_2]
\]
\[
fresh(id_e) \quad e = (id_e, \text{id}_{cb}, \text{none}, \text{void}, \kappa)
\]
\[
\text{nextStateC}(\Sigma, \text{chrome.history.deleteUrl}(\kappa, \text{id}_{cb}, \text{url})) = \Sigma'; e
\]

### 3.9 Asynchronous APIs Calls

Asynchronous calls are encoded using `nextStateC` function.

#### 3.9.1 Web Request API Calls

\[
\Sigma = (\Psi, \ldots) \quad \Psi = \Psi' :: \text{webRequestGet}(\kappa, \text{id}_{cb}, \text{info}, \text{url})
\]
\[
fresh(id_e) \quad e = (id_e, \text{webRequest.onBeforeRequest}, \text{none}, \text{info}, \kappa)
\]
\[
\psi' = \text{ws.beforeRequest}(\kappa, id_{cb}, id_e, \text{info}, \text{url}) \quad \Sigma' = \Sigma[\Psi \leftarrow \Psi' :: \psi]
\]
\[
\text{nextStateC}(\Sigma, \text{webRequestGet}(\kappa, \text{id}_{cb}, \text{info}, \text{url})) = \Sigma'; e
\]

#### 3.9.2 Messaging

The sending message APIs are asynchronous. The argument of the callback function is the response from the recipient of the message. Therefore, the browser needs to keep track of pairs of sending and receiving event handlers. The return fields of events and event handlers are used for this purpose. The return field in an event indicates that the browser’s state should change once the event handler that processes this event finishes. Rules RETURN-PAGE, RETURN-CS, RETURN-CC generate such a browser state.

**Messaging asynchronous API call example** In general asynchronous API calls, the triggered events do not contain return channels. However, the events triggered by messaging asynchronous API calls might contain return channels. Here is an example, suppose a content script wants to send a message to an extension core, it calls the API chrome.runtime.sendMessage through FIREAPICALL-A-CS with a callback function to address the core’s reply. The browser generates a state chrome.runtime.sendMessage(\(\kappa, \text{id}_{cb}, (\text{id}, \text{id}_{ext}, \text{message})\)), where \(\kappa\) and \(\text{id}\) are the content script’s simple label and ID respectively, \(\text{id}_{cb}\) is the callback handler’s event type, \(\text{id}_{ext}\) is the target extension’s
ID, and message is the message. In CSToCORE1, the chrome.runtime.sendMessage(\(\kappa, id_{cb}, (id, id_{ext}, message)\)) state is processed by issuing an event
\[ e = (id_e, \text{chrome.runtime.onMessage, some(chrome.runtime.sendMessage, id_{cb}), (id, id_{ext}, message), } \kappa). \]
Then the state chrome.runtime.sendMessage(\(\kappa, id_{cb}, (id, id_{ext}, message)\)) is replaced with the chrome.runtime.sendMessage.waitResponse(\(\kappa, id_{cb}\)) state which indicates there is content script waiting for a reply to be handled by an event handler with event type \(id_{cb}\). The event \(e\) contains a return channel:
\[ \text{some(chrome.runtime.sendMessage, id_{cb})}. \]
With EVENTFIRE2, the event \(e\) is added to all the chrome.runtime.onMessage handlers in the target extension core. Each handler may return a reply to the content script. However, only the first reply will be accepted by the browser and then be passed to the content script. When a response is sent by the core (as modeled by RETURN-CORE), a new state chrome.runtime.sendMessage.ResponseGenerated(\(\kappa, id_{cb}, response\)) is generated and added into the browser. Now there are two states related to the chrome.runtime.sendMessage API call, namely chrome.runtime.sendMessage.waitResponse(\(\kappa, id_{cb}\)) and chrome.runtime.sendMessage.ResponseGenerated(\(\kappa, id_{cb}, response\)). Then the browser knows a response has been sent by the target extension core, the internal transition rule CSToCORE2 is applied, and a callback event
\[ e = (id_e, id_{cb}, \text{none, response, } \kappa) \]
is issued. The callback events carries the core’s response. Finally, the content script’s callback handler receives the callback event and gets the core’s response.

CSToCore  Content script sends a message to extension core, it may also have a callback function to deal with the core’s response. \(id\) is the message sender’s ID.

\[
\begin{align*}
\Sigma &= (\Psi, \ldots) \\
\Psi &= \Psi' :: \text{chrome.runtime.sendMessage}(\kappa, id_{cb}, (id, id_{ext}, message)) &\text{fresh}(id_e) \\
e &= (id_e, \text{chrome.runtime.onMessage, some(chrome.runtime.sendMessage, id_{cb}), (id, id_{ext}, message), } \kappa) \\
\psi' &= \text{chrome.runtime.sendMessage.waitResponse}(\kappa, id_{cb}) \\
\psi' &\sim_{nb} e \\
\Sigma' &= \Sigma[\Psi \leftarrow \Psi' :: \psi'] \\
\text{nextStateC}(\Sigma, \text{chrome.runtime.sendMessage}(\kappa, id_{cb}, (id, id_{ext}, message))) &= \Sigma'; e \quad \text{CSToCORE1}
\end{align*}
\]

After the receiving the response, the state regarding the messaging will be removed, and a callback event will be issued.

\[
\begin{align*}
\Sigma &= (\Psi, \ldots) \\
\Psi &= \Psi' :: \text{chrome.runtime.sendMessage.waitResponse}(\kappa, id_{cb}) &\text{fresh}(id_e) \\
\psi' &= \text{chrome.runtime.sendMessage.waitResponse}(\kappa, id_{cb}) \cdot \text{ResponseGenerated}(\kappa, id_{cb}, response) \\
\Sigma' &= \Sigma[\Psi \leftarrow \Psi'] \\
\text{nextStateC}(\Sigma, \text{chrome.runtime.sendMessage.waitResponse}(\kappa, id_{cb}, (id, id_{ext}, message))) &= \Sigma'; e \quad \text{CSToCORE2}
\end{align*}
\]

CoreToCS: The rules are for one-time messaging from core to content scripts. In CoreToCS1, when a message event is sent from core, the state is changed to “waitResponse”. The same, there is no callback event triggered in this rule. \(id_1\) is the specific and unique event type for the callback event.

\[
\begin{align*}
\Sigma &= (\Psi, \ldots) \\
\Psi &= \Psi' :: \text{chrome.tabs.sendMessage}(\kappa, id_{cb}, (id_{ext}, id_1, message)) &\text{fresh}(id_e) \\
e &= (id_e, \text{chrome.runtime.onMessage, some(chrome.tabs.sendMessage, id_{cb}), (id_{ext}, id_1, message), } \kappa) \\
\psi' &= \text{chrome.tabs.sendMessage}(\kappa, id_{cb}, (id_{ext}, id_1, message)).\text{WaitResponse} \\
\psi' &\sim_{nb} e \\
\Sigma' &= \Sigma[\Psi \leftarrow \Psi' :: \psi'] \\
\text{nextStateC}(\Sigma, \text{chrome.tabs.sendMessage}(\kappa, id_{cb}, (id_{ext}, id_1, message))) &= \Sigma'; e \quad \text{CoreToCS1}
\end{align*}
\]
In `CoreToCS2`, the content script event handlers for the `chrome.runtime.onMessage` event have return a response (or none). And upon getting the response, the browser change the state to “responseGenerated”.

\[
\Sigma = (\Psi, \cdots)
\]
\[
\Psi = \Psi : chrome.tabs.sendMessage.waitForResponse(\kappa, id_e, id_c, (id_e, id_c, response))
\]
\[
fresh(id_e)\quad e = (id_e, id_c, none, response, \kappa)\quad \Sigma' = \Sigma[\Psi \leftarrow \Psi']
\]
\[
\text{nextStateC}(\Sigma, chrome.tabs.sendMessage.ResponseGenerated(\kappa, id_e, response)) = \Sigma'; e \quad \text{CoreToCS2}
\]

### 3.9.3 Chrome Tabs APIs

**Create a new blank tabs** When a user or an extension creates a new blank tab, a new tab \( t \) with fresh ID \( id_e \) is added to system state \( S \). The tab creation triggers an event \( e \). The parameters of `chrome.tabs.create` include `windowId`, `index` (optional integer), `url`, `active` (optional boolean), `pinned` (optional boolean), `openTabId` (optional integer). The extensions create a new tab explicitly through `chrome.tabs.create` API. And we assume that, when receiving a user’s command, the handler `UI` also generates code `chrome.tabs.create`. \( id_w \) is window ID.

\[
\Sigma = (\Psi, Tabs, Exts :: Ext, ExtCoreRs, \cdots)
\]
\[
\Psi = \Psi : chrome.tabs.create(\kappa, id_e, (id_e, positionIndex, activeFlag, pinnedBoolean))
\]
\[
fresh(id_e, id_c, id_e)\quad t = (id_e, \cdots, EmptyUrl, activeFlag, pinnedBoolean)
\]
\[
e_1 = (id_e, tabs.onCreated, none, (id_e, positionIndex, id_w, EmptyUrl, \kappa)
\]
\[
e_2 = (id_e, id_e, none, getInfo(t, \kappa)
\]
\[
\text{nextStateC}(\Sigma, chrome.tabs.create(\kappa, id_e, (id_e, positionIndex, activeFlag, pinnedBoolean, \ell_1))) = \Sigma[\Psi \leftarrow \Psi'][Tabs \leftarrow Tabs \circ t], e_1 \circ e_2 \quad \text{NewBlankTab}
\]

When a new blank tab is created, we set the tab label the same as the creator’s label. Here \( \kappa \) is the label of the principal that wants to create the tab. \( \kappa_i \) is the label that the creator wants the tab to have. Based on API rules, it should be the case that \( \kappa \Rightarrow \kappa_i \). If the creator is a user, by default, all extensions are allowed to access it. If the creator is an extension, by default, other extensions can not access it. \( id \) could be an extension ID or a user ID. The command can either be in extension context or user context. If the command comes from user context, \( id \) should be user, and the callback function `cmd` is set to `cmd`.

**Update a tab’s url** We need to taint the label of the tab to prevent the case where the tab goes from H to L. If we overwrite the tab’s label, then the low execution may not be able to update the url.

\[
\Sigma = (\Psi, Tabs :: t, \cdots)
\]
\[
t = (id_e, \cdots, \ell_{tab})\quad \Psi = \Psi : chrome.tabs.update(\kappa, id_e, (id_e, url, \cdots))\quad \kappa \not\subseteq \ell_{tab}^*
\]
\[
\text{nextStateC}(\Sigma, chrome.tabs.update(\kappa, id_e, (id_e, url, \cdots))) = \Sigma[\Psi \leftarrow \Psi'][Tabs \leftarrow Tabs'[\Psi \leftarrow \Psi'][f fresh(id_e, id_c, id_w)]
\]
\[
e_1 = (id_e, tabs.onUpdated, none, (id_e, info_1), \ell_1)\quad e_2 = (id_e, id_c, none, getInfo(t', \ell_1)
\]
\[
\text{nextStateC}(\Sigma, chrome.tabs.update(\kappa, id_e, (id_e, url, \cdots))) = \Sigma'; e_1 \circ e_2 \quad \text{UPDATE2}
\]

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Create a blank tab with url: Here, we allow the new tab to float to top secret.

\[
\begin{align*}
fresh(id_t, id_d, id_{ext_1}, id_{ext_2}) & \quad \Sigma = (\Psi, Tabs, \cdots) \\
\Psi = \Psi' :: \text{chrome.tabs.create}(\kappa, id_{cb}, (id_w, positionIndex, url, activeFlag, pinnedBoolean, id_{parentTab})) \\
t = (id_t, \cdots, url, \cdots, FC) \\
\psi' = \text{readyToFetchDoc}(\kappa, id_t, \cdots, url) \\
\Sigma' = \Sigma[\Psi \Leftarrow \psi'][Tabs \Leftarrow Tabs : t] \\
\mathcal{E} = (id_{e1}, \text{tabs.onCreated}, none, info_1, \kappa) :: (id_{e2}, id_{cb}, none, \text{getInfo}(t), \kappa) \\
\text{nextStateC}(\Sigma, \text{chrome.tabs.create}(\kappa, id_{cb}, (id_w, positionIndex, url, activeFlag, pinnedBoolean, id_{parentTab}))) = \Sigma', \mathcal{E} \tag{NEWTAB}
\end{align*}
\]

### 3.9.4 Script Injection

When a content script from an extension is ready to be injected, a new label for the runtime copy of the script is computed from the label associated with the state that the script is ready to be inject \((\kappa)\) and the policy of the extension \((\text{extPolicy}(id_{ext}))\). The label computation function essentially taints the policy label with \(\kappa\) \((\kappa \cup_M \text{extPolicy}(id_{ext}))\).

\[
\begin{align*}
\Sigma = (\Psi, Tabs :: t, \cdots, progInjCSs, \cdots) \\
\Psi = \Psi' :: \text{chrome.tabs.executeScript}(\kappa, id_t, id_{ext}, (cmd, EventHandlers), index, runat, \_ \_ \_ ) \\
t = (id_t, Docs :: Doc, url, \_ \_ \_ , \ell_t) \quad fresh(id_{cs}) \quad \ell = \text{computeLabel}(\kappa, \text{extPolicy}(id_{ext})) \\
\text{ExtCS}_{new} = (id_{ext}, id_{cs}, id_t, cmd, EventHandlers, \_ \_ \_ , runat, index, \ell) \\
\Sigma' = \Sigma[\text{progInjCSs} \Leftarrow \text{progInjCSs} :: \text{ExtCS}_{new}][\Psi \Leftarrow \Psi'] \\
\text{nextStateC}(\Sigma, \text{chrome.tabs.executeScript}(\kappa, id_t, id_{ext}, (cmd, EventHandlers), index, runat, \_ \_ \_ )) = \Sigma', \emptyset \tag{CSIJECTION}
\end{align*}
\]

### 3.9.5 Managing Extensions

**Enable an extension**  An extension can enable, disable another extension/app(including itself), and uninstall an extension/APP, but it cannot install other extensions or apps. Here, the \(id\) in the browserstate is the unique id matching the callback function. A call to enable an extension is discarded if the extension is already active.

\[
\begin{align*}
\Sigma = (\Psi, Tabs, Exts :: Ext, ExtCoreRs, \cdots) \\
\Psi = \Psi' :: \text{chrome.management.setEnabled}(\kappa, id_{cb}, (\text{string}, id, id_{ext}, activeFlag)) \\
\text{Ext} = (id_{ext}, ExtCore, \cdots, activeFlag', \ell_1) \quad \kappa \sqsupset \ell_1^+ \\
\text{nextStateC}(\Sigma, \text{chrome.management.setEnabled}(\kappa, id_{cb}, (\text{string}, id, id_{ext}, activeFlag))) = \Sigma[\Psi \Leftarrow \Psi'], \_ \_ \_ \tag{ENABLEDISABLEEXT1(A)}
\end{align*}
\]

\[
\begin{align*}
\Sigma = (\Psi, Tabs, Exts :: Ext, ExtCoreRs, \cdots) \\
\Psi = \Psi' :: \text{chrome.management.setEnabled}(\kappa, id_{cb}, (\text{string}, id, id_{ext}, activeFlag)) \\
\text{Ext} = (id_{ext}, ExtCore, \cdots, activeFlag, \ell_1) \quad \kappa \sqsubseteq \ell_1^- \\
\ell_2 = \kappa \triangleright_{\text{int}} \ell_1 \quad fresh(id_e) \quad e_1 = (id_e, id_{cb}, none, \text{getInfo}(Ext), \ell_2^-) \\
\text{nextStateC}(\Sigma, \text{chrome.management.setEnabled}(\kappa, id_{cb}, (\text{string}, id, id_{ext}, activeFlag))) = \Sigma[\Psi \Leftarrow \Psi'], e_1 \tag{ENABLEDISABLEEXT1(B)}
\end{align*}
\]
\[\Sigma = (\Psi, \text{Tabs}, \text{Exts} :: \text{Ext}, \text{ExtCoreRs}, \ldots)\]
\[\Psi = \Psi' :: \text{chrome.management.setEnabled}(\kappa, \text{id}_{cb}, (\text{string}, \text{id}, \text{id}_{ext}, \text{active}))\]
\[\text{Ext} = (\text{id}_{ext}, \text{ExtCore}, \ldots, \text{activeFlag}, \ell_1)\]
\[\kappa \subseteq \ell_1^* \quad \text{activeFlag} = \text{inactive} \quad \ell_2 = \kappa \uparrow_{\text{int}} \ell_1\]
\[\text{ExtCoreR} = (\text{id}_{ext}, \text{ExtCore}, \ell_2) \quad \text{Ext}' = \text{Ext}[\text{activeFlag} \leftarrow \text{active}][\ell_1 \leftarrow \ell_2]\]
\[\Sigma' = \Sigma[\text{Ext} \leftarrow \text{Ext}'][\text{ExtCoreRs} \leftarrow \text{ExtCoreRs}'] [\Psi \leftarrow \Psi']\]
\[\text{fresh}(\text{id}_{e_1}, \text{id}_{e_2}) \quad e_1 = (\text{id}_{e_1}, \text{id}_{cb}, \text{none}, \text{getInfo(Ext')}, \ell_2^-)\]
\[e_2 = (\text{id}_{e_2}, \text{management.onEnabled}, \text{none}, \text{getInfo(Ext')}, \ell_2^-)\]

nextStateC(\Sigma, \text{chrome.management.setEnabled}(\kappa, \text{id}_{cb}, (\text{string}, \text{id}, \text{id}_{ext}, \text{active}))) = \Sigma', e_1 :: e_2 \quad \text{ENABLEEXT2}

\text{Disable an extension}
\[\Sigma = (\Psi, \text{Tabs}, \text{Exts} :: \text{Ext}, \text{ExtCoreRs}, \ldots)\]
\[\Psi = \Psi' :: \text{chrome.management.setEnabled}(\kappa, \text{id}_{cb}, (\text{string}, \text{id}, \text{id}_{ext}, \text{inactive}))\]
\[\text{Ext} = (\text{id}_{ext}, \text{ExtCore}, \ldots, \text{activeFlag}, \ell_1)\]
\[\kappa \subseteq \ell_1^* \quad \text{activeFlag} = \text{active} \quad \ell_2 = \kappa \uparrow_{\text{int}} \ell_1\]
\[\text{ExtCoreR} = (\text{id}_{ext}, \text{ExtCore}, \ell_2) \quad \text{Ext}' = \text{Ext}[\text{activeFlag} \leftarrow \text{inactive}][\ell_1 \leftarrow \ell_2]\]
\[\Sigma' = \Sigma[\text{Ext} \leftarrow \text{Ext}'][\text{ExtCoreRs} \leftarrow \text{ExtCoreRs}'][\Psi \leftarrow \Psi']\]
\[\text{fresh}(\text{id}_{e_1}, \text{id}_{e_2}) \quad e_1 = (\text{id}_{e_1}, \text{id}_{cb}, \text{none}, \text{getInfo(Ext')}, \ell_2^-)\]
\[e_2 = (\text{id}_{e_2}, \text{management.onDisabled}, \text{none}, \text{getInfo(Ext')}, \ell_2^-)\]

nextStateC(\Sigma, \text{chrome.management.setEnabled}(\kappa, \text{id}_{cb}, (\text{string}, \text{id}, \text{id}_{ext}, \text{inactive}))) = \Sigma', e_1 :: e_2 \quad \text{DISABLEEXT2}

\text{The target extension does not exist.}
\[\text{DISABLEDISABLEEXT3}\]
\[\Sigma = (\Psi, \text{Tabs}, \text{Exts} :: \text{Ext}, \text{ExtCoreRs}, \ldots)\]
\[\Psi = \Psi' :: \text{chrome.management.setEnabled}(\kappa, \text{id}_{cb}, (\text{string}, \text{id}, \text{id}_{ext}, \text{activeFlag}))\]
\[\forall \text{Ext} \subseteq \text{Exts} \quad \text{Ext} = (\text{id}_{ext}, \ldots)\]

nextStateC(\Sigma, \text{chrome.management.setEnabled}(\kappa, \text{id}_{cb}, (\text{string}, \text{id}, \text{id}_{ext}, \text{activeFlag}))) = \Sigma[\Psi \leftarrow \Psi'] .

\section{Noninterference}

In this section, we introduce formal definitions of noninterference and state the main noninterference theorem.

\subsection{Projections}

We first define operations that remove elements from the state that an attacker cannot observe. We define the projection of relevant constructs given a simple label: \( x \downarrow_\kappa \). The purpose of the projection is to remove information that cannot be read by the attacker (of label \( \kappa \)) from various constructs.

We define a function \( \text{labOf}(x) \) to be the outmost label of the construct \( x \).

\textbf{Projection of actions:}
\[
\begin{align*}
\ell_s^- \subseteq \kappa & \quad \text{API}(\ell_s, \ldots) \downarrow_\kappa = \text{API}(\ell_s, \ldots) & \text{API1} \\
\ell_s^- \nsubseteq \kappa & \quad \text{API}(\ell_s, \ldots) \downarrow_\kappa = & \text{API2}
\end{align*}
\]
Projection of events:

\[
\frac{labOf(e) \sqsubseteq \kappa}{e \downarrow_{\kappa} = e} \quad \text{EVENT1} \quad \frac{labOf(e) \nsubseteq \kappa}{e \downarrow_{\kappa} = \cdot} \quad \text{EVENT2}
\]

Projection of document scripts:

\[
DocCS = (id_{ext}, id_{cs}, id_{t}, \Gamma, cmd, EventHandlers, \ell) \quad \ell^- \sqsubseteq \kappa \quad \frac{DocCS \downarrow_{\kappa} = (id_{ext}, id_{cs}, id_{t}, \Gamma, cmd, EventHandlers \downarrow_{\kappa}, \ell)}{DS1}
\]

\[
\frac{labOf(DocCS) \nsubseteq \kappa}{DocCS \downarrow_{\kappa} = \cdot} \quad \text{DS2}
\]

Projection of content scripts:

\[
\frac{labOf(ExtCS) \sqsubseteq \kappa}{ExtCS \downarrow_{\kappa} = ExtCS} \quad \text{CS1} \quad \frac{labOf(ExtCS) \nsubseteq \kappa}{ExtCS \downarrow_{\kappa} = \cdot} \quad \text{CS2}
\]

Projection of handlers

\[
EventHandler = (id, eventType, x.cmd, eventQueue, cmd, id_e, BlockingFlag, return) \quad \frac{EventHandler \downarrow_{\kappa} = (id, eventType, x.cmd, eventQueue \downarrow_{\kappa}, cmd, id_e, BlockingFlag, return)}{EH}
\]

Projection of runtime extension cores:

\[
ExtCoreR = (id_{ext}, (\Gamma, cmd, EventHandlers), \ell) \quad \ell^- \sqsubseteq \kappa \quad \frac{ExtCoreR \downarrow_{\kappa} = (id_{ext}, (\Gamma, cmd, EventHandlers \downarrow_{\kappa}), \ell)}{EXTCORE1} \quad \frac{labOf(ExtCoreR) \nsubseteq \kappa}{ExtCoreR \downarrow_{\kappa} = \cdot} \quad \text{EXTCORE2}
\]

Projection of storage:

\[
\frac{labOf(Storage) \sqsubseteq \kappa}{Storage \downarrow_{\kappa} = Storage} \quad \text{STORAGE1} \quad \frac{labOf(Storage) \nsubseteq \kappa}{Storage \downarrow_{\kappa} = \cdot} \quad \text{STORAGE2}
\]

Projection of extensions:

\[
Ext = (id_{ext}, ExtCore, ExtCSs, Storage, activeFlag, \ell) \quad \ell^- \sqsubseteq \kappa \quad \frac{Ext \downarrow_{\kappa} = (id_{ext}, ExtCore, ExtCSs \downarrow_{\kappa}, Storage \downarrow_{\kappa}, activeFlag, \ell)}{EXT1}
\]

\[
Ext = (id_{ext}, ExtCore, ExtCSs, Storage, activeFlag, \ell) \quad \ell^- \nsubseteq \kappa \quad \frac{Ext \downarrow_{\kappa} = (id_{ext}, void, ExtCSs \downarrow_{\kappa}, Storage \downarrow_{\kappa}, void, void)}{EXT2}
\]
### Projection of a document node

\[
\text{node} = (id, \ldots, \ell, \ell_{\text{children}}, \ell_{\text{succ}}), \text{nodes}, \text{content}, \ell)
\]

if \(\ell \subseteq \kappa\) then \(c = \text{content}, l = \ell\) else \(c = l = \text{void}\)

if \(\ell_{\text{succ}} \subseteq \kappa\) then \(r = \text{cnt}\) else \(c = \text{brk}\)

\(\ell_{\text{children}} \not\subseteq \kappa\) \(\quad \text{nodes} \downarrow_{\kappa} = N, \Lambda\)

\[
\text{node} \downarrow_{\kappa} = (id, \text{attributes} \downarrow_{\kappa}, N, c, l), \Lambda, r
\]

\[
\text{node} = (id, \ldots, \ell, \ell_{\text{children}}, \ell_{\text{succ}}), \text{nodes}, \text{content}, \ell)
\]

if \(\ell \subseteq \kappa\) then \(c = \text{content}, l = \ell\) else \(c = l = \text{void}\)

if \(\ell_{\text{succ}} \subseteq \kappa\) then \(r = \text{cnt}\) else \(c = \text{brk}\)

\(\ell_{\text{children}} \not\subseteq \kappa\) \(\quad \text{nodes} \downarrow_{\kappa} = N, \Lambda\)

\[
\text{node} \downarrow_{\kappa} = (id, \text{attributes} \downarrow_{\kappa}, \text{void}, c, l), (N, \Lambda), r
\]

\[
\text{node} \downarrow_{\kappa} = \text{node}', \Lambda, \text{cnt} \quad \text{nodes} \downarrow_{\kappa} = N :: N', \Lambda'
\]

\[
\text{node} :: \text{nodes} \downarrow_{\kappa} = (\text{node}' :: N) :: N', (\Lambda, \Lambda')
\]

\[
\text{node} \downarrow_{\kappa} = \text{node}', \Lambda, \text{brk} \quad \text{nodes} \downarrow_{\kappa} = N, \Lambda'
\]

\[
\text{node} :: \text{nodes} \downarrow_{\kappa} = [\text{node}'] :: N, (\Lambda, \Lambda')
\]

### Projection of a document page

\[
\text{Doc} = (id_d, \text{url}, \text{nodes}, \text{DocCSs}, \ell) \quad \ell \subseteq \kappa
\]

\[
\text{Doc} \downarrow_{\kappa} = (id_d, \text{url}, \text{nodes} \downarrow_{\kappa}, \text{DocCSs} \downarrow_{\kappa}, \ell)
\]

\[
\text{Doc} = (id_d, \text{url}, \text{nodes} \downarrow_{\kappa}, \text{DocCSs} \downarrow_{\kappa}, \ell)
\]

### Pruning page event handlers based on the result of document projection

\[
\text{EventHandler} = (id, \ldots)
\]

\[
\text{prune}(\text{EventHandler}, \text{Docs}) = \text{EventHandler}
\]

\[
\text{EventHandler} = (id, \ldots)
\]

\[
\text{prune}(\text{EventHandler}, \text{Docs}) = .
\]

### Projection of browser states:

\[
\text{labOf}(\psi) \subseteq \kappa
\]

\[
\psi \downarrow_{\kappa} = \psi
\]

\[
\text{labOf}(\psi) \not\subseteq \kappa
\]

\[
\psi \downarrow_{\kappa} = .
\]

### Projection of tabs:

\[
\ell \subseteq \kappa
\]

\[
\text{Docs}' = \text{Docs} \downarrow_{\kappa}
\]

\[
\text{EventHandler}' = \text{prune}(\text{EventHandler} \downarrow_{\kappa}, \text{Docs}')
\]

\[
\text{Tab} \downarrow_{\kappa} = (id_t, \text{Docs}', \text{url}, \text{EventHandler}', \ell)
\]

\[
\text{Tab} = (id_t, \text{Docs}, \text{url}, \text{EventHandler}, \ell)
\]

\[
\text{Docs}' \neq .
\]

\[
\text{EventHandler}' = \text{prune}(\text{EventHandler} \downarrow_{\kappa}, \text{Docs}')
\]

\[
\text{Tab} \downarrow_{\kappa} = (id_t, \text{Docs}', \text{void}, \text{EventHandler}', \text{void})
\]

\[
\text{Tab} = (id_t, \text{Docs}, \text{url}, \text{EventHandler}, \ell)
\]

\[
\text{Docs} \downarrow_{\kappa} = .
\]

\[
\text{Tab} \downarrow_{\kappa} = .
\]
4.2 Less than relation

Here, we define a binary relation that compares entities in two states. At a high-level, $S_1$ and $S_2$ are in this relation if $S_1$ and $S_2$ agrees on all the elements that an attacker can observe in $S_1$.

**Less than**  Given two lists $L_1$ and $L_2$, we say $L_1$ is a sub-list of $L_2$, written $L_1 \leq L_2$ if $\forall i \in L_1, \exists j \in L_2$ and $i \leq j$.

For any atomic (non-tuple) value $x$, $\text{void} \leq x$, and $x \leq x$.

$$
\text{EventHandlers}_1 \leq \text{EventHandlers}_2
$$

$$
(\Gamma, \text{cmd}, \text{EventHandlers}_1) \leq (\Gamma, \text{cmd}, \text{EventHandlers}_2)
$$

$$
\text{ExtCore}_1 \leq \text{ExtCore}_2
$$

$$
(id_{ext}, \text{ExtCore}_1, \ell) \leq (id_{ext}, \text{ExtCore}_2, \ell)
$$

$$
\text{EventHandlers}_1 \leq \text{EventHandlers}_2
$$

$$
(id_{ext}, id_{cs}, id_t, \Gamma, \text{cmd}, \text{EventHandlers}_1, \ell) \leq (id_{ext}, id_{cs}, id_t, \Gamma, \text{cmd}, \text{EventHandlers}_2, \ell)
$$

$$
\text{DocSS}_1 \leq \text{DocSS}_2
$$

$$
(id_d, \text{url}_1, \text{nodes}_1, \text{DocSS}_1, \ell_1) \leq (id_d, \text{url}_2, \text{nodes}_2, \text{DocSS}_2, \ell_2)
$$

$$
\text{Doc}_1 \leq \text{Doc}_2
$$

$$
(id_t, \text{Doc}_1, \text{url}_1, \text{EventHandlers}_1, \ell_1) \leq (id_t, \text{Doc}_2, \text{url}_2, \text{EventHandlers}_2, \ell_2)
$$

$$
\text{Tab}_1 \leq \text{Tab}_2
$$

$$
(id_t, \text{Tab}_1, \text{url}_1, \text{EventHandlers}_1, \ell_1) \leq (id_t, \text{Tab}_2, \text{url}_2, \text{EventHandlers}_2, \ell_2)
$$

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for all blocking event $e$, $\text{ExtCoreRs}_1 \leq_{c,e} \text{ExtCoreRs}_2$  
$\text{ExtCoreRs}_1 \leq_{c} \text{ExtCoreRs}_2$  
$\text{ExtCoreRs}_1 \leq_{c} \text{ExtCoreRs}_2$  
$\text{ExtCoreRs}_1 \leq_{c} \text{ExtCoreRs}_2$  
$\text{ExtCoreRs}_1 \leq_{c} \text{ExtCoreRs}_2$

$e$ is a blocking event $e \sim_b \psi$

$\Psi_1 = \psi : \Psi_{11} : \Psi_{12} : \Psi_{13}$  
$\Psi_{11}$ contains states of the form $\text{ProcBlkEvtState}(., ., e)$  
$\Psi_{12}$ contains states of the form $\text{DoneBlkEvtState}(., id, e, c)$  
$\exists \psi \in \Psi_{13}, \text{ s.t. } \psi = \text{ProcBlkEvtState}(., ., e)$, or $\psi = \text{DoneBlkEvtState}(., ., e, c)$

$\Psi_2 = \psi : \Psi_{11} : \Psi_{12} : \Psi_{23}$

$\exists \psi \in \Psi_{23}, \text{ s.t. } \psi = \text{ProcBlkEvtState}(., ., e)$, or $\psi = \text{DoneBlkEvtState}(., id, e, c)$  
$\Psi_1 \leq_{c,e} \Psi_2$  
$\Psi_1 \leq_{c} \Psi_2$  
$\Psi_1 \leq_{c} \Psi_2$

$\Psi \leq_{c} \Psi'$

$\Psi, \text{Tabs}, \text{ExtCoreRs}, \text{MBookmarks}, \text{UI}, \text{sMode} \leq_{\text{STATE}} \Psi', \text{Tabs}', \text{ExtCoreRs}', \text{MBookmarks}', \text{UI}, \text{sMode}$

Finally, we have an additional rule:

\[
\text{stuck} \leq \Sigma
\]

### 4.3 Lemmas

We list several lemmas before presenting our main noninterference theorem.

**Definition 2** (Well-formed configuration). We define $\text{wf}(\Sigma)$ if all of the following hold:

1. $ch = (id, \cdots) \in \text{Tab}$ and $\text{Tab} \in \Sigma$, then node with id exists
2. $e = (id, \text{DOM}.\text{scriptLoaded}, \text{none}, (id_i, id_d, id), \kappa), \kappa \not\subseteq \ell_n$ where $\ell_n$ is the label of node with ID $id$.

**Definition 3** (Matching component). We say that $\text{comp}_1$ and $\text{comp}_2$ are two matching states if the following holds:

1. $\text{comp}_1$ and $\text{comp}_2$ are components of the same type
2. one of the following hold:
   - (a) $\text{comp}_1 \leq \text{comp}_2$ and one of the following holds
     i. $\text{comp}_1$ and $\text{comp}_2$ are run time extension cores and
     ii. $\text{comp}_1$ and $\text{comp}_2$ are injected content scripts (DocCS)
     iii. $\text{comp}_1$ and $\text{comp}_2$ are lists of injected content scripts (DocCSs)
     iv. $\text{comp}_1$ and $\text{comp}_2$ are tabs (Tab)
   - (b) $\text{comp}_1 \leq_{c} \text{comp}_2$
Lemma 1 (Browserstate event relation). If $\psi \sim_b e$ or $\psi \sim_{nb} e$, then $\text{labOf}(\psi) = \text{labOf}(e)$.

Proof. By examining the definition of $\sim_b$ and $\sim_{nb}$.

Lemma 2 (Event enqueue projection 1).

1. If $\text{labOf}(e) \subseteq \kappa$ then
   
   (a) $(\text{Tab} <_Q e) \downarrow_\kappa = \text{Tab} \downarrow_\kappa <_Q e$
   
   (b) $(\text{ExtCoreR} <_Q e) \downarrow_\kappa = \text{ExtCoreR} \downarrow_\kappa <_Q e$

2. If $\text{labOf}(e) \nsubseteq \kappa$ then
   
   (a) $(\text{Tab} <_Q e) \downarrow_\kappa = \text{Tab} \downarrow_\kappa$
   
   (b) $(\text{ExtCoreR} <_Q e) \downarrow_\kappa = \text{ExtCoreR} \downarrow_\kappa$

Proof. By examining the definition of the enqueue operation.

Lemma 3 (Event enqueue projection 2).

1. If $\text{Tab}_1 \downarrow_\kappa \leq \text{Tab}_2 \downarrow_\kappa$ then $(\text{Tab}_1 <_Q e) \downarrow_\kappa \leq (\text{Tab}_2 <_Q e) \downarrow_\kappa$.

2. If $\text{ExtCoreR}_1 \downarrow_\kappa \leq \text{ExtCoreR}_2 \downarrow_\kappa$ then $(\text{ExtCoreR}_1 <_Q e) \downarrow_\kappa \leq (\text{ExtCoreR}_2 <_Q e) \downarrow_\kappa$.

3. If $\text{ExtCoreRs}_1 \downarrow_\kappa \leq_c \text{ExtCoreRs}_2 \downarrow_\kappa$ then $(\text{ExtCoreRs}_1 <_Q e) \downarrow_\kappa \leq_c (\text{ExtCoreRs}_2 <_Q e) \downarrow_\kappa$.

Lemma 4 (Node exists in Doc). If $\text{node} = (id, attributes, nodes, content, \ell) \in \text{Docs}$ and $\ell^- \nsubseteq \kappa$, then $id \in \text{Docs} \downarrow_\kappa$.

Lemma 5 (Node exists in Tab). If $\text{node} = (id, attributes, nodes, content, \ell) \in \text{Tab}$ and $\text{Docs} \in \text{Tab}$, $\ell^- \nsubseteq \kappa$, then $id \in \text{Docs} \downarrow_\kappa$.

Lemma 6 (Independent component update). If $\text{comp}_1 \downarrow_\kappa$ and $\text{comp}_2 \downarrow_\kappa$ are matching components, $\text{comp}_a \downarrow_\kappa$ and $\text{comp}_b \downarrow_\kappa$ are two pairs of matching components, $\text{comp}_a \downarrow_\kappa$ and $\text{comp}_b \downarrow_\kappa$ are two pairs of matching components, let $\text{comp}_1 = \text{comp}_1[\text{comp}_a \leftarrow \text{comp}_a']$, $\text{comp}_2 = \text{comp}_2[\text{comp}_b \leftarrow \text{comp}_b']$, then $\text{comp}_1 \downarrow_\kappa$ and $\text{comp}_2 \downarrow_\kappa$ are two pairs of matching components.

Proof. Given the definitions of matching components, it is clear that the inner components $\text{comp}_a$ and $\text{comp}_b$ are projected independently of the outer components ($\text{comp}_1$ and $\text{comp}_2$). Therefore, updating the inner components with a matching pair preserves the less than relation.

Lemma 7 (Event handler update).

1. If $\text{DocCS}_1 = (id_{ext1}, id_{cs1}, id_{r1}, \Gamma_1, cmd_1, \text{EventHandlers}_1, \ell_1)$, $\text{DocCS}_2 = (id_{ext2}, id_{cs2}, id_{r2}, \Gamma_2, cmd_2, \text{EventHandlers}_2, \ell_2)$, $\text{DocCS}_1 \downarrow_\kappa \leq \text{DocCS}_2 \downarrow_\kappa$, $\ell_1^- \nsubseteq \kappa$, $\text{EventHandlers}_1 = \text{EventHandlers}_1' :: \text{eh}_1$, $\text{EventHandlers}_2 = \text{EventHandlers}_2' :: \text{eh}_2$, $\text{eh}_1' \downarrow_\kappa \leq \text{eh}_2' \downarrow_\kappa$, then $\text{DocCS}_1[\text{eh}_1 \leftarrow \text{eh}_1'] \downarrow_\kappa \leq \text{DocCS}_2[\text{eh}_2 \leftarrow \text{eh}_2'] \downarrow_\kappa$.

2. If $\text{ExtCoreR}_1 = (id_{ext1}, (\Gamma_1, cmd_1, \text{EventHandlers}_1), \ell_1)$, $\text{ExtCoreR}_2 = (id_{ext2}, (\Gamma_2, cmd_2, \text{EventHandlers}_2), \ell_2)$, $\text{ExtCoreR}_1 \downarrow_\kappa \leq_c \text{ExtCoreR}_2 \downarrow_\kappa$, $\ell_1^- \nsubseteq \kappa$, $\text{EventHandlers}_1 = \text{EventHandlers}_1' :: \text{eh}_1$, $\text{EventHandlers}_2 = \text{EventHandlers}_2' :: \text{eh}_2$, $\text{eh}_1' \downarrow_\kappa \leq_c \text{eh}_2' \downarrow_\kappa$, for any blocking event, $e$ in the queue of $\text{eh}_1'$, if $e$ in the queue of $\text{eh}_2'$ then $\text{ExtCoreR}_1[\text{eh}_1 \leftarrow \text{eh}_1'] \downarrow_\kappa \leq_c \text{ExtCoreR}_2[\text{eh}_2 \leftarrow \text{eh}_2'] \downarrow_\kappa$.

Proof. The projection of event handlers is independent of the rest of the elements, so swapping related event handlers on both sides maintains the relation.
Lemma 8 (Event handler update in page scripts). If Docs$_1 \downarrow \kappa \leq$ Docs$_2 \downarrow \kappa$, node$_1 \in$ Docs$_1$ and node$_1 = (id_n, \ldots, \ell)$, $\ell^- \subseteq \kappa$, node$_2 \in$ Docs$_2$ and node$_2 = (id_n, \ldots, \ell)$, node$_1 \downarrow \kappa \leq$ node$_2 \downarrow \kappa$, prune(EventHandler$_1 \downarrow \kappa$, Docs$_1 \downarrow \kappa$) $\leq$ prune(EventHandler$_2 \downarrow \kappa$, Docs$_2 \downarrow \kappa$), EventHandler$_1 =$ EventHandler$_2 :: eh_1$, EventHandler$_2 =$ EventHandler$_2' :: eh_2$, eh$_1' \downarrow \kappa \subseteq$ eh$_2' \downarrow \kappa$, $\ell^- \subseteq \kappa$, node$_1' =$ node$_1[\ell \leftarrow \ell']$, node$_2' =$ node$_2[\ell \leftarrow \ell']$, node$_1' \downarrow \kappa \leq$ node$_2' \downarrow \kappa$, then prune(EventHandler$_1 :: eh_1 \downarrow \kappa$, Docs$_1[\text{node} \leftarrow \text{node}'] \downarrow \kappa$) $\leq$ prune(EventHandler$_2' :: eh_2' \downarrow \kappa$, Docs$_2[\text{node} \leftarrow \text{node}'] \downarrow \kappa$).

Proof. Use Lemma 4. The updated node still exists after the projection. Further, the updated event handlers are related. Therefore, the pruned event handlers are also related. \qed

Lemma 9 (Browserstate relation 1). Given any blocking event $e$ and $\Psi_1 \leq_c \Psi_2$, if

1. $\psi \sim_b e$
2. $\Psi_1 = \psi :: \Psi_{12} :: \Psi_{13}$,
   $\Psi_{11}$ contains states of the form ProcBlkEvtState($\ldots$, $e$),
   $\Psi_{12}$ contains states of the form DoneBlkEvtState($\ldots$, $e$, $\ldots$),
   $\exists \psi' \in \Psi_{13}$ s.t. $\psi = \text{ProcBlkEvtState}(\ldots, e, \ldots)$, or $\psi = \text{DoneBlkEvtState}(\ldots, e, \ldots)$.
3. $\Psi_2 = \psi :: \Psi_{11} :: \Psi_{12} :: \Psi_{23}$,
   $\exists \psi' \in \Psi_{23}$ s.t. $\psi = \text{ProcBlkEvtState}(\ldots, e, \ldots)$, or $\psi = \text{DoneBlkEvtState}(\ldots, e, \ldots)$.

we have $\Psi_{13} \leq_c \Psi_{23}$.

Lemma 10 (Browserstate relation 2). If $\Psi_1 \leq_c \Psi_2$, $\psi \not\in \Psi_1$, $\Psi_1 :: \psi \leq_c \Psi_2 :: \psi$.

Lemma 11 (Browserstate relation 3). If $\Psi_1 \leq_c \Psi_2$, $\forall \psi \in \Psi_1$, for all blocking event $e$, $\psi \not\sim_b e$ imply $\Psi_1 \setminus \psi \leq_c \Psi_2 \setminus \psi$.

Lemma 12 (Browserstate relation 4). If $\Psi_1 \leq_c \Psi_2$, $\forall \psi \in \Psi_1$, for all blocking event $e$, $\psi \not\sim_b e$ and $\psi$ is not a DoneBlkEvtState($\ldots$) or ProcBlkEvtState($\ldots$) related to $e$ imply $\Psi_1 \setminus \psi \leq_c \Psi_2$.

Lemma 13 (Next browserstate’s label). If $(\psi', e') = \text{nextState}(\psi, \text{void})$, then $\text{labOf}(\psi') \subseteq \text{labOf}(\psi) = \text{labOf}(e')$.

Lemma 14 (nextStateC). When the transitions are not CSINJECTION, BEFOREFETCHALLOWED, BEFOREFETCHDOCALLOWED, BEFOREFETCHDOCBLOCKED(1), BEFOREFETCHDOCBLOCKED(2), DOMAPPENDCHILDREN(1),

$\Sigma_1 \downarrow \kappa \leq \Sigma_2 \downarrow \kappa$, $\psi \in \Sigma_1$, nextStateC($\Sigma_1, \psi$) $= \Sigma_1', E_1$ implies one of the following holds

1. nextStateC($\Sigma_2, \psi$) $= \Sigma_2', E_2$ and $\Sigma_1' \downarrow \kappa \leq \Sigma_2' \downarrow \kappa$, $\Sigma_1 \downarrow \kappa \leq \Sigma_2 \downarrow \kappa$.
2. $\Sigma_1' \downarrow \kappa \leq \Sigma_2 \downarrow \kappa$, $E_1' = \cdot$

Lemma 15 (Synchronous calls). $\Sigma_1 \downarrow \kappa \leq \Sigma_2 \downarrow \kappa$, $\Sigma_1 = \Sigma_{ext}[\| \Gamma, API_s(e) \|_d]$

1. if $\Sigma_1 \xrightarrow{API_s} \Sigma_1'; E_1'$ then one of the following holds
   (a) $\Sigma_2 \xrightarrow{API_s} \Sigma_2'; E_2'$ and $\Sigma_1' \downarrow \kappa \leq \Sigma_2' \downarrow \kappa$, $\Sigma_1 \downarrow \kappa \leq \Sigma_2' \downarrow \kappa$
   (b) $\Sigma_1' \downarrow \kappa = \Sigma_2 \downarrow \kappa$ and $E_1' = \cdot$
2. if $\Sigma_1 \xrightarrow{\alpha} \Sigma_1'$, $\Sigma_1' ; E_1'$ and $\alpha \downarrow \kappa = \cdot$ then $\Sigma_1' \downarrow \kappa \leq \Sigma_2 \downarrow \kappa$ and $E_1' \downarrow \kappa = \cdot$
3. if $\Sigma_1 \xrightarrow{\alpha} \Sigma_1'$, $\Sigma_1' ; E_1'$ and $\alpha \downarrow \kappa = \alpha$ then $\Sigma_2 \xrightarrow{\alpha} \Sigma_2', E_2'$, $\Sigma_1' \downarrow \kappa \leq \Sigma_2' \downarrow \kappa$ and $E_1' \downarrow \kappa \leq E_2' \downarrow \kappa$

Lemma 16 (One step simulation). $\Xi_1 \downarrow \kappa \leq \Xi_2 \downarrow \kappa$, $\Sigma_1 \downarrow \kappa \leq \Sigma_2 \downarrow \kappa$ and $\Sigma_1 \downarrow \kappa \leq \Sigma_2 \downarrow \kappa$ and $\Xi_1 \downarrow \kappa \leq \Xi_2 \downarrow \kappa$

1. if $\Xi_1; \Sigma_1; E_1 \xrightarrow{\cdot} \Xi_1'; \Sigma_1' ; E_1'$ then one of the following holds
(a) \( \Xi_2; \Sigma_2; \mathcal{E}_2 \xrightarrow{} \Xi_2'; \Sigma_2'; \mathcal{E}_2' \) and \( \Xi_1 \xrightarrow{} \Xi_2 \), \( \Sigma_1 \xrightarrow{} \Sigma_2 \), and \( \mathcal{E}_1 \xrightarrow{} \mathcal{E}_2 \).

(b) \( \Xi_1 \xrightarrow{} \Xi_2 \), \( \Sigma_1 \xrightarrow{} \Sigma_2 \), and \( \mathcal{E}_1 \xrightarrow{} \mathcal{E}_2 \).

2. If \( \Xi_1; \Sigma_1; \mathcal{E}_1 \xrightarrow{} \Xi_1'; \Sigma_1'; \mathcal{E}_1' \) and \( \alpha \xrightarrow{} \cdot \) then \( \Xi_1 \xrightarrow{} \Xi_2 \), \( \Sigma_1 \xrightarrow{} \Sigma_2 \), \( \mathcal{E}_1 \xrightarrow{} \mathcal{E}_2 \).

3. If \( \Xi_1; \Sigma_1; \mathcal{E}_1 \xrightarrow{} \Xi_1'; \Sigma_1'; \mathcal{E}_1' \) and \( \alpha \xrightarrow{} \alpha \) then \( \Xi_2; \Sigma_2; \mathcal{E}_2 \xrightarrow{} \Xi_2'; \Sigma_2'; \mathcal{E}_2' \), \( \Xi_1 \xrightarrow{} \Xi_2 \), \( \Sigma_1 \xrightarrow{} \Sigma_2 \), and \( \mathcal{E}_1 \xrightarrow{} \mathcal{E}_2 \).

\textbf{Lemma 17 \textit{(Multi-step simulation)}}.

If \( \Xi_1 \xrightarrow{} \Xi_2 \), \( \Sigma_1 \xrightarrow{} \Sigma_2 \), \( \mathcal{E}_1 \xrightarrow{} \mathcal{E}_2 \) then \( \forall \rho \) s.t. \( \Xi_1; \Sigma_1; \mathcal{E}_1 \xrightarrow{} \Xi_2; \Sigma_2; \mathcal{E}_2 \) and the transitions do not have declassification steps exists \( \rho' \) such that \( \rho \equiv \rho' \) and \( \Xi_2; \Sigma_2; \mathcal{E}_2 \xrightarrow{} \).

\textbf{Proof.} By induction on the number of transition steps, in the inductive case, Use Lemma 16. \(\) 

\textbf{Theorem 18 \textit{(Noninterference)}}.

If \( \Xi_1 \xrightarrow{} \Xi_2 \), \( \Sigma_1 \xrightarrow{} \Sigma_2 \), \( \mathcal{E}_1 \xrightarrow{} \mathcal{E}_2 \) then

\(\) \(\forall \rho \) s.t. \( \Xi_1; \Sigma_1; \mathcal{E}_1 \xrightarrow{} \Xi_2; \Sigma_2; \mathcal{E}_2 \) and the transitions do not have declassification steps exists \( \rho' \) such that \( \rho \equiv \rho' \) and \( \Xi_2; \Sigma_2; \mathcal{E}_2 \xrightarrow{} \).

\textbf{Proof.} Because the initial states are the same, so \( \Xi_1 \xrightarrow{} \Xi_2 \), \( \Sigma_1 \xrightarrow{} \Sigma_2 \), \( \mathcal{E}_1 \xrightarrow{} \mathcal{E}_2 \) and \( \Xi_2 \xrightarrow{} \Xi_1 \), \( \Sigma_2 \xrightarrow{} \Sigma_1 \), \( \mathcal{E}_2 \xrightarrow{} \mathcal{E}_1 \).

The conclusion follows from Lemma 17 directly. \(\)

\section{Proofs}

\subsection{Proof of Lemma 16}

\textbf{Case: Context}

There are three subcases: (1) the script is a page script handler, (2) the script is a content script and (3) the script is in the extension core.

\textbf{Subcase:} the script is a page script handler.

Let \( \Sigma_1 = (\Psi_1, \text{Tabs}_1 :: \text{Tab}_1, \text{ExtCoreRs}_1, \text{progInjCSs}_1, \text{Exts}_1, \text{Cookies}_1, \text{MBookmarks}_1, \text{histories}_1, \text{UI}_1) \)

\(\) \(\Sigma_2 = (\Psi_2, \text{Tabs}_2, \text{ExtCoreRs}_2, \text{progInjCSs}_2, \text{Exts}_2, \text{Cookies}_2, \text{MBookmarks}_2, \text{histories}_2, \text{UI}_2) \)

\textbf{By assumptions}

\(\) \(\Sigma_1 = \Sigma_{ctx} \| \Gamma, \text{cmd} \| \id \)

\(\) \(\text{Tab}_1 = \text{Tab}_{ctx} \| \Gamma, \text{cmd} \| \id = (\text{TabID}_1, \text{Docs}_1 :: \text{Doc}_\text{env} \| \Gamma, \text{url}_1, \text{EventHandlers}_1 :: \text{EventHandler}_{ctx} \| \text{cmd} \| \id, \ell_1) \)

\(\) and \(\Sigma'_1 = \Sigma_{ctx} \| \Gamma', \text{cmd}' \| \id, \ell'_1 = \ell_1 \)

\textbf{Assume that the label of the node with ID \( \id \) is \( \ell_n : \text{ctxOfId}(\Sigma_1, \id) = \ell_n \)}

\textbf{Sub-case: \( \ell_n \in \kappa \)}

\textbf{By Lemma 5,}

\(\) \(\id \in \text{Docs}_1 \) and exists \( \text{node}_\text{env} \| \Gamma \| \id \in \text{Doc}_\text{env} \)

\textbf{By definition of Prune,}

\(\) \(\text{EventHandler}_{ctx} \| \text{cmd} \| \id \in \text{Tab}_1 \)

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By $\Sigma_1 \downarrow_\kappa \leq \Sigma_2 \downarrow_\kappa$

(2) $\text{Tabs}_2 = \text{Tabs}_2' \circ \text{Tab}_2$ and $\text{EventHandler}_{\text{CTX}} \mid \text{cmd} \mid \text{id} \in \text{Tab}_2 \downarrow_\kappa$

By definitions and (2),

(3) exists $\text{Docs}_2' \in \text{Tab}_2 \downarrow_\kappa$ and exists $\text{node}'_\text{env} \mid \Gamma \mid \text{id} \in \text{Docs}_2' \text{s.t. } \text{node}_\text{env} \mid \Gamma \mid \text{id} \leq \kappa \text{node}'_\text{env} \mid \Gamma \mid \text{id}$

By (2) and (3)

(4) $\text{Tab}_2 = (\text{TabID}_2, \text{Docs}_2 \mid \Gamma, \text{url}_2, \text{EventHandler}_2 \circ \text{EventHandler}_{\text{CTX}} \mid \text{cmd} \mid \text{id}, \ell_2)$

Apply CONTEXT to $\Sigma_2$, let $\Sigma_2' = \Sigma_{\text{ctx}_2} \mid \Gamma, \text{cmd} \mid \text{id}$

(5) $\Sigma_{\text{ctx}_2} \mid \Gamma, \text{cmd} \mid \text{id}; \Sigma_2 \downarrow_\kappa \Sigma_{\text{ctx}_2} \mid \Gamma', \text{cmd}' \mid \text{id}; \Sigma_2$

By $\Sigma_1 \downarrow_\kappa \leq \Sigma_2 \downarrow_\kappa, \Sigma_1 = \Sigma_{\text{ctx}} \mid \Gamma, \text{cmd} \mid \text{id}, \Sigma_2 = \Sigma_{\text{ctx}_2} \mid \Gamma, \text{cmd} \mid \text{id},$

and CONTEXT does not change $\Sigma_{\text{ctx}}$ and $\Sigma_{\text{ctx}_2}$

(6) $\Sigma_{\text{ctx}} \mid \Gamma' \mid \text{cmd}' \mid \text{id} \downarrow_\kappa \leq \Sigma_{\text{ctx}_2} \mid \Gamma' \mid \text{cmd}' \mid \text{id} \downarrow_\kappa$

By assumption

(7) $\Sigma_1 \downarrow_\kappa \leq \Sigma_2 \downarrow_\kappa$

(8) $\Sigma_1 \downarrow_\kappa = \Sigma_2 \downarrow_\kappa$

sub-case ii. $\ell \downarrow_\kappa \subseteq \kappa$

By definitions

(1) $\text{id} \notin \text{Docs}_1 \downarrow_\kappa$ and $\text{EventHandler}_{\text{CTX}} \mid \text{cmd} \mid \text{id} \notin \text{Tab}_1 \downarrow_\kappa$ and $\text{node}_\text{env} \mid \Gamma \mid \text{id} \notin \text{Tab}_1 \downarrow_\kappa$

By $\Sigma_1 \downarrow_\kappa \leq \Sigma_2 \downarrow_\kappa, \Sigma_1 = \Sigma_{\text{ctx}} \mid \Gamma, \text{cmd} \mid \text{id}, \text{and CONTEXT does not change } \Sigma_{\text{ctx}}$

(2) $\Sigma_{\text{ctx}} \mid \Gamma' \mid \text{cmd}' \mid \text{id} \downarrow_\kappa = \Sigma_{\text{ctx}_2} \mid \Gamma, \text{cmd} \mid \text{id} \downarrow_\kappa \leq \Sigma_2 \downarrow_\kappa$

By assumption

(3) $\Sigma_1 \downarrow_\kappa \leq \Sigma_2 \downarrow_\kappa$

Subcase: the script is a content script handler

Let $\Sigma_1 = (\Psi_1, \text{Tabs}_1 \circ \text{Tab}_1, \text{ExtCoreRs}_1, \text{progInjCS}_1, \text{Exts}_1, \text{Cookies}_1, \text{MBookmarks}_1, \text{histories}_1, \text{UI}_1)$

$\Sigma_2 = (\Psi_2, \text{Tabs}_2 \circ \text{ExtCoreRs}_2, \text{progInjCS}_2, \text{Exts}_2, \text{Cookies}_2, \text{MBookmarks}_2, \text{histories}_2, \text{UI}_2)$

By assumptions

$\Sigma_1 = \Sigma_{\text{ctx}} \mid \Gamma, \text{cmd} \mid \text{id}$

$\text{Tab}_1 = \text{Tab}_{\text{CTX}} \mid \Gamma, \text{cmd} \mid \text{id} = (\text{TabID}_1, \text{Docs}_1 \circ \text{Doc}_{\text{CTX}} \mid \Gamma, \text{cmd} \mid \text{id}, \text{url}_1, \text{EventHandler}_1, \ell_1)$

$\text{Doc}_{\text{CTX}} \mid \Gamma, \text{cmd} \mid \text{id} = (\text{id}_d, \text{url}, \text{nodes}, \text{Docs}_\text{CS} \circ \text{DocCS}_{\text{CTX}} \mid \Gamma, \text{cmd} \mid \text{id}, \ell_d)$

$\text{DocCS}_{\text{CTX}} \mid \Gamma, \text{cmd} \mid \text{id} = (\text{id}_\text{ext}, \text{id}, \text{id}_1, \text{|\Gamma|}, \text{|cmd|}, \text{EventHandler}, \ell - \text{|\Gamma|}, \text{|\Gamma|}, \text{|cmd|}, \text{EventHandler}_2, \ell_2)$

or $\text{DocCS}_{\text{CTX}} \mid \Gamma, \text{cmd} \mid \text{id} = (\text{id}_\text{ext}, \text{id}, \text{id}_1, \text{|\Gamma|}, \text{|cmd|}, \text{EventHandler}_2, \ell_2)$

sub-case i. $\ell \downarrow_\kappa \subseteq \kappa$

By $\text{DS}_1$

$\text{DocCS}_{\text{CTX}} \mid \Gamma, \text{cmd} \mid \text{id} \downarrow_\kappa = (\text{id}_\text{ext}, \text{id}, \text{id}_1, \text{|\Gamma|}, \text{|cmd|}, \text{EventHandler}_2, \ell_2)$

or $\text{DocCS}_{\text{CTX}} \mid \Gamma, \text{cmd} \mid \text{id} \downarrow_\kappa = (\text{id}_\text{ext}, \text{id}, \text{id}_1, \text{|\Gamma|}, \text{|cmd|}, \text{EventHandler}_2, \ell_2)$

By definition

(1) $\text{DocCS}_{\text{CTX}} \mid \Gamma, \text{cmd} \mid \text{id} \downarrow_\kappa \subseteq \text{Tab}_1 \downarrow_\kappa$

By $\Sigma_1 \downarrow_\kappa \leq \Sigma_2 \downarrow_\kappa$

(2) $\text{Tabs}_2 = \text{Tabs}_2' \circ \text{Tab}_2$ and $\text{DocCS}_{\text{CTX}} \mid \Gamma, \text{cmd} \mid \text{id} \in \text{Tab}_2 \downarrow_\kappa$

By definitions and (2),

(3) exists $\text{DocCS}_{\text{CTX}} \mid \Gamma, \text{cmd} \mid \text{id} \in \text{DocCS}_2, \text{DocCS}_2' \in \text{Doc}_2, \text{Doc}_2' \in \text{Docs}_2, \text{Docs}_2' \in \text{Tab}_2 \downarrow_\kappa$

By (2) and (3)

(4) $\text{Tab}_2 = (\text{TabID}_2, \text{Docs}_2' \circ \text{Doc}_2' \mid \Gamma, \text{cmd} \mid \text{id}, \text{url}_2, \text{EventHandler}_2, \ell_2)$

Apply CONTEXT to $\Sigma_2$, let $\Sigma_2' = \Sigma_{\text{ctx}_2} \mid \Gamma, \text{cmd} \mid \text{id}$

(5) $\Sigma_{\text{ctx}_2} \mid \Gamma, \text{cmd} \mid \text{id}; \Sigma_2 \downarrow_\kappa \Sigma_{\text{ctx}_2} \mid \Gamma', \text{cmd}' \mid \text{id}; \Sigma_2$

By $\Sigma_1 \downarrow_\kappa \leq \Sigma_2 \downarrow_\kappa, \Sigma_1 = \Sigma_{\text{ctx}} \mid \Gamma, \text{cmd} \mid \text{id}, \Sigma_2 = \Sigma_{\text{ctx}_2} \mid \Gamma, \text{cmd} \mid \text{id},$

and CONTEXT does not change $\Sigma_{\text{ctx}}$ and $\Sigma_{\text{ctx}_2}$
(6) $\Sigma_{ctx} \updownarrow \Gamma', cmd' \uparrow_{id} \leq \Sigma_{ctx2} \uparrow \Gamma', cmd' \uparrow_{id}$

By assumption
(7) $E_1 \uparrow_{\kappa} \leq E_2 \downarrow_{\kappa}$
(8) $E_1' \downarrow_{\kappa} = E_1 \downarrow_{\kappa} \leq E_2 \downarrow_{\kappa}$

Sub-case ii. $\ell \not\in \kappa$

By DS2
(1) $DocCS_{ctx} \uparrow, \Gamma, cmd \uparrow_{id} \not\in Tab_1 \downarrow_{\kappa}$
By $\Sigma_1 \downarrow_{\kappa} \leq \Sigma_2 \downarrow_{\kappa}$, $\Sigma_1 = \Sigma_{ctx} \uparrow \Gamma, cmd \uparrow_{id}$, and CONTEXT does not change $\Sigma_{ctx}$
(2) $\Sigma_{ctx} \uparrow \Gamma', cmd' \uparrow_{id} \downarrow_{\kappa} = \Sigma_{ctx2} \uparrow \Gamma, cmd \uparrow_{id} \downarrow_{\kappa} \leq \Sigma_2 \downarrow_{\kappa}$

By assumption
(3) $E_1 \downarrow_{\kappa} \leq E_2 \downarrow_{\kappa}$

Subcase: the script is in extension core

Let $\Sigma_1 = (\Psi_1, Tabs_1, ExtCoreRs_1 :: ExtCoreR, progInvCS_1, Ext_1, Cookies_1, MBookmarks_1, histories_1, UI_1)$
$\Sigma_2 = (\Psi_2, Tabs_2, ExtCoreRs_2, progInvCS_2, Ext_2, Cookies_2, MBookmarks_2, histories_2, UI_2)$

By assumptions
$\Sigma_1 = \Sigma_{ctx} \uparrow \Gamma, cmd \uparrow_{id}$
$ExtCoreR = ExtCoreR_{ctx} \uparrow \Gamma, cmd \uparrow_{id} = (id, (|\Gamma|, |cmd|, EventHandlers), \ell)$
or $(id, (|\Gamma|, cmd, EventHandlers :: EventHandler_{ctx}(cmd)), \ell)$

Sub-case i. $\ell \not\in \kappa$

By EXTCore1,
$ExtCoreR_{ctx} \uparrow \Gamma, cmd \uparrow_{id} \downarrow_{\kappa} = (id, (|\Gamma|, |cmd|, EventHandlers \downarrow_{\kappa}), \ell)$
or $ExtCoreR_{ctx} \uparrow \Gamma, cmd \uparrow_{id} \downarrow_{\kappa} = (id, (|\Gamma|, cmd, EventHandlers \downarrow_{\kappa} :: EventHandler_{ctx}(cmd) \downarrow_{\kappa}), \ell)$

By definition
(1) $ExtCoreR_{ctx} \uparrow \Gamma, cmd \uparrow_{id} \downarrow_{\kappa} \in \Sigma_1 \downarrow_{\kappa}$
By $\Sigma_1 \downarrow_{\kappa} \leq \Sigma_2 \downarrow_{\kappa}$
(2) $ExtCoreR_{ctx} \uparrow \Gamma, cmd \uparrow_{id} \downarrow_{\kappa} \in ExtCoreRs_2 \downarrow_{\kappa}$

By definitions and (2)
(3) exists $ExtCoreR'_{ctx} \uparrow \Gamma, cmd \uparrow_{id} \downarrow_{\kappa} \in ExtCoreRs_2 \downarrow_{\kappa}$ s.t. $ExtCoreR'_{ctx} \uparrow \Gamma, cmd \uparrow_{id} \downarrow_{\kappa} \leq ExtCoreR_{ctx} \uparrow \Gamma, cmd \uparrow_{id} \downarrow_{\kappa}$

let $\Sigma_2 = \Sigma_{ctx2} \uparrow \Gamma, cmd \uparrow_{id}$, apply CONTEXT to $\Sigma_2$
(4) $\Sigma_{ctx2} \uparrow \Gamma, cmd \uparrow_{id} \downarrow_{\kappa} \rightarrow E_2 \rightarrow \Sigma_{ctx2} \uparrow \Gamma', cmd' \uparrow_{id} \downarrow_{\kappa}$
By $\Sigma_1 \downarrow_{\kappa} \leq \Sigma_2 \downarrow_{\kappa}$, $\Sigma_1 = \Sigma_{ctx} \uparrow \Gamma, cmd \uparrow_{id}$, $\Sigma_2 = \Sigma_{ctx2} \uparrow \Gamma, cmd \uparrow_{id}$, and rule CONTEXT does not change $\Sigma_{ctx}$ and $\Sigma_{ctx2}$
(5) $\Sigma_{ctx} \uparrow \Gamma', cmd' \uparrow_{id} \downarrow_{\kappa} \leq \Sigma_{ctx2} \uparrow \Gamma', cmd' \uparrow_{id} \downarrow_{\kappa}$

By assumption
(6) $E_1 \downarrow_{\kappa} \leq E_2 \downarrow_{\kappa}$
(7) $E_1' \downarrow_{\kappa} = E_1 \downarrow_{\kappa} \leq E_2 \downarrow_{\kappa}$

Sub-case ii. $\ell \not\in \kappa$

By EXTCore2
(1) $ExtCoreR \downarrow_{\kappa} = \cdot, ExtCoreR_{ctx} \uparrow \Gamma, cmd \uparrow_{id} \not\in \Sigma_1 \downarrow_{\kappa}$
By $\Sigma_1 \downarrow_{\kappa} \leq \Sigma_2 \downarrow_{\kappa}$, $\Sigma_1 = \Sigma_{ctx} \uparrow \Gamma, cmd \uparrow_{id}$, and CONTEXT does not change $\Sigma_{ctx}$
(2) $\Sigma_{ctx} \uparrow \Gamma', cmd' \uparrow_{id} \downarrow_{\kappa} \leq \Sigma_{ctx2} \uparrow \Gamma, cmd \uparrow_{id} \downarrow_{\kappa} \leq \Sigma_2 \downarrow_{\kappa}$

By assumption
(3) $E_1 \downarrow_{\kappa} \leq E_2 \downarrow_{\kappa}$

Case: Return-Core
Let $\Sigma_1 = (\Psi_1, Tabs_1, ExtCoreR_{s_1}, progInjCS_{s_1}, ExtS_1, Cookies_1, MBookmarks_1, histories_1, U_{11})$

$\Sigma_2 = (\Psi_2, Tabs_2, ExtCoreR_{s_2}, progInjCS_{s_2}, ExtS_2, Cookies_2, MBookmarks_2, histories_2, U_{12})$

By assumptions

(A1) $\Sigma_1 = \Sigma_{ctx} \parallel \Gamma, \text{ret } v | id$

(A2) $ExtCoreR_{ctx} \parallel \Gamma, \text{ret } v | id \in ExtCoreR_{s_1}$

(A3) $ExtCoreR = ExtCoreR_{ctx} \parallel \Gamma, \text{ret } v | id = (id, (\parallel \Gamma, cmd, EventHandlers :: EventHandler_{ctx}[\text{ret } v]), \ell)$

(A4) $EventHandler_{ctx}[\text{ret } v] = (\parallel id, eventType, x.cmd, \mathcal{E}, \parallel \text{ret } v, \parallel id, \parallel id, \parallel \text{nonblocking, some}(R, id_r))$

(A5) $\Sigma'_1 = \Sigma'_{ctx} \parallel \Gamma, \text{skip } | id = \Sigma_{ctx} \parallel \Gamma, \text{skip } | id[\Psi_1 \leftarrow \Psi_1 \parallel \psi_1]$

(A6) $\psi_1 = \text{asyncAPIRetState}(R, \ell^-, id_r, v)$

(A7) $E'_1 | \parallel E_1$

sub-subcase i. \(\ell^- \subseteq \kappa\)

By EXTCORE1,

(1) $ExtCoreR_{ctx} \parallel \Gamma, \text{ret } v | id \downarrow \kappa = (id, (\parallel \Gamma, cmd, EventHandlers \downarrow \kappa :: EventHandler_{ctx}[\text{ret } v]), \ell)$

(2) $ExtCoreR_{ctx} \parallel \Gamma, \text{ret } v | id \downarrow \kappa \in \Sigma_1 | \parallel \kappa$

By ExtCoreR_{s_1} \(\downarrow \kappa \leq ExtCoreR_{s_2} \downarrow \kappa\)

(3) $\exists \text{ExtCore}_{ctx} \parallel \Gamma, \text{ret } v | id \in ExtCoreR_{s_2}$

s.t. $ExtCoreR_{ctx} \parallel \Gamma, \text{ret } v | id \downarrow \kappa \leq ExtCoreR_{ctx'} \parallel \Gamma, \text{ret } v | id \downarrow \kappa$

$ExtCoreR_{ctx'} \parallel \Gamma, \text{ret } v | id \downarrow \kappa = (id, (\parallel \Gamma, cmd, EventHandlers' \downarrow \kappa :: EventHandler'_{ctx}[\text{ret } v \downarrow \kappa]), \ell)$

$EventHandlers \downarrow \kappa \leq EventHandlers' \downarrow \kappa$

$EventHandler'_{ctx}[\text{ret } v] = (\parallel id, eventType, x.cmd, \mathcal{E}', \parallel \text{ret } v, \parallel id, \parallel id, \parallel \text{nonblocking, some}(R, id_r))$

$E \downarrow \kappa \leq E' \downarrow \kappa$

let $\Sigma_2 = \Sigma_{ctx2} \parallel \Gamma, \text{ret } v | id \downarrow \kappa = \text{apply RETURN-CORE to } \Sigma_2,$

(4) $\Sigma_{ctx2} \parallel \Gamma, \text{ret } v | id; E_2 \Downarrow \Sigma'_{ctx2} \parallel \Gamma, \text{skip } | id; E_2$

(5) $\Sigma'_{ctx2}(id) = \Sigma_{ctx2}(id)|\Psi_2 \leftarrow \Psi_2 :: \psi_2$

(6) $\psi_2 = \text{asyncAPIRetState}(R, \ell^-, id_r, v) = \psi_1$

By BROWSERSTATE1

(7) $\psi_1 \downarrow \kappa = \psi_1, \psi_2 \downarrow \kappa = \psi_2.$

By $\Psi_1 \downarrow \kappa \leq \Psi_2 \downarrow \kappa \leq \Psi_2 :: \psi_2,$ Lemma 10

(8) $\Psi_1 :: \psi_1 \downarrow \kappa \leq \Psi_2 :: \psi_2 \downarrow \kappa$

By $\Sigma_1 \downarrow \kappa \leq \Sigma_2 \downarrow \kappa, \Sigma_1 = \Sigma_{ctx} \parallel \Gamma, \text{ret } v | id, \Sigma_2 = \Sigma_{ctx} \parallel \Gamma, \text{ret } v | id,$ (5), (6), and (7)

and RETURN-CORE only change the browser state,

(9) $\Sigma'_{ctx} \parallel \Gamma', \text{skip } | id \downarrow \kappa \leq \Sigma'_{ctx2} \parallel \Gamma', \text{skip } | id \downarrow \kappa$

By assumption

(10) $E'_1 \downarrow \kappa \leq E_2 \downarrow \kappa$

sub-subcase ii. \(\ell^- \not\subseteq \kappa\)

By EXTCORE2

(1) $ExtCoreR \downarrow \kappa = \cdot, ExtCoreR_{ctx} \parallel \Gamma, \text{ret } v | id \notin \Sigma_1 \downarrow \kappa$

By BROWSERSTATE2, EXTCORE2

(2) $\psi_1 \downarrow \kappa = \cdot, ExtCoreR_{ctx} \parallel \Gamma, \text{skip } | id \notin \Sigma'_1 \downarrow \kappa$

By $\Sigma_1 \downarrow \kappa \leq \Sigma_2 \downarrow \kappa, \Sigma_1 = \Sigma_{ctx} \parallel \Gamma, \text{ret } v | id, \Sigma_2 = \Sigma_{ctx} \parallel \Gamma, \text{skip } | id,$ (1) and (2)

(3) $\Sigma'_1 \downarrow \kappa = \Sigma_1 \downarrow \kappa \leq \Sigma_2 \downarrow \kappa$

By assumption

(4) $E'_1 \downarrow \kappa = E_1 \downarrow \kappa \leq E_2 \downarrow \kappa$

case: RETURN-CS, RETURN-PAGE, RETURN-N-CORE, RETURN-N-CS, RETURN-N-PAGE: the proofs are similar to the proofs for RETURN-CORE.

case: RETURN-CORE-BLOCKING

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\[ \Sigma_{ctx}(id) = (\Psi, Tabs, ExtCoreRs_{ctx}(id), \cdots) \]

\[ \Psi = \psi' \triangleq ProcBlkEvtState(\ell^-, id_r, e) \]

\[ ExtCoreRs_{ctx}(id) = \langle id_r, \cdots, EventHandlers :: EventHandler_{ctx}, \ell \rangle \]

\[ \psi = DoneBlkEvtState(\ell^-, id_r, e, v) \]

\[ \Sigma_{ctx}(id) = \Sigma'_{ctx}(id) | \Psi \equiv \Psi':: \psi \]

\[ \Sigma_{ctx} | \Gamma, ret v | id; E \rightarrow \Sigma'_{ctx} | \Gamma, skip | id; E \]

**RETURN-CORE-BLOCKING**

Let \( \Sigma_1 = (\Psi_1, Tabs_1, ExtCoreRs_1, progInjCSs_1, Extss_1, Cookies_1, MBookmarks_1, histories_1, UI_1) \)

\[ ExtCoreRs_1 = ExtCoreR_{\psi}[\Sigma_1] :: ExtCoreR_1 \]

\[ \Sigma_2 = (\Psi_2, Tabs_2, ExtCoreRs_2, progInjCSs_2, Extss_2, Cookies_2, MBookmarks_2, histories_2, UI_2) \]

By assumptions

(A1) \[ \Sigma_1 = \Sigma_{ctx} | \Gamma, ret v | id \]

(A2) \[ ExtCoreR_1 = ExtCoreRs_{ctx} | \Gamma, ret v | id = (id, (\|\Gamma\|, cmd, EventHandlers_1 :: EventHandler_{ctx}|ret v|, \ell) \]

(A3) \[ EventHandler_{ctx}|ret v| = \langle id, \cdots, blocking, some(e, id_r) \rangle \]

(A4) \[ \Psi_1 = \psi_{1a} \Psi_1 = ProcBlkEvtState(\ell^-, id_r, e) \]

(A5) \[ \psi_{1b} = DoneBlkEvtState(\ell^-, id_r, e, v) \]

(A6) \[ \Sigma'_{ctx} | \Gamma, skip | id = \Sigma_{ctx} | \Gamma, skip | id | \Psi_1 \equiv \psi_{1b} \]

(A7) \[ \Sigma'_{ctx} | \Gamma, skip | id \]

**sub-sub-case \( i. \ell^- \subseteq \kappa \)**

By **EXTCORE1**

(1) \[ ExtCoreRs_{ctx} | \Gamma, ret v | id \]

By definition

(2) \[ ExtCoreRs_{ctx} | \Gamma, ret v | id \]

By \( \Sigma_1 \uparrow_\kappa \leq \Sigma_2 \uparrow_\kappa \)

(3) \[ ExtCoreRs_1 \uparrow_\kappa \leq c ExtCoreRs_2 \uparrow_\kappa \]

(4) \[ \Psi_1 \downarrow_\kappa \leq \Psi_2 \downarrow_\kappa \]

By (3)

(5) \[ ExtCoreRs_1 \downarrow \kappa \leq ExtCoreRs_2 \downarrow \kappa \]

(6) \[ ExtCoreRs_1 = ExtCoreRs_2 :: ExtCoreR_2, s.t. ExtCoreR_2 \downarrow \kappa \leq ExtCoreR_1 \downarrow \kappa \]

Let \( EventHandler_{2\cdot ctx}|ret v| = \langle id, \cdots, blocking, some(e, id_r) \rangle \]

By (7)

(8) \[ \kappa \leq \kappa \]

By (4), Lemma

(9) \[ \psi_1 \equiv \Psi_1 :: ExtCoreRs_1 :: \Psi_1, \text{where } \psi_1 \sim_\kappa e \]

\[ \Psi_1 \equiv \text{contains states of the form ProcBlkEvtState(\ell^-, e)} \]

\[ \Psi_1 \equiv \text{contains states of the form ProcBlkEvtState}(\ell^-, e) \]

\[ \exists \psi \in \Psi_1, \text{s.t. } \psi = \text{ProcBlkEvtState}(\ell^-, e) \]

(10) \[ \forall \psi \in \psi_1 :: ExtCoreRs_1 :: \Psi_1, \text{labOf}(\psi) = \text{labOf}(e) \]

(11) \[ \psi_{1a} \in \psi_1 \]

(12) \[ \psi_{1b} \equiv \psi_1 :: ExtCoreRs_1 :: \Psi_2 \]

\[ \exists \psi \in \Psi_2, \text{s.t. } \psi = \text{ProcBlkEvtState}(\ell^-, e) \]

let \( \Sigma_2 = \Sigma_{ctx} | \Gamma, ret v | id \), by (6), (11), (12), we can apply **RETURN-CORE-BLOCKING** to \( \Sigma_2 \).

(13) \[ \psi_{2b} = \text{ProcBlkEvtState}(\ell^-, id_r, e, v) = \psi_{1b} \]

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(14) $\Sigma'_{ctx2} \vdash \Gamma, \text{skip} \mid id = \Sigma_{ctx2} \parallel \Gamma, \text{skip} \mid id [\Psi_2 \leftarrow \Psi_2 \vdash \psi_{2b}]

(15) \Sigma_{ctx2} \vdash \Gamma, \text{ret} \mid id; E_2 \overset{\tau}{\rightarrow} \Sigma'_{ctx2} \parallel \Gamma, \text{skip} \mid id; E'_2, E'_2 = E_2$

RETURN-CORE-BLOCKING does not change the event handler other than the current command

(16) $ExtCoreR_{ctx} \parallel \Gamma, \text{skip} \mid id \downarrow \kappa \le c ExtCoreR_{ctx'} \parallel \Gamma, \text{skip} \mid id \downarrow \kappa$

By (9), (13), BROWSERSTATE1, Lemma 10

(17) $(\Psi_1 \vdash \psi_{1b}) \downarrow \kappa \le (\Psi_2 \vdash \psi_{2b}) \downarrow \kappa$

By $\Sigma_1 \downarrow \kappa \le \Sigma_2 \downarrow \kappa$, $\Sigma_1 = \Sigma_{ctx} \parallel \Gamma, \text{ret} \mid id$, $\Sigma_2 = \Sigma_{ctx2} \parallel \Gamma, \text{ret} \mid id$, (A6) (14), (17) and STATE

(18) $\Sigma'_{ctx} \parallel \Gamma, \text{skip} \mid id \downarrow \kappa \le \Sigma'_{ctx2} \parallel \Gamma, \text{skip} \mid id \downarrow \kappa$

By assumption, (A7), (15)

(19) $E'_1 \downarrow \kappa \le E'_2 \downarrow \kappa$

sub-case ii. $\ell \not\in \kappa$

By ExtCore2

(1) $ExtCoreR \downarrow \kappa = \cdot, ExtCoreR_{ctx} \parallel \Gamma, \text{ret} \mid id \not\in \Sigma_1 \downarrow \kappa$

By BROWSERSTATE2, Lemma 1

(2) $\psi_{1b} \downarrow \kappa = \cdot, ExtCoreR_{ctx} \parallel \Gamma, \text{skip} \mid id \not\in \Sigma'_1 \downarrow \kappa$

(3) $(\Psi_1 \vdash \psi_{1b}) \downarrow \kappa \le (\Psi_2 \vdash \psi_{2b}) \downarrow \kappa$

By $\Sigma_1 \downarrow \kappa \le \Sigma_2 \downarrow \kappa$, $\Sigma_1 = \Sigma_{ctx} \parallel \Gamma, \text{ret} \mid id$, and $\Sigma'_1 = \Sigma'_{ctx} \parallel \Gamma, \text{skip} \mid id$, (2) and (3)

(4) $\Sigma'_1 \downarrow \kappa = \Sigma_1 \downarrow \kappa \le \Sigma_2 \downarrow \kappa$

By assumption

(5) $E'_1 \downarrow \kappa = E_1 \downarrow \kappa \le E_2 \downarrow \kappa$

case: SKIPAPICALL-S1

There are three subcases: (1) the script is a page script handler, (2) the script is a content script and (3) the script is in the extension core.

\[
\ell = \text{ctxOfld}(\Sigma_{ctx} \parallel \Gamma, API_s(\bar{v}) \mid id, id) \quad \ell \not\in \kappa \quad \text{labOf}(API_s) \quad \text{the last argument of } \bar{v} \text{ is not a label} \quad \Sigma_{ctx} \parallel \Gamma, API_s(\bar{v}) \mid id; E \overset{\tau}{\rightarrow} \Sigma_{ctx} \parallel \Gamma, \text{void} \mid id; E'_1 \quad \text{SKIPAPICALL-S1}
\]

Subcase: the script is a page script handler.

Let $\Sigma_1 = (\Psi_1, \text{Tabs}_1 :: \text{Tab}_1, \text{ExtCoreRs}_1, \text{progInjCSs}_1, \text{Exts}_1, \text{Cookies}_1, \text{MBookmarks}_1, \text{histories}_1, \text{UI}_1)$

$\Sigma_2 = (\Psi_2, \text{Tabs}_2, \text{ExtCoreRs}_2, \text{progInjCSs}_2, \text{Exts}_2, \text{Cookies}_2, \text{MBookmarks}_2, \text{histories}_2, \text{UI}_2)$

By assumptions

$\Sigma_1 = \Sigma_{ctx} \parallel \Gamma, API_s(\bar{e}) \mid id$

$\text{Tab}_1 = \text{Tab}_{ctx} \parallel \Gamma, API_s(\bar{e}) \mid id = (\text{TabID}_1, \text{Docs}_1 :: \text{Doc}_{env} \parallel \Gamma, \text{url}_1, \text{EventHandlers}_1 :: \text{EventHandler}_{ctx} \parallel \Gamma, API_s(\bar{e}) \mid id, \ell_1)$

and $\Sigma'_1 = \Sigma_{ctx} \parallel \Gamma, \text{void} \mid id, E'_1 = E_1$

Assume that the label of the node with ID id is $\ell_n$: ctxOfld($\Sigma_1, id$) = $\ell_n$

sub-case i. $\ell_n \not\in \kappa$

By Lemma 5,

$\ell_n \not\in \kappa$, and exists $\text{node}_{env} \mid id \in \text{Doc}_{env} \parallel \Gamma \downarrow \kappa$

By definition of Prune.

(1) $\text{EventHandler}_{ctx} \parallel API_s(\bar{e}) \mid id \in \text{Tab}_1 \downarrow \kappa$

By $\Sigma_1 \downarrow \kappa \le \Sigma_2 \downarrow \kappa$

(2) $\text{Tab}_2 = \text{Tabs}_2 :: \text{Tab}_2$ and $\text{EventHandler}_{ctx} \parallel API_s(\bar{e}) \mid id \in \text{Tab}_2 \downarrow \kappa$

By definitions and (2)

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(3) exists Docs'_2 ∈ Tab_2 ↓_κ and exists node'_env∥\Gamma∥_id ∈ Docs'_2 s.t. node'_env∥\Gamma∥_id ≤_κ node'_env∥\Gamma∥_id

By (2) and (3)

(4) Tab_2 = (TabID_2, Docs'_2∥\Gamma∥_id, url_2, EventHandlers'_2 :: EventHandler_{ctx}∥API_s(\vec{e})∥_id, \ell_2)

By (3), assumption, and node'_env∥\Gamma∥_id = (id, attributes', nodes', [\Gamma], \ell_n)

(5) \ell_n ≤ skip labOf(API_s)

Apply SKIPAPICALL-S1 to \Sigma_2, let \Sigma_2 = \Sigma_{ctx2}✿ Γ, API_s(\vec{e})∥_id

(6) \Sigma_{ctx2}✿ Γ, API_s(\vec{e})∥_id; \Sigma_2 \rightarrow \Sigma_{ctx2}∥\Gamma, void∥_id; \Sigma_2

\Sigma_1 \perp \Sigma_2; \Sigma_1 = \Sigma_{ctx}✿ Γ, API_s(\vec{e})∥_id, \Sigma_2 = \Sigma_{ctx2}✿ Γ, API_s(\vec{e})∥_id.

and SKIPAPICALL-S1 does not change \Sigma_{ctx} and \Sigma_{ctx2}

(7) \Sigma_{ctx}✿ Γ, void∥_id \perp \Sigma_{ctx2}∥\Gamma, void∥_id \perp \Sigma_2

By assumption

(8) \Sigma_1 \perp \Sigma_2

(9) \Sigma_1 \perp \Sigma_2

sub-case ii. \ell_n \perp \Sigma

By definitions

(1) id \not∈ Docs_1 \perp \kappa and EventHandler_{ctx}∥API_s(\vec{e})∥_id \not∈ Tab_1 \perp \kappa and node_env∥\Gamma∥_id \not∈ Tab_1 \perp \kappa

By \Sigma_1 \perp \Sigma_2; \Sigma_1 = \Sigma_{ctx}✿ Γ, API_s(\vec{e})∥_id, and SKIPAPICALL-S1 does not change \Sigma_{ctx}

(2) \Sigma_{ctx}✿ Γ, void∥_id \perp \Sigma_{ctx2}∥\Gamma, API_s(\vec{e})∥_id \perp \Sigma_2

By assumption

(3) \Sigma_1 \perp \Sigma_2

Subcase: the script is a content script handler

Let \Sigma_1 = (Ψ_1, Tabs_1 :: Tab_1, ExtCoreRs_1, progInjCSs_1, Exts_1, Cookies_1, MBookmarks_1, histories_1, UI_1)

\Sigma_2 = (Ψ_2, Tabs_2, ExtCoreRs_2, progInjCSs_2, Exts_2, Cookies_2, MBookmarks_2, histories_2, UI_2)

By assumptions

\Sigma_1 = \Sigma_{ctx}✿ Γ, API_s(\vec{e})∥_id

Tab_1 = Tab_{ctx}✿ Γ, API_s(\vec{e})∥_id = (TabID_1, Docs_1 :: Doc_{ctx}✿ Γ, API_s(\vec{e})∥_id, url_1, EventHandlers_1, \ell_1)

Doc_{ctx}✿ Γ, API_s(\vec{e})∥_id = (id, url, nodes, DocCSs :: Doc_{ctx}✿ Γ, API_s(\vec{e})∥_id, \ell_d)

DocCS_{ctx}✿ Γ, API_s(\vec{e})∥_id = (id, id, id, [\Gamma], [API_s(\vec{e})], EventHandlers, \ell)

or (id, id, id, [\Gamma], cmd, EventHandlers, :: EventHandler_{ctx}∥API_s(\vec{e})∥, \ell)

sub-case i. \ell \subseteq \kappa

By DS1,

\Sigma_1 \perp \Sigma_2

(1) DocCS_{ctx}✿ Γ, API_s(\vec{e})∥_id \perp \kappa ∈ Tab_1 \perp \kappa

By \Sigma_1 \perp \Sigma_2

(2) Tabs_1 = Tabs'_2 :: Tab_2 and DocCS_{ctx}✿ Γ, API_s(\vec{e})∥_id \perp \kappa ∈ Tab_2 \perp \kappa

By definitions and (2)

(3) exists Docs'_2 ∥Γ∥API_s(\vec{e})∥_id ∈ Docs'_2 ∥Γ∥API_s(\vec{e})∥_id, Docs'_2 ∥Γ∥API_s(\vec{e})∥_id \not∈ Docs'_2 ∥Γ∥API_s(\vec{e})∥_id

By (2) and (3)

(4) Tab_2 = (TabID_2, Docs'_2 ∥Γ∥API_s(\vec{e})∥_id, url_2, EventHandlers'_2, \ell_2)

By assumption

(5) \ell \subseteq labOf(API_s)
Apply \(\text{SKIPAPICALL-S1}\) to \(\Sigma_2\), let \(\Sigma_2 = \Sigma_{ctx2} \mid \Gamma, \text{API}_s(\vec{e}) \mid_{id}\).

By assumption

- \(\Sigma_1 \downarrow_{\kappa} \Sigma_2 \downarrow_{\kappa}\), \(\Sigma_1 = \Sigma_{ctx} \mid \Gamma, \text{API}_s(\vec{e}) \mid_{id}\), \(\Sigma_2 = \Sigma_{ctx2} \mid \Gamma, \text{API}_s(\vec{e}) \mid_{id}\).
- \(\text{SKIPAPICALL-S1}\) does not change \(\Sigma_{ctx}\) and \(\Sigma_{ctx2}\).

By assumption

- \(\Sigma_{ctx} \mid \Gamma, \text{void} \mid_{id} \downarrow_{\kappa} \Sigma_{ctx2} \mid \Gamma, \text{void} \mid_{id} \downarrow_{\kappa}\).

By definition

- \(\Sigma_1 \downarrow_{\kappa} \Sigma_2 \downarrow_{\kappa}\).
- \(\Sigma_1' = \Sigma_1 \downarrow_{\kappa} \leq \Sigma_2 \downarrow_{\kappa}\).

**Sub-case ii.** \(\ell \not\subseteq \kappa\)

By \(\text{DS2}\)

1. \(\text{DocCS}_{ctx} \mid \Gamma, \text{API}_s(\vec{e}) \mid_{id} \not\in \text{Tab} \downarrow_{\kappa}\)

By assumption

- \(\Sigma_1 \downarrow_{\kappa} \subseteq \Sigma_2 \downarrow_{\kappa}\), \(\Sigma_1 = \Sigma_{ctx} \mid \Gamma, \text{API}_s(\vec{e}) \mid_{id}\), \(\text{SKIPAPICALL-S1}\) does not change \(\Sigma_{ctx}\).
- \(\Sigma_{ctx} \mid \Gamma, \text{void} \mid_{id} \downarrow_{\kappa} = \Sigma_{ctx2} \mid \Gamma, \text{API}_s(\vec{e}) \mid_{id} \downarrow_{\kappa} \subseteq \Sigma_2 \downarrow_{\kappa}\).

By assumption

- \(\Sigma_1 \downarrow_{\kappa} \subseteq \Sigma_2 \downarrow_{\kappa}\).
- \(\Sigma_1' = \Sigma_1 \downarrow_{\kappa} \leq \Sigma_2 \downarrow_{\kappa}\).

**Sub-case:** the script is in extension core

Let \(\Sigma_1 = (\Psi_1, \text{Tabs}_1, \text{ExtCoreR}_{s_1} :: \text{ExtCoreR}, \text{progInjCS}_{s_1}, \text{Exts}_1, \text{sMode}_1)\)

\(\Sigma_2 = (\Psi_2, \text{Tabs}_2, \text{ExtCoreR}_{s_2}, \text{progInjCS}_{s_2}, \text{Exts}_2, \text{Cookies}_2, \text{MBookmarks}_2, \text{histories}_2, \text{UI}_2)\)

By assumptions

- \(\Sigma_1 = \Sigma_{ctx} \mid \Gamma, \text{API}_s(\vec{e}) \mid_{id}\)
- \(\text{ExtCoreR} = \text{ExtCoreR}_{ctx} \mid \Gamma, \text{API}_s(\vec{e}) \mid_{id} = (id, ([\Gamma], [\text{API}_s(\vec{e})], \text{EventHandlers}), \ell)\)
- or \(id, ([\Gamma], \text{cmd}, \text{EventHandlers} :: \text{EventHandler}_{ctx} \mid \text{API}_s(\vec{e})), \ell)\)

**Sub-case i.** \(\ell \not\subseteq \kappa\)

By \(\text{ExtCORE1}\)

- \(\text{ExtCoreR}_{ctx} \mid \Gamma, \text{API}_s(\vec{e}) \mid_{id} \downarrow_{\kappa} = (id, ([\Gamma], [\text{API}_s(\vec{e})], \text{EventHandlers} \downarrow_{\kappa}), \ell)\)
- or \(\text{ExtCoreR}_{ctx} \mid \Gamma, \text{API}_s(\vec{e}) \mid_{id} \downarrow_{\kappa} = (id, ([\Gamma], \text{API}_s(\vec{e}), \text{EventHandlers} \downarrow_{\kappa} :: \text{EventHandler}_{ctx} \mid \text{cmd} \downarrow_{\kappa}), \ell)\)

By definition

- \(\text{ExtCoreR}_{ctx} \mid \Gamma, \text{API}_s(\vec{e}) \mid_{id} \downarrow_{\kappa} \in \Sigma_{ctx} \downarrow_{\kappa}\)

By assumption

- \(\Sigma_1 \downarrow_{\kappa} \subseteq \Sigma_2 \downarrow_{\kappa}\).
- \(\Sigma_2 \downarrow_{\kappa} \subseteq \text{ExtCoreR}_{ctx} \mid \Gamma, \text{API}_s(\vec{e}) \mid_{id} \downarrow_{\kappa} \subseteq \Sigma_{ctx} \downarrow_{\kappa}\).

By definitions and (2)

- \(\exists \text{ExtCoreR}_{ctx} ' \mid \Gamma, \text{API}_s(\vec{e}) \mid_{id} \downarrow_{\kappa} \in \text{ExtCoreR}_{ctx} \mid \Gamma, \text{API}_s(\vec{e}) \mid_{id} \downarrow_{\kappa}\)

By definitions and assumption

- \(\text{ctxOfId}(\Sigma_2, \text{id}) = \ell', \ell' = \ell, \ell' \not\subseteq \emptyset \text{ labOf}(\text{API}_s)\)

Apply \(\text{SKIPAPICALL-S1}\) to \(\Sigma_2\), let \(\Sigma_2 = \Sigma_{ctx2} \mid \Gamma, \text{API}_s(\vec{e}) \mid_{id}\).

By assumption

- \(\Sigma_1 \downarrow_{\kappa} \subseteq \Sigma_2 \downarrow_{\kappa}\), \(\Sigma_1 = \Sigma_{ctx} \mid \Gamma, \text{API}_s(\vec{e}) \mid_{id}\), \(\Sigma_2 = \Sigma_{ctx2} \mid \Gamma, \text{API}_s(\vec{e}) \mid_{id}\).

By assumption

- \(\Sigma_{ctx} \mid \Gamma, \text{void} \mid_{id} \downarrow_{\kappa} \leq \Sigma_{ctx2} \mid \Gamma, \text{void} \mid_{id} \downarrow_{\kappa}\).

By assumption

- \(\Sigma_{ctx} \mid \Gamma, \text{void} \mid_{id} \downarrow_{\kappa} \leq \Sigma_{ctx2} \mid \Gamma, \text{void} \mid_{id} \downarrow_{\kappa}\).

By assumption

- \(\Sigma_{ctx} \mid \Gamma, \text{void} \mid_{id} \downarrow_{\kappa} \leq \Sigma_{ctx2} \mid \Gamma, \text{void} \mid_{id} \downarrow_{\kappa}\).

**Sub-case ii.** \(\ell \not\subseteq \kappa\)

By \(\text{ExtCORE2}\)

- \(\text{ExtCoreR} \downarrow_{\kappa} = \cdot, \text{ExtCoreR}_{ctx} \mid \Gamma, \text{API}_s(\vec{e}) \mid_{id} \not\in \Sigma_{ctx} \downarrow_{\kappa}\)
By $\Sigma_1 \downarrow \kappa \leq \Sigma_2 \downarrow \kappa$, $\Sigma_1 = \Sigma_{ctx} \parallel_\Gamma, API_s(\vec{v}) \parallel_{id}$, and SKIPAPICALL-S1 does not change $\Sigma_{ctx}$.

(2) $\Sigma_{ctx} \parallel_\Gamma, void \parallel_{id} \downarrow \kappa = \Sigma_{ctx} \parallel_\Gamma, API_s(\vec{v}) \parallel_{id} \downarrow \kappa \leq \Sigma_2 \downarrow \kappa$

By assumption

(3) $\mathcal{E}_1 \downarrow \kappa \leq \mathcal{E}_2 \downarrow \kappa$

case: SKIPAPICALL-S2, SKIPAPICALL-A1, SKIPAPICALL-A2, the proofs are similar to the proofs for SKIPAPICALL-S1.

case: FIREAPICALL-S1

$$\ell = ctxOfld(\Sigma_{ctx} \parallel_\Gamma, API_s(\vec{v}) \parallel_{id}, id)$$

the last argument of $\vec{v}$ is not a label

$$\ell \subseteq \text{labOf}(API_s) \quad \Sigma_{ctx} \parallel_\Gamma, API_s(\vec{v}) \parallel_{id} \Rightarrow_{API_s} \Sigma'; \mathcal{E}'$$

By assumption

$$\Sigma_1 = \Sigma_{ctx} \parallel_\Gamma, API_s(\vec{v}) \parallel_{id}$$

$$\Sigma_{ctx} \parallel_\Gamma, API_s(\vec{v}) \parallel_{id} \Rightarrow_{API_s} \Sigma_1'; \mathcal{E}_1'$$

$$\Sigma_{ctx} \parallel_\Gamma, API_s(\vec{v}) \parallel_{id}; \mathcal{E} \Rightarrow_{\beta} \Sigma'; \mathcal{E} :: \mathcal{E}'$$

By Lemma 15, $\Sigma_1 \downarrow \kappa \leq \Sigma_2 \downarrow \kappa$

if $\beta = \tau$, then

either $\Sigma_2 \Rightarrow_{\tau} \Sigma_2'; \mathcal{E}_2'; \Sigma_1 \downarrow \kappa \leq \Sigma_2 \downarrow \kappa$ and $\mathcal{E}_1 \downarrow \kappa \leq \mathcal{E}_2 \downarrow \kappa$

or $\mathcal{E}_1 \downarrow \kappa \leq \Sigma_2 \downarrow \kappa$ and $\mathcal{E}_1 \downarrow \kappa$.

if $\beta = \alpha$, $\alpha \downarrow \kappa = \cdot$, then $\mathcal{E}_1 \downarrow \kappa \leq \Sigma_2 \downarrow \kappa$ and $\mathcal{E}_1 \downarrow \kappa$.

if $\beta = \alpha$, $\alpha \downarrow \kappa = \alpha$

$\Sigma_2 \Rightarrow_{\alpha} \Sigma_2'; \mathcal{E}_2'$

$\Sigma_2; \mathcal{E}_2 \Rightarrow_{\alpha} \Sigma_2'; \mathcal{E}_2 :: \mathcal{E}_2'$

where $\Sigma_1 \downarrow \kappa \leq \Sigma_2 \downarrow \kappa$ and $\mathcal{E}_1 \downarrow \kappa \leq \mathcal{E}_2 \downarrow \kappa$.

case: FIREAPICALL-S2. The proofs are similar to the proofs for FIREAPICALL-S1.

case: FIREAPICALL-A-CORE

$$\Sigma_{ctx}(id) = (\Psi, \text{tabs}, \text{ExtCoreRs}_{ctx}(id), \cdots) \quad \text{ExtCoreRs}_{ctx}(id) \in \text{ExtCoreRs}_{ctx}(id)$$

$$\text{ExtCoreRs}_{ctx}(\Gamma, API_a(\vec{v})) \parallel_{id} = (id, \cdot, \text{EventHandler}, \ell)$$

$$\text{labOf}(API_a) \subseteq \ell^* \quad \text{when } \vec{v} = \cdots, \kappa_1, \ell \Rightarrow \kappa_1 \quad \text{callbackOf}(\vec{v}) = x.cmd$$

$$\text{fresh}(id_{cb}), \text{fresh}(id_h) \quad \text{eh} = (id_h, id_{cb}, x.cmd, \cdot, \text{skip, void, nonblocking, none})$$

$$\text{ExtCoreRs}_{ctx}(id) = \text{ExtCoreRs}_{ctx}(id)[\text{EventHandler} \Leftarrow \text{EventHandler} :: \text{eh}]$$

$$\text{ExtCoreRs}_{ctx}(\Gamma, API_a(\vec{v})) \parallel_{id} = \text{ExtCoreRs}_{ctx}(\Gamma, API_a(\vec{v}))$$

$$\psi = \text{agmcAPIstate}(\ell, id_{cb}, API_a(\vec{v}))$$

$$\Sigma'_{ctx}(id) = \Sigma_{ctx}(id)[\text{ExtCoreRs}_{ctx}(id) \Leftarrow \text{ExtCoreRs}_{ctx}'(id)]$$

$$\Psi = \Psi \Leftarrow \psi$$

$$\Sigma_{ctx} \parallel_\Gamma, API_a(\vec{v}) \parallel_{id} \Rightarrow_{\tau} \Sigma_{ctx}' \parallel_\Gamma, \text{skip} \parallel_{id}; \mathcal{E}$$

By assumption

$$\Sigma_1 = \Sigma_{ctx} \parallel_\Gamma, API_a(\vec{v}) \parallel_{id}$$

Let $\Sigma_1 = (\Psi_1, \text{tabs}_1, \text{ExtCoreRs}_1 :: \text{ExtCoreR}, \text{proglnCuts}_1, \text{Extts}_1, \text{Cookies}_1, \text{MBookmarks}_1, \text{histories}_1, \text{UI}_1)$

$\Sigma_2 = (\Psi_2, \text{tabs}_2, \text{ExtCoreRs}_2, \text{proglnCuts}_2, \text{Extts}_2, \text{Cookies}_2, \text{MBookmarks}_2, \text{histories}_2, \text{UI}_2)$

By assumption

$$\Sigma_1 = \Sigma_{ctx} \parallel_\Gamma, API_a(\vec{v}) \parallel_{id}$$

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ExtCoreR = ExtCoreR_{ctx} \upharpoonright \Gamma, API_a(\vec{v}) \upharpoonright id = (id, (\|\Gamma\|, \|API_a(\vec{v})\|, EventHandlers), \ell)

or (id, (\|\Gamma\|, \|API_a(\vec{v})\|, EventHandlers :: ExtendedHandler_{ctx} \|API_a(\vec{v})\|), \ell)

callbackOf(\vec{v}) = x.cmd, fresh(id_{cb})

eh = (id_{cb}, x.cmd, .., skip, void, nonblocking, none)

ExtCoreR_{ctx}'(id) = ExtCoreR_{ctx}(id)[EventHandlers \Leftarrow EventHandlers :: eh]

\psi = asyncAPIState(\ell', id_{cb}, API_a(\vec{v}))

\Sigma'_{ctx}(id) = \Sigma_{ctx}(id) \Leftarrow ExtCoreR_{ctx}(id) \Leftarrow ExtCoreR_{ctx}'(id)[\Psi \Leftarrow \Psi :: \psi]

\Sigma' = \Sigma'_{ctx}(\Gamma, skip) \downarrow id

**sub-subcase i.** \( \ell' \subseteq \kappa \)

**By EXTCore1,**

\( ExtCoreR_{ctx} \upharpoonright \Gamma, API_a(\vec{v}) \upharpoonright id \downarrow \kappa = (id, (\|\Gamma\|, \|API_a(\vec{v})\|, EventHandlers \downarrow \kappa), \ell) \)

or \( ExtCoreR_{ctx} \upharpoonright \Gamma, API_a(\vec{v}) \upharpoonright id \downarrow \kappa = (id, (\|\Gamma\|, \|API_a(\vec{v})\|, EventHandlers \downarrow \kappa :: ExtendedHandler_{ctx} \upharpoonright cmd \downarrow \kappa), \ell) \)

**By definition**

1. \( ExtCoreR_{ctx} \upharpoonright \Gamma, API_a(\vec{v}) \upharpoonright id \downarrow \kappa \in \Sigma_1 \downarrow \kappa \)

2. \( ExtCoreR_{ctx} \upharpoonright \Gamma, API_a(\vec{v}) \upharpoonright id \downarrow \kappa \in \text{ExtCoreR}_{ctx} \downarrow \kappa \)

**By definitions and (2)**

3. \( \exists \text{ ExtCoreR}_{ctx}\_{ext2} \upharpoonright \Gamma, API_a(\vec{v}) \upharpoonright id \downarrow \kappa \in \text{ExtCoreR}_{ctx} \downarrow \kappa \)

s.t. \( ExtCoreR_{ctx} \upharpoonright \Gamma, API_a(\vec{v}) \upharpoonright id \downarrow \kappa \leq ExtCoreR_{ctx}\_{ext2} \upharpoonright \Gamma, API_a(\vec{v}) \upharpoonright id \downarrow \kappa \)

4. \( ExtCoreR_{ctx}\_{ext2} \upharpoonright \Gamma, API_a(\vec{v}) \upharpoonright id = (id, (\|\Gamma\|, \|API_a(\vec{v})\|, EventHandlers_{\downarrow \kappa}), \ell) \)

or \( (id, (\|\Gamma\|, \|API_a(\vec{v})\|, EventHandlers_{\downarrow \kappa} :: ExtendedHandler_{ctx} \upharpoonright cmd \downarrow \kappa), \ell) \)

**Apply FIREAPICALL-A-CORE to \( \Sigma_2, \) let \( \Delta = \Sigma_{ctx2} \upharpoonright \Gamma, API_a(\vec{v}) \upharpoonright id \)

5. \( \Sigma_{ctx2} \upharpoonright \Gamma, API_a(\vec{v}) \upharpoonright id : \mathcal{E}_2 \xrightarrow{\Sigma_{ctx2}} \Gamma, \text{void} \upharpoonright id : \mathcal{E}_2 \)

6. \( \text{Let} \ id_{cb2} = id_{cb}, \text{then} \ ch_2 = (id_{cb2}, x.cmd, .., skip, void, nonblocking, none) = eh \)

7. \( ExtCoreR_{\downarrow \kappa} (id) = ExtCoreR_{ctx}\_{ext2}(id)[EventHandlers_{\downarrow \kappa} \Leftarrow EventHandlers_{\downarrow \kappa}] \)

8. \( ExtCoreR_{\downarrow \kappa} (id) = ExtCoreR_{\downarrow \kappa} (id)[ExtCoreR_{ctx}\_{ext2}(id) \Leftarrow ExtCoreR_{\downarrow \kappa}(id)] \)

9. \( \psi_2 = \psi = \text{asyncAPIState}(\ell', id_{cb}, API_a(\vec{v})) \)

10. \( \Sigma_{ctx}(id) = \Sigma_{ctx}(id)[ExtCoreR_{\downarrow \kappa}(id) \Leftarrow ExtCoreR_{\downarrow \kappa}(id)][\Psi_2 \Leftarrow \Psi_2 :: \psi_2] \)

**By assumption**

11. \( \Sigma_{ctx}(\Gamma, skip) \upharpoonright id \downarrow \kappa \leq \Sigma_{ctx}\downarrow \kappa \)

**By assumption**

12. \( \mathcal{E}_1 \downarrow \kappa \leq \mathcal{E}_2 \downarrow \kappa \)

**sub-case ii.** \( \ell' \nleq \kappa \)

**By EXTCore2 and BROWSERSTATE2**

1. \( ExtCoreR \downarrow \kappa = \cdot, ExtCoreR_{ctx} \upharpoonright \Gamma, API_a(\vec{v}) \upharpoonright id \notin \Sigma_1 \downarrow \kappa \)

2. \( ExtCoreR' \downarrow \kappa = \cdot, ExtCoreR_{ctx} \upharpoonright \Gamma, \text{skip} \upharpoonright id \notin \Sigma_1 \downarrow \kappa \)

3. \( \psi \downarrow = \cdot \)

**By assumptions, \( \Sigma_1 \downarrow \kappa \leq \Sigma_2 \downarrow \kappa \), \( \Sigma_1 = \Sigma_{ctx} \upharpoonright \Gamma, API_a(\vec{v}) \upharpoonright id, \Sigma_1' = \Sigma_{ctx} \upharpoonright \Gamma, \text{skip} \upharpoonright id, \) and \( \Sigma_{ctx}'(id) = \Sigma_{ctx}(id)[ExtCoreR_{ctx}(id) \Leftarrow ExtCoreR_{ctx}'(id)][\Psi \Leftarrow \Psi :: \psi] \)

4. \( \Sigma_{ctx}' \upharpoonright \Gamma, \text{skip} \upharpoonright id \downarrow \kappa = \Sigma_{ctx} \upharpoonright \Gamma, API_a(\vec{v}) \upharpoonright id \downarrow \kappa \leq \Sigma_2 \downarrow \kappa \)

**By assumption**

5. \( \mathcal{E}_1 \downarrow \kappa \leq \mathcal{E}_2 \downarrow \kappa \)

**case: FIREAPICALL-A-CS and FIREAPICALL-A-PAGE.** The proofs are similar to the proofs for FIREAPICALL-A-CORE.

**case: EventFireNonBL**
By assumptions
\[ \forall ExtCoreR \in ExtCoreRs, \text{EHs} = \text{getActiveHandlers}(ExtCoreR, e), \]
\[ \forall e \in \text{EHs}, \text{labOf}(eh) \rightarrow \text{labOf}(e) \Rightarrow \text{isBlocking}(eh) = \text{false} \]
\[ (\psi', e') = \text{nextState}(\psi, \text{void}) \Rightarrow \Sigma' = \Sigma[\psi \leftarrow \psi'] \leftarrow \text{ExtCoreRs} \leftarrow \text{ExtCoreRs} \leftarrow e \]
\[ \Sigma; \mathcal{E} :: e \rightarrow \Sigma'^{\mathcal{E}}; \mathcal{E} :: e' \]

**By assumptions**

(A1) \[ \Sigma_1 = (\Psi_1, \text{Tabs}_1, \text{ExtCoreRs}_1, \cdots), \Psi_1 = \Psi''_1::\psi_1 \]

(A2) \[ \mathcal{E}_1 = \mathcal{E}''_1::e_1, \psi_1 \sim_e e_1 \]

(A3) \[ \forall ExtCoreR \in \text{ExtCoreRs}_1, \text{EHs} = \text{getActiveHandlers}(\text{ExtCoreR}, e_1), \]
\[ \forall e \in \text{EHs}, \text{labOf}(eh) = \text{labOf}(e) \Rightarrow \text{isBlocking}(eh) = \text{false} \]

(A4) \[ (\psi'_1, e'_1) = \text{nextState}(\psi_1, \text{void}) \]

(A5) \[ \Sigma'_1 = \Sigma_1[\psi_1 \leftarrow \psi'_1][\text{ExtCoreRs}_1 \leftarrow \text{ExtCoreRs}_1 \leftarrow e_1] \]

(A6) \[ \mathcal{E}'_1 = \mathcal{E}''_1::e'_1 \]

(A7) \[ \Sigma_2 = (\Psi_2, \text{Tabs}_2, \text{ExtCoreRs}_2, \cdots) \]

**sub-case i. labOf\((e_1) \subseteq \kappa\)**

By \( \psi_1 \sim_e e_1 \), Lemma 1, BROWSERSTATE1

(1) \[ \text{labOf}(\psi_1) = \text{labOf}(e_1) \subseteq \kappa, \psi_1 \sim_e \psi_1 \]

By \( \mathcal{E}_1 \downarrow_{\kappa} \leq \mathcal{E}_2 \downarrow_{\kappa}, \text{labOf}(e_1) \subseteq \kappa, \text{EVENT1} \)

(2) \[ e_1 \downarrow_{\kappa} = e_1, \exists e_2 \in \mathcal{E}_2, \text{s.t. } \mathcal{E}_2 = \mathcal{E}''_2 :: e_2, \mathcal{E}''_2 \subseteq \mathcal{E}_2 \downarrow_{\kappa}, e_1 \downarrow_{\kappa} \leq e_2 \downarrow_{\kappa}, \text{that is } e_2 = e_1. \]

By \( \psi_1 \downarrow_{\kappa} \leq \psi_2 \downarrow_{\kappa}, e_1 \text{ is a blocking event}, e_2 = e_1 \)

(3) \[ \Psi_1 \downarrow_{\kappa} \leq \psi_2 \downarrow_{\kappa} \]

(4) \[ \Psi_1 \downarrow_{\kappa} \leq \psi_2 \downarrow_{\kappa} \]

(5) \[ \Psi_1 \downarrow_{\kappa} = \psi_1 :: \Psi_{11} :: \Psi_{12} :: \Psi_{13} \]
\[ \Psi_{11} \text{ contains states of the form } \text{ProcBlkEvtState}(\cdot, \cdot, e_1) \]
\[ \Psi_{12} \text{ contains states of the form } \text{DoneBlkEvtState}(\cdot, \cdot, e_1, \cdot) \]
\[ \Psi_{13} \text{ contains states of the form } \text{DoneBlkEvtState}(\cdot, \cdot, e_1, \cdot) \]

(6) \[ \Psi_{21} \downarrow_{\kappa} = \psi_1 :: \Psi_{11} :: \Psi_{12} :: \Psi_{23} \]
\[ \Psi_{23} \text{ contains states of the form } \text{ProcBlkEvtState}(\cdot, \cdot, e_2), \text{or } \Psi = \text{DoneBlkEvtState}(\cdot, \cdot, e_2, \cdot) \]

**By EVENTFIRENONBL is an event firing rule, Lemma 9**

(7) \[ \psi_{11} = \cdot, \psi_{12} = \cdot \]

(8) \[ \psi_{13} \leq \psi_{23} \]

By \( \psi_1 \sim_e e_1, \psi_1 \in \psi_2 \downarrow_{\kappa}, e_1 = e_2. \)

(9) \[ \psi_1 \in \psi_2, \text{and } \psi_1 \sim_e e_2, \psi_2 = \psi''_2::\psi_1 \]

By ExtCoreRs \( \downarrow_{\kappa} \leq \downarrow_{\kappa} \) ExtCoreRs_2 \( \downarrow_{\kappa} \)

(10) \[ \downarrow_{\kappa} \leq \downarrow_{\kappa} \]
\[ \text{ExtCoreRs}_1 \downarrow_{\kappa} \leq \downarrow_{\kappa} \quad \text{ExtCoreRs}_1 \downarrow_{\kappa} \leq \downarrow_{\kappa} \quad \text{ExtCoreRs}_2 \downarrow_{\kappa} \]
ExtCoreR' = (id_ext, \ldots, EventHandlers_2 :: eh_2, e)

\begin{align*}
  e_{h1} &= (eventTypeOf(e), \ldots, eventQueue_1, \ldots, blocking, \ldots) \\
  e_{h2} &= (eventTypeOf(e), \ldots, eventQueue_2, \ldots, blocking, \ldots)
\end{align*}

ExtCoreR' \leq ExtCoreR'

By (A3), (12), \( e_1 = e_2 \)

(13) \( \forall ExtCoreR' \in ExtCoreRs_2, EHS = getActiveHandlers(ExtCoreR', e_2), \)

\( \forall eh \in EHS, \text{labOf}(eh)^\neg = \text{labOf}(e_2) \Rightarrow \text{isBlocking}(eh) = false \)

This can be show by contradiction: if (11) is not true, then (A3) is not satisfied.

By (9), (13), apply EVENTFIRENONBL to \( \Sigma_2 \)

(14) \( (\psi'_1, e'_1) = nextState(\psi_1, \text{void}) \)

(15) \( \Sigma'_2 = \Sigma_2|_\Psi_2 \Leftarrow \Psi'_2 :: \psi'_1_{[\hat{\Sigma} \exists CoreRs_2 \Leftarrow \text{ExtCoreRs}_2 <_Q e_2]} \)

(16) \( \Sigma'_2; \Sigma_2 \xrightarrow{\tau} \Sigma'_2; \Sigma'_2 = \Sigma''_2 :: e'_1 \)

By \( \Psi_{13} \leq_c \Psi_{23}, \text{Lemma 10} \)

(17) \( \Psi_{13} :: \psi'_1 \leq_c \Psi_{23} :: \psi'_1 \)

(\( \Psi''_2 :: \psi'_1 \)) \( \Downarrow_\kappa = \Psi_{13} :: \psi'_1 \leq_c \Psi_{23} :: \psi'_1 \)

By ExtCoreRs_1 \( \downarrow_\kappa \leq ExtCoreRs_2 \downarrow_\kappa, e_1 = e_2, \text{Lemma 3} \)

(18) \( \text{ExtCoreRs}_1 <_Q e_1 \downarrow_\kappa \leq_c (\text{ExtCoreRs}_2 <_Q e_2) \downarrow_\kappa \)

By \( \Sigma_1 \downarrow_\kappa \leq \Sigma_2 \downarrow_\kappa, (15), (17), (18), \text{STATE} \)

(19) \( \Sigma'_1 \downarrow_\kappa \leq \Sigma''_2 \downarrow_\kappa \)

By (A6), (2), (15)

(20) \( \Sigma'_1 \downarrow_\kappa \leq \Sigma'_2 \downarrow_\kappa \)

**sub-subcase ii. labOf(e_1) \nsubseteq \kappa**

By Lemma 2

(1) \( \text{ExtCoreRs}_1 <_Q e_1 \downarrow_\kappa = \text{ExtCoreRs}_1 \downarrow_\kappa \leq \text{ExtCoreRs}_2 \downarrow_\kappa \)

By (A4), Lemma 13

(2) \( \psi_1 \downarrow_\kappa = \cdot, \psi'_1 \downarrow_\kappa = \cdot, e'_1 \downarrow_\kappa = \cdot \)

(3) \( \Psi'_1 \downarrow_\kappa = \Psi_1 \downarrow_\kappa \leq_c \Psi_2 \downarrow_\kappa \) By (1), (3), (A5)

(4) \( \Sigma''_1 \downarrow_\kappa = \Sigma_2 \downarrow_\kappa \)

(5) \( \Sigma'_1 \downarrow_\kappa = \Sigma'_2 \downarrow_\kappa \)

**case: EVENTFIREBL satisfies Lemma 16.**

\( e \) is a blocking event \( \Sigma = (\Psi :: \psi, Tabs, ExtCoreRs, \cdots) \psi \preceq_b e \)

\( \exists \text{ExtCoreR} \in \text{ExtCoreRs}, EHS = \text{getActiveHandlers}(\text{ExtCoreR}, e), \)

\( \exists eh \in EHS, \text{isBlocking}(eh) = true \land \text{labOf}(eh)^\neg = \text{labOf}(e) \)

\( \Sigma' = \Sigma[\text{ExtCoreRs} \Leftarrow \text{ExtCoreRs} <_Q e] \)

\[ \Sigma, \Sigma' \xrightarrow{\tau} \Sigma', \Sigma' \]

**EVENTFIREBL**

By assumptions

(A1) \( \Sigma_1 = (\Psi_1, Tabs_1, ExtCoreRs_1, \cdots), \Psi_1 = \Psi''_1 :: \psi_1 \)

(A2) \( \Sigma_1 = \Sigma''_1 :: e_1, \psi_1 \preceq_b e_1 \)

(A3) \( \exists \text{ExtCoreR} \in \text{ExtCoreRs}_1, EHS = \text{getActiveHandlers}(\text{ExtCoreR}, e_1), \)

\( \exists eh \in EHS, \text{isBlocking}(eh) = true \)

(A4) \( \Sigma''_1 = \Sigma_1[\text{ExtCoreRs}_1 \Leftarrow \text{ExtCoreRs}_1 <_Q e_1] \)

(A5) \( \Sigma'_1 = \Sigma'_1' \)

(A6) \( \Sigma_2 = (\Psi_2, Tabs_2, ExtCoreRs_2, \cdots) \)

**sub-subcase i. labOf(e_1) \nsubseteq \kappa**

By \( \psi_1 \preceq_b e_1, \text{Lemma 1}, \text{BROWSERSTATE1} \)
(1) \(\text{labOf}(\psi_1) = \text{labOf}(e_1) \subseteq \kappa, \psi_1 \downarrow_{\kappa} = \psi_1\)

By \(E_1 \downarrow_{\kappa} \subseteq E_2 \downarrow_{\kappa}, \text{labOf}(e_1) \subseteq \kappa, \text{EVENT1}\)

(2) \(e_1 \downarrow_{\kappa} = e_1, \exists e_2 \in E_2, \text{st. } E_2 = E'_2 \supseteq e_2, E''_2 \downarrow_{\kappa} \subseteq E'_{2} \downarrow_{\kappa}, e_1 \downarrow_{\kappa} \subseteq e_2 \downarrow_{\kappa}, \text{that is } e_2 = e_1.\)

By \(\Psi_1 \downarrow_{\kappa} \subseteq \kappa, \Psi_2 \downarrow_{\kappa}, e_1 \text{ is a blocking event, } e_2 = e_1\)

(3) \(\Psi_1 \downarrow_{\kappa} \subseteq e_1, \Psi_2 \downarrow_{\kappa}\)

(4) \(\Psi_1 \downarrow_{\kappa} \subseteq \Psi_2 \downarrow_{\kappa}\)

(5) \(\Psi_1 \downarrow_{\kappa} = \psi_1 : \Psi_{11} : \Psi_{12} : \Psi_{13}\)

\(\Psi_{11} \text{ contains states of the form } \text{ProcBlkEvtState}(\ldots, e_1)\)

\(\Psi_{12} \text{ contains states of the form } \text{DoneBlkEvtState}(\ldots, e_1, \ldots)\)

\(\exists \psi \in \Psi_{13}, \text{st. } \psi = \text{ProcBlkEvtState}(\ldots, e_1, \ldots)\), or \(\psi = \text{DoneBlkEvtState}(\ldots, e_1, \ldots)\)

(6) \(\Psi_2 \downarrow_{\kappa} = \psi_1 : \Psi_{11} : \Psi_{12} : \Psi_{23}\)

\(\exists \psi \in \Psi_{23}, \text{st. } \psi = \text{ProcBlkEvtState}(\ldots, e_2, \ldots)\), or \(\psi = \text{DoneBlkEvtState}(\ldots, e_2, \ldots)\)

By \(\psi_1 \sim_{\kappa} e_1, \psi_1 \in \Psi_2 \downarrow_{\kappa}, e_1 = e_2, \)

(7) \(\psi_1 \in \Psi_2, \text{ and } \psi_1 \sim_{\kappa} e_2\)

By \(\text{ExtCoreRs}_1 \downarrow_{\kappa} \subseteq \text{ExtCoreRs}_2 \downarrow_{\kappa}\)

(8) \(\text{ExtCoreRs}_1 \downarrow_{\kappa} \subseteq \text{ExtCoreRs}_2 \downarrow_{\kappa}\)

\(\text{ExtCoreRs}_1 \downarrow_{\kappa} \subseteq \text{ExtCoreRs}_2 \downarrow_{\kappa}, \text{ ExtCoreRs}_1 \downarrow_{\kappa} = \text{ExtCoreRs}_{1b1}, \)

\(\text{ExtCoreRs}_2 \downarrow_{\kappa} = \text{ExtCoreRs}_{2b2}, \text{ ExtCoreRs}_{1b1} \leq_{\kappa} \text{ExtCoreRs}_{2b2}\)

\(\text{every core in } \text{ExtCoreRs}_{1b1} \text{ and } \text{ExtCoreRs}_{2b2} \text{ contains a blocking event handler for } e_1, \)

no blocking event handlers for \(e_1\) in \(\text{ExtCoreRs}_{1b1}\) and \(\text{ExtCoreRs}_{2b2}\)

(9) \(\forall \text{ExtCoreR} \in \text{ExtCoreRs}_1 \downarrow_{\kappa}, \exists \text{ExtCoreR'} \in \text{ExtCoreRs}_2 \downarrow_{\kappa}, \text{ st. } \text{ExtCoreR} \downarrow_{\kappa} \subseteq \text{ExtCoreR'} \downarrow_{\kappa}\)

By \(\text{labOf}(e_1) \subseteq \kappa, \text{ and } \forall \text{eh} \in \text{ExtCoreR}, \text{labOf}(\text{eh}) = \text{labOf}(\text{ExtCoreR})\)

(10) \(\forall \text{ExtCoreR} \in \text{ExtCoreRs}_1, \text{ s.t. } \text{EHs} = \text{getActiveHandlers}(\text{ExtCoreR}, e_1), \)

\(\exists \text{eh} \in \text{EHs, isBlocking(} \text{eh}) = \text{true}\)

\(\land \text{labOf}(\text{eh}) = \text{labOf}(e_1)\)

\(\text{labOf}(\text{extCoreR}) \subseteq \kappa, \text{ExtCoreR} \in \text{ExtCoreRs}_{1b1}\)

(11) \(\text{ExtCoreRs}_{1b1} \neq \cdot\)

By \(\text{ExtCoreRs}_{1b1} \leq_{\kappa} \text{ExtCoreRs}_{2b2}\)

(12) \(\forall \text{ExtCoreR} \in \text{ExtCoreRs}_{1b1}, \text{ there is } \text{ExtCoreR'} \in \text{ExtCoreRs}_{2b2}\)

\(\text{s.t. } \text{ExtCoreR} = (id, (\ldots, \text{EventHandler}_{1} : \text{eh}_1, \ldots), \ldots)\)

\(\text{ExtCoreR'} = (id, (\ldots, \text{EventHandler}_{2} : \text{eh}_2, \ldots), \ldots)\)

\(\text{eh}_1 = (\text{eventTypeOf}(e), \ldots, \text{eventQueue}, \ldots, \text{blocking}, \ldots)\)

\(\text{eh}_2 = (\text{eventTypeOf}(e), \ldots, \text{eventQueue}, \ldots, \text{blocking}, \ldots)\)

\(\text{ExtCoreR} \leq \text{ExtCoreR'}\)

By (2), (10), (11), (12), \(e_1 = e_2\)

(13) \(\exists \text{ExtCoreR'} \in \text{ExtCoreRs}_{2b2}, \text{EHs} = \text{getActiveHandlers}(\text{ExtCoreR}, e_2), \)

\(\exists \text{eh} \in \text{EHs, isBlocking(} \text{eh}) = \text{true} \land \text{labOf}(\text{eh}) = \text{labOf}(e_2)\)

By (7), (13), apply \text{EVENTFIREBL} to \(\Sigma_2\)

(14) \(\Sigma_2; E_2 \xrightarrow{e_2} \Sigma'_2; E'_2 = E''_2\)

(15) \(\Sigma'_2 = \Sigma_2[\text{ExtCoreRs}_{2b2} \leftarrow \text{ExtCoreRs}_{2b2} \downarrow_{\kappa} e_2]\)

By \(\text{ExtCoreRs}_1 \downarrow_{\kappa} \subseteq \text{ExtCoreRs}_2 \downarrow_{\kappa}, e_1 = e_2, \text{Lemma 3}\)

(16) \(\text{(ExtCoreRs}_{1b1} \downarrow_{\kappa} e_1) \downarrow_{\kappa} \subseteq (\text{ExtCoreRs}_{2b2} \downarrow_{\kappa} e_2) \downarrow_{\kappa}\)

By \(\Sigma_1 \downarrow_{\kappa} \subseteq \Sigma_2 \downarrow_{\kappa}, \text{STATE}\)

(17) \(\Sigma'_1 \downarrow_{\kappa} \subseteq \Sigma'_2 \downarrow_{\kappa}\)

By (A5), (2), (14)

(18) \(E'_1 \downarrow_{\kappa} \subseteq E'_2 \downarrow_{\kappa}\)
sub-subcase ii. \( \text{labOf}(e_1) \nsubseteq \kappa \)

By Lemma 2

1. \( \text{ExtCoreRs}_1 \prec_Q e_1 \downarrow_\kappa = \text{ExtCoreRs}_1 \downarrow_\kappa \)

By (A4), (1)

2. \( \Sigma'_1 \downarrow_\kappa = \Sigma_1 \downarrow_\kappa \leq \Sigma_2 \downarrow_\kappa \)

By (A2), (A5)

3. \( \mathcal{E}'_1 \downarrow_\kappa \leq \mathcal{E}'_1 \downarrow_\kappa \leq \mathcal{E}_2 \downarrow_\kappa \)

case: BLOCKFinished1

\( e \) is a blocking event \( e \sim_b \psi \)
\( \Sigma = (\Psi, \text{Tabs}, \text{ExtCoreRs}, \ldots) \)
\( \Psi = \Psi_1 :: \psi :: \Psi_2 \)
\( \nexists \psi \in \Psi_1, \text{s.t. } \psi = \text{ProcBlkEvtState}(\ldots, e) \text{ or } \text{DoneBlkEvtState}(\ldots, e) \)
\( \Psi_2 \) contains matching pairs of \( \text{ProcBlkEvtState}(\ldots, id_r, e) \) and \( \text{DoneBlkEvtState}(\ldots, id_r, e, 0) \)
\( \forall \text{ExtCoreR} \in \text{ExtCoreRs}, \text{EHs} = \text{getActiveHandlers}(\text{ExtCoreR}, e), \)
\( \forall eh \in \text{EHs}, \text{labOf}(eh) = \text{labOf}(e) \land \text{isBlocking}(eh) \land e \notin Qof(eh) \)

By assumptions

(A1) \( \Sigma_1 = (\Psi_1, \text{Tabs}_1, \text{ExtCoreRs}_1, \ldots) \)

(A2) \( \Psi_1 = \Psi_{11} :: \psi_1 :: \Psi_{12} \)
\( \psi_1 \sim_b e_1, e_1 \) is a blocking event
\( \nexists \psi \in \Psi_{11}, \text{s.t. } \psi = \text{ProcBlkEvtState}(\ldots, e) \text{ or } \text{DoneBlkEvtState}(\ldots, e) \)
\( \Psi_{12} \) contains matching pairs of \( \text{ProcBlkEvtState}(\ldots, id_r, e) \) and \( \text{DoneBlkEvtState}(\ldots, id_r, e, 0) \)
\( \text{labOf}(\psi_1) = \text{labOf}(e_1) \)

(A3) \( \forall \psi \in \Psi_{12}, \text{labOf}(\psi) = \text{labOf}(e_1), \Psi_{12} \downarrow_\kappa = \Psi_{12} \)

(A4) \( \forall \text{ExtCoreR} \in \text{ExtCoreRs}_1, \text{EHs} = \text{getActiveHandlers}(\text{ExtCoreR}, e_1), \)
\( \forall eh \in \text{EHs}, \text{isBlocking}(eh) \land \text{labOf}(eh) = \text{labOf}(e_1), e_1 \notin Qof(eh) \)

(A5) \( (\psi', \mathcal{E}'_1) = \text{nextState}(\psi_1, \text{noChange}), \Psi'_1 = \Psi_{11} :: \psi'_1 \)

(A6) \( \Sigma'_1 = \Sigma_1[\Psi_1 \leftarrow \Psi'_1] \)

(A7) \( \mathcal{E}'_1 = \mathcal{E}_1 :: \mathcal{E}'_2 \)

(A8) \( \Sigma_2 = (\Psi_2, \text{Tabs}_2, \text{ExtCoreRs}_2, \ldots) \)

sub-subcase i. \( \text{labOf}(e_1) \subseteq \kappa \)

By Lemma 1

1. \( \text{labOf}(\psi_1) = \text{labOf}(e_1) \subseteq \kappa, \psi_1 \downarrow_\kappa = \psi_1 \)

By \( \Psi_1 \downarrow_\kappa \leq \Psi_2 \downarrow_\kappa \), which forces the projection of the two states to have the same states with regard to \( e_1 \)

2. \( \exists \psi_2 \in \Psi_2 \downarrow_\kappa, \text{s.t. } \psi_1 \downarrow_\kappa \leq \psi_2 \downarrow_\kappa \), that is \( \psi_1 \leq \psi_2, \psi_2 = \psi_1 \).

3. \( \psi_2 \sim_b e_1 \),

4. \( \psi_2 = \Psi_{21} :: \psi_2 :: \Psi_{12} \)
\( \exists \psi \in \Psi_{21}, \text{s.t. } \psi = \text{ProcBlkEvtState}(\ldots, e_2) \text{ or } \text{DoneBlkEvtState}(\ldots, e_2) \)

By Lemma 9

5. \( \Psi_{11} \downarrow_\kappa \leq \Psi_{21} \downarrow_\kappa \)

By \( \text{ExtCoreRs}_1 \downarrow_\kappa \leq \text{ExtCoreRs}_2 \downarrow_\kappa \).

6. \( \text{ExtCoreRs}_1 \downarrow_\kappa \leq \text{ExtCoreRs}_2 \downarrow_\kappa \)
\( \text{ExtCoreRs}_1 \downarrow_\kappa \leq \text{ExtCoreRs}_2 \downarrow_\kappa \)
\( \text{ExtCoreRs}_1 \downarrow_\kappa = \text{ExtCoreRs}_1 :: \text{ExtCoreRs}_1 \downarrow_\kappa \)
\( \text{ExtCoreRs}_2 \downarrow_\kappa = \text{ExtCoreRs}_2 :: \text{ExtCoreRs}_2 \downarrow_\kappa \)
\( \text{ExtCoreRs}_1 \downarrow_\kappa \leq \text{ExtCoreRs}_2 \downarrow_\kappa \)
\( \text{ExtCoreRs}_1 \downarrow_\kappa \leq \text{ExtCoreRs}_2 \downarrow_\kappa \)

By Lemma 9
every core in $\text{ExtCoreRs}_{b1}$ and $\text{ExtCoreRs}_{b2}$ contains a blocking event handler for $e_1$,

no blocking event handlers for $e_1$ in $\text{ExtCoreRs}_{nb1}$ and $\text{ExtCoreRs}_{nb2}$

(7) $\forall \text{ExtCore} \in \text{ExtCoreRs}_{b1} \downarrow \kappa$, $\exists \text{ExtCore}' \in \text{ExtCoreRs}_{b2} \downarrow \kappa$, s.t. $\text{ExtCore} \downarrow \kappa \leq \text{ExtCore}' \downarrow \kappa$

By labOf($e_1$) $\subseteq \kappa$, and $\forall eh \in \text{ExtCore}, \text{labOf}(eh) = \text{labOf}(\text{ExtCore})$

(8) $\forall \text{ExtCore} \in \text{ExtCoreRs}_{b1}$, s.t. $\text{EHs} = \text{getActiveHandlers}(\text{ExtCore}, e_1)$,

$\exists eh \in \text{EHs}$, $\text{isBlocking}(eh) = \text{true}$

and $\text{labOf}(eh) = \text{labOf}(e_1)$

labOf($\text{ExtCore}$) $\subseteq \kappa$, ExtCore $\in \text{ExtCoreRs}_{b1}$

(9) $\text{ExtCoreRs}_{b1} \neq$.

By $\text{ExtCoreRs}_{b1} \leq b_{e_1} \text{ ExtCoreRs}_{b2}$

(10) There are matching pairs of $\text{ExtCore}$ and $\text{ExtCore}'$

s.t. $\text{ExtCore} = (id_{\text{ext}}, (\_ , \_ , \text{EventHandlers}_1 :: \text{eh}_1), \_ )$

$\text{ExtCore}' = (id_{\text{ext}}, (\_ , \_ , \text{EventHandlers}_2 :: \text{eh}_2), \_ )$

$\text{eh}_1 = (\text{eventTypeOf}(e_1), \_ , \text{eventQueue}_1, \_ , \_ , \text{blocking}, \_ )$

$\text{eh}_2 = (\text{eventTypeOf}(e_1), \_ , \text{eventQueue}_2, \_ , \_ , \text{blocking}, \_ )$

if $e_1 \notin \text{eventQueue}_1$, $e_1 \notin \text{eventQueue}_2$

$\text{ExtCore} \leq \text{ExtCore}'$

By (A4), (8), (9), (10), $e_1 = e_2$

(11) $\forall \text{ExtCore}' \in \text{ExtCoreRs}_{b2}$, $\text{EHs} = \text{getActiveHandlers}(\text{ExtCore}', e_2)$,

$\forall eh \in \text{EHs}$, $\text{isBlocking}(eh) = \text{true} \land \text{labOf}(eh) = \text{labOf}(e_2)$, $e_2 \notin Qof(\text{eh})$

By (4) (A2) and (11), we can apply BLOCKEDFINISHED$1$ to $\Sigma_2$

(12) $\Sigma_2; \Sigma_2 \rightarrow \Sigma_2; \Sigma_2 :: \Sigma_2'$

(13) $(\psi'_1, \Sigma''_1) = \text{nextState}(\psi_2, \text{noChange})$, $\Psi'_2 = \Psi_{21} :: \psi'_2$

(14) $\psi'_2 = \psi'_1$, $\Sigma''_1 = \Sigma''_2$, $\text{labOf}(\psi'_2) = \text{labOf}(\psi'_1) = \text{labOf}(\Sigma''_1) = \text{labOf}(\Sigma''_2) = \text{labOf}(e_1)$

note that we write labOf($\Sigma$) to denote the uniform label of all events in $\Sigma$

(15) $\Sigma'_2 = \Sigma_2[\Psi_2 \leftarrow \psi'_2]$

By (5), (13), (14), Lemma 10

(16) $\Psi'_1 \downarrow \kappa \leq_c \Psi'_2 \downarrow \kappa$

By assumption, (14), (15), (16) and STATE

(17) $\Sigma'_1 \downarrow \kappa \leq \Sigma'_2 \downarrow \kappa$

By (A7), $\Sigma'_1 \downarrow \kappa \leq \Sigma'_2 \downarrow \kappa$

(18) $\Sigma''_2 = \Sigma''_1 \Sigma''_2 = \Sigma''_2 :: \Sigma''_1 \downarrow \kappa \leq \Sigma''_2 \downarrow \kappa$

sub-case ii. labOf($e_1$) $\not\in \kappa$

By Lemma 1, (13)

(1) labOf($\psi_1$) = labOf($\psi'_1$) = labOf($e_1$)

(2) $\forall \psi \in \Psi_{12}$, labOf($\psi$) = labOf($e_1$)

(3) labOf($\psi'_1$) = labOf($e_1$)

(4) $\psi_1 \downarrow \kappa = \cdot$, $\Sigma''_1 \downarrow \kappa = \cdot$, $\psi'_1 \downarrow \kappa = \cdot$, $\Psi_{12} \downarrow \kappa = \cdot$

(5) $\Psi'_1 \downarrow = \Psi_1 \downarrow$

(6) $\Sigma'_1 \downarrow \kappa = \Sigma_1 \downarrow \kappa \leq \Sigma_2 \downarrow \kappa$

(7) $\Sigma'_1 \downarrow \kappa = \Sigma_1 \downarrow \kappa \leq \Sigma_2 \downarrow \kappa$

case: BLOCKEDFINISHED$2$
By assumptions and Lemma 1

(A1) \( \Sigma_1 = (\Psi_1, Tabs_1, ExtCoreRs_1, \cdots), \Psi_1 = \Psi_{11} :: \psi_1 :: \Psi_{12} \)

(A2) \( \psi_1 \sim_b e_1, e_1 \) is a blocking event, \( labOf(\psi_1) = labOf(e_1) \)
\( \exists \psi \in \Psi_{11}, \text{s.t. } \psi = ProcBlkEvtState(\cdot, \cdot, e_1) \text{ or } DoneBlkEvtState(\cdot, \cdot, e_1, \cdot) \)
\( \forall \psi \in \Psi_{12}, labOf(e_1) \neq 0 \)
\( (\psi', E_1) = nextState(\psi, Blocked(c_j)) \)

By Lemma 1

(1) \( labOf(\psi_1) = labOf(e_1) \subseteq \kappa \)
\( \forall \psi \in \Psi_{12}, labOf(e_1) \subseteq \kappa \)
\( \psi_1 \downarrow_{\kappa} = \psi_1, \Psi_{12} \downarrow_{\kappa} = \Psi_{12} \)

By Lemma 9

(5) \( \Psi_{11} \downarrow_{\kappa} \leq_c \Psi_{21} \downarrow_{\kappa} \)

By Lemma 1

(2) \( \exists \psi_2 \in \Psi_{2} \downarrow_{\kappa}, \text{ s.t. } \psi_1 \downarrow_{\kappa} \leq c \psi_2 \downarrow_{\kappa}, \text{ that is } \psi_1 \leq \psi_2, \psi_2 = \psi_1 \).

(3) \( \psi_2 \sim_b e_2, e_1 = e_2, e_2 \) is a blocking event

(4) \( \Psi_2 = \Psi_{21} :: \psi_2 :: \Psi_{12} \)
\( \exists \psi \in \Psi_{21}, \text{s.t. } \psi = ProcBlkEvtState(\cdot, \cdot, e_2) \text{ or } DoneBlkEvtState(\cdot, \cdot, e_2, \cdot) \)

By Lemma 9

(5) \( \Psi_{11} \downarrow_{\kappa} \leq_c ExtCoreRs_1 \downarrow_{\kappa} \)

By Lemma 1

(6) \( \Psi_{22} = \Psi_{12}, getLastInstalledReturn(\Psi_{22}) = (id_{j_2}, c_{j_2}) \text{ s.t. } c_{j_2} \neq 0 \)
\( c_{j_2} = c_{j_1} \)

By Lemma 9

(7) \( ExtCoreRs_1 \downarrow_{\kappa} \leq_c ExtCoreRs_2 \downarrow_{\kappa} \)
\( ExtCoreRs_1 \downarrow_{\kappa} = ExtCoreRs_{sb1} :: ExtCoreRs_{sb2} \downarrow_{\kappa} \)
\( ExtCoreRs_2 \downarrow_{\kappa} = ExtCoreRs_{sb1} :: ExtCoreRs_{sb2} :: ExtCoreRs_{sb3} \downarrow_{\kappa} \)
\( ExtCoreRs_{sb1} \leq_{\kappa} c_{j_1}, ExtCoreRs_{sb2} \)

every core in \( ExtCoreRs_{sb1} \) and \( ExtCoreRs_{sb2} \) contains a blocking event handler for \( e_1 \), no blocking event handlers for \( e_1 \) in \( ExtCoreRs_{sb1} \) and \( ExtCoreRs_{sb2} \)
(8) \( \forall \text{ExtCore} R \in \text{ExtCoreRs}_1 \downarrow \kappa, \exists \text{ExtCore} R' \in \text{ExtCoreRs}_2 \downarrow \kappa, \) s.t. \( \text{ExtCore} R \downarrow \kappa \leq \text{ExtCore} R' \downarrow \kappa \)

By \( \text{labOf}(e_1) \leq \kappa, \) and \( \forall \text{eh} \in \text{ExtCore} R, \text{labOf}(\text{eh}) = \text{labOf}(\text{ExtCore} R) \)

(9) \( \forall \text{ExtCore} \in \text{ExtCoreRs}_1, \) s.t. \( \text{EHs} = \text{getActiveHandlers}(\text{ExtCore} R, e_1) \),

\[ \exists \text{eh} \in \text{EHs}, \text{isBlocking}(\text{eh}) = \text{true} \]

\[ \land \text{labOf}(\text{eh})^- = \text{labOf}(e_1) \]

\[ \text{labOf}(\text{extCore} R) \leq \kappa, \text{ExtCore} R \in \text{ExtCoreRs}_{b_1} \]

(10) \( \text{ExtCoreRs}_{b_1} \neq \cdot \)

By \( \text{ExtCoreRs}_{b_1} \leq_{b_c} \text{ExtCoreRs}_{b_2} \)

(11) There are matching pairs of \( \text{ExtCore} R \) and \( \text{ExtCore} R' \),

s.t. \( \text{ExtCore} R = (\text{id}_{\text{ext}}, (\cdot, \cdot, \cdot), \text{EventHandlers}_1 :: \text{eh}_1), (\cdot) \)

\( \text{ExtCore} R' = (\text{id}_{\text{ext}}, (\cdot, \cdot, \cdot), \text{EventHandlers}_2 :: \text{eh}_2), (\cdot) \)

\( \text{eh}_1 = (\text{eventTypeOf}(e_1), (\cdot, \cdot, \cdot), \text{eventQueue}_1, \cdot), \cdot, \cdot, \text{blocking}, \cdot) \)

\( \text{eh}_2 = (\text{eventTypeOf}(e_1), (\cdot, \cdot, \cdot), \text{eventQueue}_2, \cdot), \cdot, \cdot, \text{blocking}, \cdot) \)

if \( e_1 \notin \text{eventQueue}_1, e_1 \notin \text{eventQueue}_2 \)

\( \text{ExtCore} R \leq \text{ExtCore} R' \)

By (A4), (9), (10), (11), \( e_1 = e_2 \)

(12) \( \forall \text{ExtCore}' \in \text{ExtCoreRs}_2, \text{EHs} = \text{getActiveHandlers}(\text{ExtCore}', e_2), \)

\( \forall \text{eh} \in \text{EHs}, \text{isBlocking}(\text{eh}) = \text{true} \land \text{labOf}(\text{eh})^- = \text{labOf}(e_2), e_2 \notin \text{Qof}(\text{eh}) \)

By (A2), (4), (12), apply \text{BLOCKEDFINISHED}2 to \( \Sigma_2 \)

(13) \( (\psi'_2, E''_2) = \text{nextState}(\psi_2, \text{Blocked}(e_{j2})) \)

(14) \( \psi'_2 = \psi'_1, E''_2 = E'_1 \)

(15) \( \Psi'_2 = \Psi'_2 :: \psi'_2 \)

(16) \( \Sigma'_2 = \Sigma'_2[\Psi'_2 <e \Psi'_2] \)

(17) \( \Sigma'_2; E'_2 \xrightarrow{\cdot} \Sigma'_2; E'_2 \)

(18) \( E'_2 = E'_2 :: E''_2 \)

By (5), (14), Lemma 10

(19) \( \Psi'_1 \downarrow \kappa \leq \psi'_2 \downarrow \kappa \)

By assumption, (A9), (16), (19) and \text{STATE}

(20) \( \Sigma'_1 \downarrow \kappa \leq \Sigma'_2 \downarrow \kappa \)

By \( \mathcal{E}_1 \leq \mathcal{E}_2, \) (A10), (18), (22)

(21) \( \mathcal{E}'_1 \downarrow \kappa \leq \mathcal{E}'_2 \downarrow \kappa \)

\text{sub-subcase ii.} \text{ labOf}(e_1) \nsubseteq \kappa \)

By Lemma 1, 13

(1) \( \text{labOf}(\psi_1) = \text{labOf}(\psi'_1) = \text{labOf}(e_1) \)

(2) \( \forall \psi \in \Psi_{12}, \text{labOf}(\psi) = \text{labOf}(e_1) \)

(3) \( \text{labOf}(e'_1) = \text{labOf}(e_1) \)

(4) \( \psi_1 \downarrow \kappa = \cdot, \mathcal{E}'_1 \downarrow \kappa = \cdot, \psi'_1 \downarrow \kappa = \cdot, \Psi_{12} \downarrow \kappa = \cdot \)

(5) \( \Psi'_1 \downarrow \kappa = \Psi_1 \downarrow \kappa \)

(6) \( \Sigma'_1 \downarrow \kappa = \Sigma_1 \downarrow \kappa \leq \Sigma_2 \downarrow \kappa \)

(7) \( \mathcal{E}'_1 \downarrow \kappa = \mathcal{E}_1 \downarrow \kappa \leq \mathcal{E}_2 \downarrow \kappa \)

\text{case: EVENTDEQUEUECS1}
Let $\Sigma_1 = (\Psi, \text{Tabs}_1, \text{ExtCoreRs}_1, \text{progInjCS}_1, \text{Exts}_1, \text{Cookies}_1, \text{MBookmarks}_1, \text{histories}_1, \text{UI}_1)$

$\Sigma_2 = (\Psi, \text{Tabs}_2, \text{ExtCoreRs}_2, \text{progInjCS}_2, \text{Exts}_2, \text{Cookies}_2, \text{MBookmarks}_2, \text{histories}_2, \text{UI}_2)$

By assumptions

(1) $\Sigma_1 = \Sigma_{ctx}[\Gamma, \text{skip} \mid \cdot]$  
(2) $\text{Tabs}_1 = \text{Tabs}_1'[\cdot]$  
(3) $\text{Tab}_1 = \text{Tab}_{ctx}[\Gamma, \text{skip} \mid \cdot] = (\text{TabID}_1, \text{Docs} : \text{Doc}_{ctx}[\Gamma, \text{skip} \mid \cdot, \text{url}_1, \text{EventHandler}_1, \ell_1)$  
(4) $\text{Doc}_{ctx}[\Gamma, \text{skip} \mid \cdot] = (\text{id}, \text{url}, \text{nodes}, \text{DocCS} : \text{Doc}_{ctx}[\Gamma, \text{skip} \mid \cdot, \ell_1)$  
(5) $\text{DocCS}_{ctx}(\Gamma, \text{skip} \mid \cdot) = (\text{id}_\text{ext}, \text{id}, \Gamma, \text{cmd}, \text{EventHandler} : \text{eh}_{ctx}[\text{skip}], \ell)$  
(6) $\text{eh}_{ctx} = (\cdot, \text{eventType}, \text{cmd}, \text{e}_1 : \text{E}_1'[\cdot, \ell], \text{id}, \text{BlockingFlag}, \text{return})$  
(7) $\text{eh}_{ctx} = (\cdot, \text{eventType}, \text{cmd}, \text{e}_1 : \text{E}_1'[\cdot, \ell], \text{id}, \text{BlockingFlag}, \text{return})$  
(8) $\text{Doc}_{ctx}(\Gamma, \text{skip} \mid \cdot) = \text{Doc}_{ctx}(\Gamma, \text{skip} \mid \cdot, \ell)$  
(9) $\text{Doc}_{ctx}(\Gamma, \text{skip} \mid \cdot) = \text{Doc}_{ctx}(\Gamma, \text{skip} \mid \cdot, \ell)$  
(10) $\text{Doc}_{ctx}(\Gamma, \text{skip} \mid \cdot) = \text{Doc}_{ctx}(\Gamma, \text{skip} \mid \cdot, \ell)$  
(11) $\text{Doc}_{ctx}(\Gamma, \text{skip} \mid \cdot) = \text{Doc}_{ctx}(\Gamma, \text{skip} \mid \cdot, \ell)$  
(12) $\Sigma_1' = \Sigma_{ctx}[\Gamma, \text{skip} \mid \cdot]$  
(13) $\text{labOf}(\ell_1) \not\subseteq \kappa$  
(14) $\text{labOf}(\ell_1) \not\subseteq \kappa$

Sub-case i. $\ell' \subseteq \kappa$ and $\text{labOf}(\ell_1) \not\subseteq \kappa$

By DS1, EH, EVENT1

(1) $\text{Doc}_{ctx}(\Gamma, \text{skip} \mid \cdot) = (\text{id}_\text{ext}, \text{id}, \Gamma, \text{cmd}, \text{EventHandler} \downarrow \downarrow, :: \text{eh}_{ctx}[\text{skip}] \downarrow \downarrow, \ell)$

By definition

(3) $\text{Doc}_{ctx}(\Gamma, \text{skip} \mid \cdot) \downarrow \downarrow \in \text{Tab}_1 \downarrow \downarrow$

By $\Sigma_1 \downarrow \downarrow \subseteq \Sigma_2 \downarrow \downarrow$

(4) $\text{Tabs}_2 = \text{Tabs}_2''$ and $\text{Tabs}_2'' \downarrow \downarrow \subseteq \text{Tabs}_2'' \downarrow \downarrow$ and $\text{Tab}_1 \downarrow \downarrow \subseteq \text{Tab}_2 \downarrow \downarrow$

By definitions and (4)

(5) exists $\text{Doc}_{CS2} = \text{Doc}_{CS2}' : \text{Doc}_{CS2}, \text{Doc}_{CS2} \in \text{Doc}_2, \text{Doc}_2 \in \text{Doc}_{CS2}, \text{Doc}_{CS2} \in \text{Tab}_2$

s.t. $\text{Doc}_{CS2}[\Gamma, \text{skip} \mid \cdot] \downarrow \downarrow \subseteq \text{Doc}_{CS2} \downarrow \downarrow$

(6) $\text{Doc}_{CS2}[\Gamma, \text{skip} \mid \cdot] = (\text{id}_\text{ext}, \text{id}, \Gamma, \text{cmd}, \text{EventHandler}_2 \downarrow \downarrow, :: \text{eh}_2 \downarrow \downarrow, \ell)$

where $\text{EventHandler} \downarrow \downarrow \subseteq \text{EventHandler}_2 \downarrow \downarrow, \text{eh}_{ctx}[\text{skip}] \downarrow \downarrow \subseteq \text{eh}_2 \downarrow \downarrow$

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By (6)

(7) \( e_{h_2} = (\cdot, \text{eventType}, x, \text{cmd}, e_2 :: E''^\nu, \text{skip}, \|e\|_e, \text{BlockingFlag}, \text{return}) \)
where \( e_1 \leq e_2 \), namely \( e_1 = e_2 \) and \( \Delta''_{\kappa} \leq \Delta''_{\kappa} \).

(8) \( e_{h_2} = e_{h_2 \text{ctx}_2} \| \text{skip} \| \)

(9) \( \text{DocCS}_{h_2} = \text{DocCS}_{h_2 \text{ctx}_2} \| \Gamma, \text{skip} \| \text{id} \)
\( \text{DocCS}_{h_2^s} = \text{DocCS}_{h_2^s \text{ctx}_2} \| \Gamma, \text{skip} \| \text{id} \)
\( \text{Tab}_2 = \text{Tab}_{2 \text{ctx}_2} \| \Gamma, \text{skip} \| \text{id} \)
\( \text{Tab}_{2^s} = \text{Tab}_{2^s \text{ctx}_2} \| \Gamma, \text{skip} \| \text{id} \)
\( \Sigma_2 = \Sigma_{2 \text{ctx}_2} \| \Gamma, \text{skip} \| \text{id} \)

Apply \text{EVENTDEQUEUECS1} to \( \Sigma_2 \)

(11) \( e_{h_2 \text{ctx}_2} = (\cdot, \text{eventType}, x, \text{cmd}, E''^\nu, \text{skip}, \|e\|_e, \text{BlockingFlag}, \text{return}) \)

(12) \( e_{h_1 \text{ctx}_1} \text{skip} \| \leq \Delta''_{\text{ctx}_2} \| \text{skip} \| \downarrow_{\kappa} \)

(13) \( \text{DocCS}_{\text{ctx}_2}(id) = \text{DocCS}_{\text{ctx}_2}(id)[e_{h_2 \text{ctx}_2} \leftarrow e_{h_2 \text{ctx}_2} \]

(14) \( \text{Doc}_{\text{ctx}_2}(id) = \text{Doc}_{\text{ctx}_2}(id)[\text{DocCS}_{\text{ctx}_2}(id) \leftarrow \text{DocCS}'_{\text{ctx}_2}(id)] \)

(15) \( \text{Tab}_{\text{ctx}_2}(id) = \text{Tab}_{\text{ctx}_2}(id)[\text{Doc}_{\text{ctx}_2}(id) \leftarrow \text{Doc}_{\text{ctx}_2}(id)] \)

(16) \( \text{Tab}_{\text{ctx}_2}(id) = \text{Tab}_{\text{ctx}_2}(id)[\text{Tab}_{\text{ctx}_2}(id) \leftarrow \text{Tab}_{\text{ctx}_2}(id)] \)

(17) \( \Sigma''_{\text{ctx}_2}(id) = \Sigma_{\text{ctx}_2}(id)[\text{Tab}_{\text{ctx}_2}(id) \leftarrow \text{Tab}_{\text{ctx}_2}(id)] \)

(18) \( \Sigma_{\text{ctx}_2} \| \Gamma, \text{skip} \| \text{id} ; E_2 \xrightarrow{r} \Sigma''_{\text{ctx}_2} \| \Gamma, \text{skip} \| \text{id} ; E_2' = E_2 \)

By (4), (5), (12), (13), (14), (15), (16), and Lemma 6

(19) \( \text{DocCS}'_{\text{ctx}_2}(id) \downarrow_{\kappa} \leq \text{DocCS}'_{\text{ctx}_2}(id) \downarrow_{\kappa} \)

(20) \( \text{DocCS}_{\text{ctx}_2}(id) \downarrow_{\kappa} \leq \text{DocCS}_{\text{ctx}_2}(id) \downarrow_{\kappa} \)

(21) \( \text{Doc}_{\text{ctx}_2}(id) \downarrow_{\kappa} \leq \text{Doc}_{\text{ctx}_2}(id) \downarrow_{\kappa} \)

(22) \( \text{Tab}_{\text{ctx}_2}(id) \downarrow_{\kappa} \leq \text{Tab}_{\text{ctx}_2}(id) \downarrow_{\kappa} \)

(23) \( \text{Tab}_{\text{ctx}_2}(id) \downarrow_{\kappa} \leq \text{Tab}_{\text{ctx}_2}(id) \downarrow_{\kappa} \)

By assumption, \( \Sigma_1 \downarrow_{\kappa} \leq \Sigma_2 \downarrow_{\kappa} \)
\( \Sigma_1 = \Sigma_{\text{ctx}_2} \| \Gamma, \text{skip} \| \text{id} ; \Sigma_2 = \Sigma_{\text{ctx}_2} \| \Gamma, \text{skip} \| \text{id} ; (15), (21), \text{STATE} \)

(24) \( \Sigma''_{\text{ctx}_2} \| \Gamma, \text{skip} \| \text{id} \downarrow_{\kappa} \leq \Sigma''_{\text{ctx}_2} \| \Gamma, \text{skip} \| \text{id} \downarrow_{\kappa} \)

By assumption and (16)

(25) \( E_2' \downarrow_{\kappa} = E_1 \downarrow_{\kappa} \leq E_2 \downarrow_{\kappa} \)

\text{sub-subcase ii.} \( \ell \subseteq \kappa \) and \( \text{labOf}(e_1) \not\subseteq \kappa \)

By DS1, EH, EVENT2

(1) \( \text{DocCS}_{\text{ctx}}(\Gamma, \text{skip} \| \downarrow_{\kappa} = (\text{id}_{\text{ctx}} \| \text{id}_{\ell}, \| \Gamma \|, \text{cmd}, \text{EventHandlers} \| :: e_{\text{ctx}} \| \text{skip} \| \downarrow_{\kappa} \}) \)

(2) \( e_{\text{ctx}} \| \text{skip} \| \downarrow_{\kappa} = (\cdot, \text{eventType}, x, \text{cmd}, E''^\nu, \text{skip}, \|e\|_e, \text{BlockingFlag}, \text{return}) \)

(3) \( e_{\text{ctx}} \| \text{skip} \| \downarrow_{\kappa} = (\cdot, \text{eventType}, x, \text{cmd}, E''^\nu, \text{skip}, \|e\|_e, \text{BlockingFlag}, \text{return}) \)

(4) \( e_{\text{ctx}} \| \text{skip} \| \downarrow_{\kappa} = e_{\text{ctx}} \| \text{skip} \| \downarrow_{\kappa} \)

By (4), (A8), (A9), (A10), (A11), (A12), Lemma 6 and \text{STATE}

(5) \( \text{DocCS}'_{\text{ctx}}(id) \downarrow_{\kappa} \leq \text{DocCS}_{\text{ctx}}(id) \downarrow_{\kappa} \)

(6) \( \text{DocCS}'_{\text{ctx}}(id) \downarrow_{\kappa} \leq \text{DocCS}_{\text{ctx}}(id) \downarrow_{\kappa} \)

(7) \( \text{Doc}_{\text{ctx}}(id) \downarrow_{\kappa} \leq \text{Doc}_{\text{ctx}}(id) \downarrow_{\kappa} \)

(8) \( \text{Tab}_{\text{ctx}}(id) \downarrow_{\kappa} \leq \text{Tab}_{\text{ctx}}(id) \downarrow_{\kappa} \)

(9) \( \text{Tab}_{\text{ctx}}(id) \downarrow_{\kappa} \leq \text{Tab}_{\text{ctx}}(id) \downarrow_{\kappa} \)

(10) \( \Sigma''_{\text{ctx}} \downarrow_{\kappa} \leq \Sigma''_{\text{ctx}} \downarrow_{\kappa} \)

By (10), \( \Sigma_1 \downarrow_{\kappa} \leq \Sigma_2 \downarrow_{\kappa} \)

(11) \( \Sigma''_{\text{ctx}} \downarrow_{\kappa} \leq \Sigma''_{\text{ctx}} \downarrow_{\kappa} \leq \Sigma_2 \downarrow_{\kappa} \)

By (A14), \( \Sigma_1 \downarrow_{\kappa} \leq \Sigma_2 \downarrow_{\kappa} \)

(12) \( \Sigma''_{\text{ctx}} \downarrow_{\kappa} \leq \Sigma''_{\text{ctx}} \downarrow_{\kappa} \leq \Sigma_2 \downarrow_{\kappa} \)

\text{sub-subcase iii.} \( \ell \not\subseteq \kappa \)

By DS2

(1) \( \text{DocCS}_{\text{ctx}}(\Gamma, \text{skip} \| \not\in \Sigma_1 \downarrow_{\kappa} \)

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By $\Sigma_1 \downarrow_{=\kappa} \Sigma_2 \downarrow_{\kappa}$, $\Sigma'_1 = \Sigma_{ctx} \downarrow_{\kappa}$, and EVENTDEQUEUECS1 does not change $\Sigma_{ctx} \downarrow_{\kappa}$, except $DocCS_{ctx}(\Gamma, skip) \downarrow_{id}$, $DocCS'_{ctx}(\Gamma, skip) \downarrow_{id} \notin \Sigma'_1 \downarrow_{\kappa}$

(2) $\Sigma_{ctx} \downarrow_{\kappa}$, $skip \downarrow_{id} \downarrow_{\kappa} = \Sigma_{ctx} \downarrow_{\kappa}$, $skip \downarrow_{id} \downarrow_{\kappa} \leq \Sigma_2 \downarrow_{\kappa}$

By assumption

(3) $\mathcal{E}_1' = \mathcal{E}_1 \downarrow_{\kappa} \leq \mathcal{E}_2 \downarrow_{\kappa}$

**case: EVENTDEQUEUECS2**

$$
\begin{align*}
\Sigma_{ctx}(id) &= (\Psi, Tabs_{ctx}(id), \ldots) \quad t_{ctx}(id) \in Tabs_{ctx}(id) \\
t_{ctx}(id) &= (\ldots, Doc_{ctx}(id), \ldots) \quad Doc_{ctx}(id) \in Doc_{ctx}(id) \\
Doc_{ctx}(id) &= (\ldots, Doc_{CS}(id), \ldots) \quad Doc_{CS}(id) \in Doc_{CS}(id) \\
Doc_{CS}(id) &= (\ldots, \text{EventType}, x, cmd, e :: \mathcal{E}_1, \|, id, BlockingFlag, return') \\
e &= (\|, \text{EventType}, return, \ldots, \kappa_e) \\
\ell' &= \kappa_e \triangleright \triangleright_{\text{int}} \ell \\
\ell'^{'} &= (\ldots, \text{EventType}, x, cmd, \mathcal{E}_1, \|, id, BlockingFlag, return')
\end{align*}
$$

Let $\Sigma_1 = (\Psi, Tabs_1, ExtCoreR1, proginjCS_1, Exts_1, Cookies_1, MBookmarkss_1, histories_1, U_1)$ and $\Sigma_2 = (\Psi, Tabs_2, ExtCoreR2, proginjCS_2, Exts_2, Cookies_2, MBookmarkss_2, histories_2, U_2)$

By assumptions

(A1) $\Sigma_1 = \Sigma_{ctx} \downarrow_{\kappa}$, $skip \downarrow_{id}$, $Tabs_1 = Tabs''_1 :: Tab_1$

(A2) $Tab_1 = Tab_{ctx} \downarrow_{\kappa}$, $skip \downarrow_{id} = (\text{TabID}_1, Docs :: Doc_{ctx}, \Gamma, skip \downarrow_{id}, \|, \text{EventType}, \text{cmd}, EventHandlers :: eh_{ctx}, \ell)$

(A3) $Doc_{ctx}(\Gamma, skip \downarrow_{id} = (\|, \|, \text{EventType}, \text{cmd}, Doc_{CS} :: Doc_{CS}(\Gamma, skip \downarrow_{id}, \|)$

(A4) $\mathcal{E}_1 = (\|, \|, \|, \text{eventType}, \text{cmd}, \text{return}', \ldots, \kappa_e)$

(A5) $eh_{ctx}[skip] = (\ldots, \text{eventType}, \text{cmd}, \mathcal{E}_1, \|, \|, \text{BlockingFlag}, return')$

(A7) $\kappa_e \triangleright \triangleright_{\text{int}} \ell, \ell' = \kappa_e \triangleright \triangleright_{\text{int}} \ell$

(A8) $eh_{ctx}[\text{cmd}] = (\ldots, \text{eventType}, \text{cmd}, \mathcal{E}_1, \|, \|, \text{BlockingFlag}, return')$

(A9) $Doc_{CS}(id) = Doc_{CS}(id)[eh_{ctx} \\Rightarrow eh_{ctx}[\ell \\leftarrow \ell']$

(A10) $Doc_{CS}'(id) = Doc_{CS}'(id)[Doc_{CS}(id) \\Leftarrow Doc_{CS}(id)]$

(A11) $Table_{ctx}(id) = Table_{ctx}(id)[Doc_{ctx}(id) \\Leftarrow Doc_{ctx}(id)]$

(A12) $Table_{ctx}'(id) = Table_{ctx}'(id)[Table_{ctx}(id) \\Leftarrow Table_{ctx}(id)]$

(A13) $\Sigma_1' = \Sigma_{ctx} \downarrow_{\kappa}$, $\Sigma_{ctx} \downarrow_{\kappa}$, $\Sigma_{ctx} \downarrow_{\kappa}$, $\Sigma_{ctx} \downarrow_{\kappa}$, $\Sigma_{ctx} \downarrow_{\kappa}$, $\Sigma_{ctx} \downarrow_{\kappa}$, $\Sigma_{ctx} \downarrow_{\kappa}$

(A14) $\mathcal{E}_1' = \mathcal{E}_1$

**sub-case i.** $\ell'^{'} \subseteq \kappa, \kappa_e \subseteq \kappa, updLab(e, \ell'^{'}), \downarrow_{\kappa} = updLab(e, \ell'^{'})$

By DS1.

(1) $Doc_{CS}_{ctx}(\Gamma, skip \downarrow_{id} = (\|, \|, \text{EventType}, \text{cmd}, EventHandlers \downarrow_{\kappa} :: eh_{ctx}[\text{cmd}] \downarrow_{\kappa}, \ell)$

By definition

(2) $Doc_{CS}(\Gamma, skip \downarrow_{id} \in Tab \downarrow_{\kappa}$

By $\Sigma_1 \downarrow_{\kappa} \subseteq \Sigma_2 \downarrow_{\kappa}$

(3) $Tabs_1 = Tabs''_1 :: Tab_2$ and $Tabs'' \downarrow_{\kappa} \subseteq Tabs'' \downarrow_{\kappa}$ and $Tabs_1 \downarrow_{\kappa} \subseteq Tabs_2 \downarrow_{\kappa}$

By definitions and (3)

(4) $exists Doc_{CS} \in Doc_{CS}s, Doc_{CS} \in Doc_{CS}, Doc_{CS} \in Doc_{CS}s, Doc_{CS} \in Doc_{CS}$
s.t. \( \text{DocCS}_{\text{ctx}} \Gamma \| \text{skip} \| \text{id} \downarrow \kappa \leq \text{DocCS}_2 \downarrow \kappa \)

\( \text{DocCS}_{\text{ctx}} \Gamma \| \text{skip} \| \text{id} \downarrow \kappa \leq \text{DocCS}_2 \downarrow \kappa \)

\( \text{DocCS}_{\text{ctx}} \Gamma \| \text{skip} \| \text{id} \downarrow \kappa \leq \text{Doc}_2 \downarrow \kappa \)

\( \text{DocCS}_{\text{ctx}} \Gamma \| \text{skip} \| \text{id} \downarrow \kappa \leq \text{DocCS}_2 \downarrow \kappa \)

By (4), DocCS

\( \text{DocCS}_2 = (\text{id}_{\text{ext}}, \text{id}, \text{id}_t, [\Gamma], \text{cmd}, \text{EventHandlers}_2 :: \text{eh}_2, \ell) \)

where \( \text{EventHandlers}_2 \downarrow \kappa \leq \text{EventHandlers}_2 \downarrow \kappa \), \( \text{eh} \downarrow \kappa \leq \text{eh}_2 \downarrow \kappa \)

By (5)

\( \text{eh}_2 = (\text{\textit{eventType}}, \text{x}, \text{cmd}, \text{e}_2 :: \text{\textit{skips}}, \text{id}_e, \text{BlockingFlag}, \text{return}) \)

where \( e_1 \leq e_2 \), namely \( e_1 = e_2 \) and \( \text{DocCS}_s \downarrow \kappa \leq \text{\textit{skips}}_2 \downarrow \kappa \).

\( \text{DocCS}_2 = \text{DocCS}_{\text{ctx}_2} \Gamma \| \text{skip} \| \text{id} \)

\( \text{DocCS}_{\text{ctx}_2} (\text{id}) \downarrow \kappa \leq \text{eh}_{\text{ctx}_2} (\ell) \downarrow \kappa \)

\( \text{Doc} \Gamma \| \text{skip} \| \text{id} \downarrow \kappa \leq \text{Doc} \downarrow \kappa \)

\( \text{Doc} \Gamma \| \text{skip} \| \text{id} \downarrow \kappa \leq \text{Doc} \downarrow \kappa \)

Apply EVENTDEQUEUECS to \( \Sigma_2 \)

\( \text{eh}_{\text{ctx}_2} (\text{id}) = (\text{\textit{eventType}}, \text{x}, \text{cmd}, \text{e}_2 :: \text{\textit{skips}}, \text{id}_e, \text{BlockingFlag}, \text{return}) \)

\( \text{eh}_{\text{ctx}_2} (\text{id}) = (\text{\textit{eventType}}, \text{x}, \text{cmd}, \text{e}_2 :: \text{\textit{skips}}, \text{id}_e, \text{BlockingFlag}, \text{return}) \)

\( \text{eh}_{\text{ctx}_2} (\text{id}) = (\text{\textit{eventType}}, \text{x}, \text{cmd}, \text{e}_2 :: \text{\textit{skips}}, \text{id}_e, \text{BlockingFlag}, \text{return}) \)

\( \text{eh}_{\text{ctx}_2} (\text{id}) = (\text{\textit{eventType}}, \text{x}, \text{cmd}, \text{e}_2 :: \text{\textit{skips}}, \text{id}_e, \text{BlockingFlag}, \text{return}) \)

\( \text{eh}_{\text{ctx}_2} (\text{id}) = (\text{\textit{eventType}}, \text{x}, \text{cmd}, \text{e}_2 :: \text{\textit{skips}}, \text{id}_e, \text{BlockingFlag}, \text{return}) \)

\( \Sigma_2 \downarrow \kappa \leq \text{eh}_{\text{ctx}_2} (\ell) \downarrow \kappa \)

By assumption and (6)

\( \text{\textit{labOf}} (\text{e}_2) = \text{\textit{labOf}} (\text{e}_1), \text{\textit{labOf}} (\text{e}_2) \subseteq \kappa \) and \( \text{\textit{labOf}} (\text{e}_2) \subseteq \ell^* \)

\( \text{DocCS}_{\text{ctx}} (\text{id}) \downarrow \kappa \leq \text{DocCS}_{\text{ctx}_2} (\text{id}) \downarrow \kappa \)

By (4), (11), (12), (13), (14), (15) and Lemma 6

\( \text{DocCS}_{\text{ctx}} (\text{id}) \downarrow \kappa \leq \text{DocCS}_{\text{ctx}_2} (\text{id}) \downarrow \kappa \)

\( \text{DocCS}_{\text{ctx}} (\text{id}) \downarrow \kappa \leq \text{DocCS}_{\text{ctx}_2} (\text{id}) \downarrow \kappa \)

\( \Sigma_2 \downarrow \kappa \leq \text{eh}_{\text{ctx}_2} (\ell) \downarrow \kappa \)

By assumption, \( \Sigma_2 \downarrow \kappa \leq \text{eh}_{\text{ctx}_2} (\ell) \downarrow \kappa \)

\( \Sigma_2 \downarrow \kappa \leq \text{eh}_{\text{ctx}_2} (\ell) \downarrow \kappa \)

\( \Sigma_2 \downarrow \kappa \leq \text{eh}_{\text{ctx}_2} (\ell) \downarrow \kappa \)

By assumption and (17)

\( \Sigma_2 \downarrow \kappa \leq \text{eh}_{\text{ctx}_2} (\ell) \downarrow \kappa \)

\( \Sigma_2 \downarrow \kappa \leq \text{eh}_{\text{ctx}_2} (\ell) \downarrow \kappa \)

By DS1

\( \text{DocCS}_{\text{ctx}} (\text{id}) \downarrow \kappa \leq (\text{id}_{\text{ext}}, \text{id}, \text{id}_t, [\Gamma], \text{cmd}, \text{EventHandlers}_2 :: \text{eh}_{\text{ctx}} \| \text{skip} \| \text{id} \downarrow \kappa \)

By (A7)

\( \ell^* \downarrow \kappa \leq \text{updLab}(\ell^* \downarrow \kappa) \downarrow \kappa \)

By DS2

\( \text{DocCS}_{\text{ctx}} (\text{id}) \downarrow \kappa \leq \text{DocCS}_{\text{ctx}} (\text{id}) \downarrow \kappa \)

By (A10), (A11), (A12), (A13) Lemma 6 and STATE

\( (\text{DocCS} :: \text{DocCS}_{\text{ctx}} (\text{id}) \downarrow \kappa \leq (\text{DocCS} :: \text{DocCS}_{\text{ctx}} (\text{id}) \downarrow \kappa \)

\( \text{DocCS}_{\text{ctx}} (\text{id}) \downarrow \kappa \leq \text{DocCS}_{\text{ctx}} (\text{id}) \downarrow \kappa \)
By (A8), (A9), (A10)

(6) \( \text{Tab}'_{\text{CTX}}(id) \downarrow_{\kappa} \leq \text{Tab}_{\text{CTX}}(id) \downarrow_{\kappa} \)
(7) \( \text{Tabs}_{\text{CTX}}(id) \downarrow_{\kappa} \leq \text{Tabs}_{\text{CTX}}(id) \downarrow_{\kappa} \)
(9) \( \Sigma_{1}' \downarrow_{\kappa} \leq \Sigma_{1} \downarrow_{\kappa} \leq \Sigma_{2} \downarrow_{\kappa} \)

By (A14)
(10) \( \mathcal{E}_{1}' \downarrow_{\kappa} = \mathcal{E}_{1} \downarrow_{\kappa} \leq \mathcal{E}_{2} \downarrow_{\kappa} \)

sub-subcase iii. \( \ell^- \not\subseteq \kappa, \kappa_e \not\subseteq \kappa, \) updLab(\( e, \ell^- \)) \( \downarrow_{\kappa} = \cdot \)

By DS2
(1) \( \text{DocCS}_{\text{CTX}}[\Gamma, \text{skip} \mid id \notin \Sigma_{1} \downarrow_{\kappa} \)

By \( \Sigma_{1} \downarrow_{\kappa} \leq \Sigma_{2} \downarrow_{\kappa}, \Sigma_{1} = \Sigma_{\text{CTX}} \parallel \Gamma, \text{skip} \mid id, \) and applying EVENTDEQUEUECS2 only changes \( \text{DocCS}, \text{DocCS} \downarrow_{\kappa} = \cdot \)

(2) \( \Sigma_{\text{CTX}}' \parallel \Gamma, \text{cmd}[e/x] \mid id \downarrow_{\kappa} = \Sigma_{\text{CTX}}', \text{skip} \mid id \downarrow_{\kappa} \leq \Sigma_{2} \downarrow_{\kappa} \)

By assumption
(3) \( \mathcal{E}_{1}' = \mathcal{E}_{1}, \mathcal{E}_{1}' \downarrow_{\kappa} \leq \mathcal{E}_{2} \downarrow_{\kappa} \)

case: The proofs for EVENTDEQUEUECORE1 are similar to the proofs for EVENTDEQUEUECS1.

case: The proofs for EVENTDEQUEUECORE2, are similar to the proofs for EVENTDEQUEUECS2.

\[
\begin{align*}
\Sigma_{\text{CTX}}(id) &= (\Psi, \text{Tabs}_{\text{CTX}}(id), \cdots) \\
\text{tabs}_{\text{CTX}}(id) &= (id, \text{Doc}_{\text{CTX}}(id), \text{url}, \text{EventHandlers} \parallel \text{ctx}_{\text{CTX}}(id), \cdots) \\
\text{ctx}_{\text{CTX}}(id) &= (id, \text{eventType}, x, \text{cmd}, e :: \mathcal{E}_{1}, \parallel, \text{id}_{e}, \text{BlockingFlag}, \text{return}) \\
\text{Doc}_{\text{CTX}}(id) &= \text{Docs}_{\text{CTX}}(id) \\
\text{node}_{\text{CTX}}(id) &= \text{node}_{\text{CTX}}(id) \\
\text{labOf}(e) &= \ell^* \\
\text{ctx}_{\text{CTX}}(id) &= \text{ctx}_{\text{CTX}}(id) \parallel \text{ctx}_{\text{CTX}}(id) \\
\Sigma_{\text{CTX}} \parallel \Gamma, \text{skip} \mid id \parallel \mathcal{E} \mapsto \Sigma_{\text{CTX}} \parallel \Gamma, \text{skip} \mid id \parallel \mathcal{E} \\
\end{align*}
\]

EVENTDEQUEUEPAGE1

case: EVENTDEQUEUEPAGE1 satisfies Lemma 16.

Let \( \Sigma_{1} = (\Psi_{1}, \text{Tabs}_{1}, \text{ExtCoreRs}_{1}, \text{progInjCSS}_{1}, \text{Exts}_{1}, \text{Cookies}_{1}, \text{MBookmarks}_{1}, \text{histories}_{1}, \text{UI}_{1}) \)
\( \Sigma_{2} = (\Psi_{2}, \text{Tabs}_{2}, \text{ExtCoreRs}_{2}, \text{progInjCSS}_{2}, \text{Exts}_{2}, \text{Cookies}_{2}, \text{MBookmarks}_{2}, \text{histories}_{2}, \text{UI}_{2}) \)

By assumptions
(A1) \( \Sigma_{1} = \Sigma_{\text{CTX}} \parallel \Gamma, \text{skip} \mid id, \text{Tabs}_{1} = \text{Tabs}'_{\text{CTX}} \parallel \text{Tab}_{1} \)
(A2) \( \text{Tab}_{1} = \text{Tab}_{\text{CTX}} \parallel \Gamma, \text{skip} \mid id \parallel (id, \text{Doc}_{\text{CTX}}(id), \text{url}_{1}, \text{EventHandlers}_{\text{CTX}}(id), \ell_{1}) \)
(A3) \( \text{EventHandler}_{\text{CTX}}(id) \in \text{EventHandlers}_{\text{CTX}}(id) \)
(A4) \( \text{Doc}_{\text{CTX}}(id) = \text{Doc}_{\text{CTX}}(id) \parallel \text{Doc}_{\text{CTX}}(id) \)
(A5) \( \text{node}_{\text{CTX}}(id) \in \text{node}_{\text{CTX}}(id) \)
(A6) \( \text{node}_{\text{CTX}}(id) = (id_{1}, \cdots, \parallel \Gamma, \ell) \)
(A7) \( \text{labOf}(e_{1}) \not\subseteq \ell'^{*} \)
(A8) \( \text{ctx}_{\text{CTX}}(id) = \text{ctx}_{\text{CTX}}(id) \parallel \mathcal{E}_{1}' \parallel \mathcal{E}'_{1} \)
(A9) \( \text{Tab}_{\text{CTX}}(id) = (id, \text{Doc}_{\text{CTX}}(id), \text{url}_{1}, \text{EventHandlers}_{\text{CTX}}(id), \mathcal{E}_{1}, \ell_{1}) \)
(A10) \( \Sigma_{1} = \Sigma_{\text{CTX}}'(id) = \Sigma_{\text{CTX}}'(id) \parallel \text{Tab}_{\text{CTX}}(id) \parallel \text{Tab}_{\text{CTX}}(id) \)
(A11) \( \mathcal{E}_{1}' = \mathcal{E}_{1} \)

By (A8), (A9), (A10)

(1) The only difference between \( \Sigma_{1}' \) and \( \Sigma_{1} \) is \( \Sigma_{1} \) contains \( e_{1} \), while \( \Sigma_{1}' \) does not.

By TAB1, TAB2, EVENT1, EVENT2

(2) \( \forall e_{1}, \Sigma_{1}' \downarrow_{\kappa} \leq \Sigma_{1} \downarrow_{\kappa} \leq \Sigma_{2} \downarrow_{\kappa} \)
By (A11)
(3) \( E'_1 = E_1 \leq E_2 \)

case: EVENTDEQUEUEPAGE2

Let \( \Sigma_1 = (\Psi_1, Tabs_1, ExtCoreRs_1, proghijCSs_1, Exts_1, Cookies_1, MBookmarks_1, histories_1, UI_1) \)
\( \Sigma_2 = (\Psi_2, Tabs_2, ExtCoreRs_2, proghijCSs_2, Exts_2, Cookies_2, MBookmarks_2, histories_2, UI_2) \)

By assumptions
(A1) \( \Sigma_1 = \Sigma_{ctx} \mid \Gamma, \text{skip} \mid id, Tabs_1 = Tabs' :: Tab_1 \)
(A2) \( Tab_1 \Gamma, \text{skip} \mid id = (id, Docs_env(id), \text{url}_1, \text{EventHandler}_\text{CTX}(id), \ell_1) \)
(A3) \( \text{EventHandler}_\text{CTX}(id) \in \text{EventHandler}_\text{CTX}(id) \)
(A4) \( \text{EventHandler}_\text{CTX}(id) = (id, \text{eventType}, \text{x.cmd}, e_1 :: E_1, \text{\langle \text{skip}, \text{id}_c, \text{BlockingFlag}, \text{return} \rangle}) \)
(A5) \( \text{Docs}_\text{env}(id) \in \text{Docs}_\text{env}(id), \text{Docs}_\text{env}(id) = (\ldots, \text{nodes}_\text{env}(id), \ldots) \)
(A6) \( \text{node}_\text{env}(id) \in \text{node}_\text{env}(id) \)
(A7) \( \text{node}_\text{env}(id) = (\ldots, \text{nodes}_1, \ldots, [\Gamma], \ell) \)
(A8) \( e_1 = (\text{id}_c, \text{eventType}, \text{return'}, \ldots, \kappa_e) \)
(A9) \( \kappa_e \subseteq \ell' \)
(A10) \( \ell' = \kappa_e \triangleright \text{int} \ell \)
(A11) \( \text{EventHandler}_\text{CTX}(id) = (id, \text{eventType}, \text{x.cmd}, E_1, \text{\langle \text{cmd}[e_1/x], e_2, \text{BlockingFlag}, \text{return} \rangle}) \)
(A12) \( \text{node}''_\text{env}(id) = \text{node}_\text{env}(id)[\ell \leftrightarrow \ell'], \text{nodes}_1''_\text{env}(id) = \text{nodes}_\text{env}(id)[\text{node}_\text{env}(id) \leftrightarrow \text{node}''_\text{env}(id)] \)
(A13) \( \text{Docs}_\text{env}(id) = \text{Docs}_\text{env}(id)[\text{node}_\text{env}(id) \leftrightarrow \text{node}''_\text{env}(id)] \)
(A14) \( \text{Tab}_\text{CTX}(id) = \text{Tab}_\text{CTX}(id)[\text{Docs}_\text{env}(id) \rightarrow \text{Docs}'_\text{env}(id)] \)
(A15) \( \Sigma'_1 = \Sigma_{ctx} \mid \Gamma, \text{skip} \mid id = \text{Tab}_\text{CTX}(id) \rightarrow \text{Tab}_\text{CTX}(id) \)
(A16) \( \Sigma' = \Sigma'_{ctx} \mid \Gamma, \text{skip} \mid id = \Sigma_1 \rightarrow \Sigma_1 \)

sub-case 1. \( \ell' \triangleq \kappa_e \triangleq \kappa, \text{updLab}(e_1, \ell') \downarrow_\kappa = \text{updLab}(e_1, \ell') \)

By TAB1, TAB2, EVENT1, (A8)

(1) \( \text{Tab}_1\text{CTX} \mid \Gamma, \text{skip} \mid id \downarrow_\kappa = (id, Docs\_env(id) \downarrow_\kappa, \ldots, \text{EventHandler}_\text{CTX}(id), Docs\_env(id) \downarrow_\kappa) \rightarrow \downarrow_\kappa \)

(2) \( \text{Tab}_1\text{CTX} \mid \Gamma, \text{skip} \mid id \downarrow_\kappa = \Sigma_1 \rightarrow \Sigma_1 \downarrow_\kappa \)

By (A7), NODE1, EVENT1

(3) \( \text{node}''_\text{env}(id) \downarrow_\kappa \in \Sigma_1 \downarrow_\kappa \)
(4) \( id \in Docs\_env(id) \downarrow_\kappa \)
(5) \( \text{EventHandler}_\text{CTX}(id) \downarrow_\kappa = (id, \text{eventType}, \text{x.cmd}, e_1 :: E_1, \langle \text{skip}, \text{id}_c, \text{BlockingFlag}, \text{return} \rangle) \)
(6) \( \text{EventHandler}_\text{CTX}(id) \downarrow_\kappa = \text{Tab}_\text{CTX} \mid \Gamma, \text{skip} \mid id \rightarrow_\kappa \)

By \( \Sigma_1 \rightarrow_\kappa \leq \Sigma_2 \rightarrow_\kappa \)

(7) \( \exists \text{Tab}_2\text{CTX} \mid \Gamma, \text{skip} \mid id \in \Sigma_2, \text{such that} \text{Tab}_\text{CTX} \mid \Gamma, \text{skip} \mid id \downarrow_\kappa \leq \text{Tab}_2\text{CTX} \mid \Gamma, \text{skip} \mid id \downarrow_\kappa \)

(8) \( \text{Tab}_2\text{CTX} \mid \Gamma, \text{skip} \mid id \rightarrow_\kappa = (id, Docs\_env(id), \ldots, \text{EventHandler}_\text{CTX}(id), \downarrow_\kappa), \text{where} Docs''_\kappa \downarrow_\kappa \leq Docs''_\kappa \downarrow_\kappa, Docs\_env(id) \downarrow_\kappa \leq Docs\_env(id) \downarrow_\kappa, Docs\_env(id) \rightarrow_\kappa \text{Docs\_env(id)} \)

By (A1), (8), apply EVENTDEQUEUEPAGE2 to \( \Sigma_2, \Sigma_2 = \Sigma_{ctx2} \mid \Gamma, \text{skip} \mid id \)

(9) \( \text{EventHandler}_\text{CTX}(id) = (id, \text{eventType}, \text{x.cmd}, E_2, \langle \text{cmd}[e_2/x], \text{id}_c', \text{BlockingFlag}, \text{return} \rangle) \)
(10) \( \text{node}_\text{env}(id) = \text{node}_\text{env}(id)[\ell \leftrightarrow \ell'] \)
(11) $Docs_{2env}'(id) = Docs_{2env}(id)[node_{2env}(id) \leftarrow node_{2env}'(id)]$

(12) $Tab_{2ctx}'(id) = Tab_{2ctx}(id)[Docs_{2}(id)_{env} \leftarrow Docs_{2}'(id)_{env}]$

(13) $\Sigma'_1 = \Sigma_{ctx}(id) = \Sigma_{ctx}(id)[Tab_{2ctx}(id) \leftarrow Tab_{2ctx}'(id)]$

(14) $E'_2 = \mathcal{E}_2$

By (12), (A11), (A12), (A13), (A14), (A15), (9), (10), (11), (12), (13), Lemma 6, STATE

(17) $node_{env}''(id) \downarrow_{\kappa} \subseteq node_{env}''_{2}(id) \downarrow_{\kappa}$

(18) $Docs_{env}'(id) \downarrow_{\kappa} \subseteq Docs_{env}''_{2}(id) \downarrow_{\kappa}$

(19) $Tab_{ctx}'(id) \downarrow_{\kappa} \subseteq Tab_{ctx}''_{2}(id) \downarrow_{\kappa}$

(20) $\Sigma'_1 \downarrow_{\kappa} \subseteq \Sigma''_1 \downarrow_{\kappa}$

By (A16), (14), $E_1' \subseteq E_2'$

(21) $E_1' \subseteq E_2'$

sub-case ii. $\ell^\prime \subseteq \kappa$, labOf($e_1$) $\not\subseteq \kappa$, updLab($e_1$, $\ell^\prime$) $\downarrow_{\kappa} =$. By (A10), labOf($e_1$) $\not\subseteq \kappa$

(1) $\ell^\prime \not\subseteq \kappa$

By (1), (A11-14), NODE, NODE1, NODE2, TAB1, TAB2, Lemma 6

(2) $node_{env}' \downarrow_{\kappa} = nodes_1 \downarrow_{\kappa}$

(3) $nodes_{env}(id) \downarrow_{\kappa} \subseteq nodes_{env}'(id) \downarrow_{\kappa}$

(4) $Docs_{env}(id) \downarrow_{\kappa} \subseteq Docs_{env}'(id) \downarrow_{\kappa}$

(5) $Docs_{env}(id) \downarrow_{\kappa} \subseteq Docs_{env}'(id) \downarrow_{\kappa}$

(6) $\beta id \in Docs_{env}''(id) \downarrow_{\kappa}$

(7) $\Sigma''_1 \downarrow_{\kappa} \subseteq \Sigma''_1 \downarrow_{\kappa}$

(8) $\Sigma''_1 \downarrow_{\kappa} \subseteq \Sigma''_1 \downarrow_{\kappa}$

By (A15), STATE

(10) $\Sigma'_1 \downarrow_{\kappa} \subseteq \Sigma_1 \downarrow_{\kappa}$

By (A16)

(11) $E'_1 \downarrow_{\kappa} \subseteq E_1 \downarrow_{\kappa}$

sub-case iii. $\ell^\prime \not\subseteq \kappa$, updLab($e_1$, $\ell^\prime$) $\downarrow_{\kappa} =$. By (A5), (A6), (A7), TAB1, TAB2 DOC1, DOC2, NODE2

(1) $\beta node = (id, \ldots) \in Docs_{env}(id) \downarrow_{\kappa}$

(2) $id \notin Docs_{env}(id) \downarrow_{\kappa}$

(3) $prune(EventHandlers_{ctx}(id), Docs_{env}(id) \downarrow_{\kappa}) \downarrow_{\kappa} \not\subseteq Tab_{ctx}(id) \downarrow_{\kappa}$

By $\ell^\prime \not\subseteq \kappa$, (A12), TAB1, TAB2 DOC1, DOC2, NODE2

(4) $\ell^\prime \not\subseteq \kappa$

(5) $\beta node = (id, \ldots) \in Docs_{env}'(id) \downarrow_{\kappa}$

(6) $id \notin Docs_{env}'(id) \downarrow_{\kappa}$

(7) $prune(EventHandlers_{ctx}(id), Docs_{env}'(id) \downarrow_{\kappa}) \downarrow_{\kappa} \not\subseteq Tab_{ctx}'(id) \downarrow_{\kappa}$

By (A11-15), (1), (3), (5), (7)

and EventDequeuePage2 dose not change other components except node_{env}(id) and EventHandler_{ctx}(id)

(8) $\Sigma'_1 \downarrow_{\kappa} \subseteq \Sigma_1 \downarrow_{\kappa}$

By (A15)

(9) $E'_1 \downarrow_{\kappa} \subseteq E_1 \downarrow_{\kappa}$

case: EventDequeueCoreBlocking1
\[ \Sigma_{\text{ctx}}(id) = (\Psi, \text{Tab}s, \text{ExtCoreRs}_{\text{ctx}}(id), \cdots) \]
\[ \text{ExtCore}_R_{\text{ctx}}(id) \in \text{ExtCoreRs}_{\text{ctx}}(id) \]
\[ \text{ExtCore}_R_{\text{ctx}}(id) = (\text{id}, \{\text{\ldots}\}, \text{EventHandlers} :: \text{eh}_{\text{ctx}}, \ell) \]
\[ \text{eh}_{\text{ctx}} = (\cdot, \text{eventType}, \text{x.cmd}, e :: \mathcal{E}_1, \text{|id}_e, \text{blocking}, \text{return}) \]
\[ \text{labOf}(e) \neq \ell \rightarrow \text{eh}_{\text{ctx}}' = (\cdot, \text{eventType}, \text{x.cmd}, \mathcal{E}_1, \text{|id}_e, \text{blocking}, \text{return}) \]
\[ \text{ExtCore}_R_{\text{ctx}}'(id) = \text{ExtCore}_R_{\text{ctx}}(id)[\text{ExtCoreRs}_{\text{ctx}}(id) \leftarrow \text{ExtCoreRs}_{\text{ctx}}'(id)] \]
\[ \Sigma'_{\text{ctx}}(id) = \Sigma_{\text{ctx}}(id)[\text{ExtCoreRs}_{\text{ctx}}(id) \leftarrow \text{ExtCoreRs}_{\text{ctx}}'(id)] \]

By \text{EventDequeueCoreBlocking1}

\[ \Sigma_{\text{ctx}} \cdot \Gamma, \text{skip} \cdot \text{id}; \mathcal{E} \xrightarrow{\tau} \Sigma'_{\text{ctx}} \cdot \Gamma, \text{skip} \cdot \text{id}; \mathcal{E} \]

Let \( \Sigma_1 = (\Psi_1, \text{Tab}s_1, \text{ExtCoreRs}_1, \text{proginjCS}s_1, \text{Ext}s_1, \text{Cookies}_1, \text{MBookmarks}_1, \text{histories}_1, \text{UI}_1) \)
\[ \Sigma_2 = (\Psi_2, \text{Tab}s_2, \text{ExtCoreRs}_2, \text{proginjCS}s_2, \text{Ext}s_2, \text{Cookies}_2, \text{MBookmarks}_2, \text{histories}_2, \text{UI}_2) \]

By assumptions

(A1) \( \Sigma_1 = \Sigma_{\text{ctx}} \cdot \Gamma, \text{skip} \cdot \text{id}, \text{ExtCore}_R_1 = \text{ExtCoreRs}_1'' :: \text{ExtCore}_R \)

(A2) \( \text{ExtCore}_R = \text{ExtCore}_R_1(\text{ctx}); \text{skip} \cdot \text{id} = (\text{id}, (\text{\Gamma}), \text{cmd}, \text{EHs} :: \text{eh}_{\text{ctx}}\text{[skip]}), \ell) \)

(A3) \( \text{eh}_{\text{ctx}}\text{[skip]} = (\cdot, \text{eventType}, \text{x.cmd}, \mathcal{E} :: \text{e}_1, \text{|id}_e, \text{blocking}, \text{return}) \)

(A4) \( \text{labOf}(e_1) \neq \ell \)

(A5) \( \text{eh}_{\text{ctx}}'\text{[skip]} = (\cdot, \text{eventType}, \text{x.cmd}, \mathcal{E} :: \text{e}_1, \text{|id}_e, \text{blocking}, \text{return}) \)

(A6) \( \text{ExtCore}_R_{\text{ctx}}'(id) = \text{ExtCore}_R_{\text{ctx}}(id)[\text{eh}_{\text{ctx}}\text{[skip]} \leftarrow \text{eh}_{\text{ctx}}'] \)

(A7) \( \text{ExtCoreRs}_{\text{ctx}}'(id) = \text{ExtCoreRs}_{\text{ctx}}(id)[\text{ExtCoreRs}_{\text{ctx}}(id) \leftarrow \text{ExtCoreRs}_{\text{ctx}}'(id)] \)

(A8) \( \Sigma'_{\text{ctx}}(id) = \Sigma_{\text{ctx}}(id)[\text{ExtCoreRs}_{\text{ctx}}(id) \leftarrow \text{ExtCoreRs}_{\text{ctx}}'(id)] \)

(A9) \( \Sigma'_1 = \Sigma_{\text{ctx}}(id) \)

(A10) \( \Sigma_{\text{ctx}} \cdot \Gamma, \text{skip} \cdot \text{id}; \mathcal{E}_1 \xrightarrow{\tau} \Sigma'_{\text{ctx}} \cdot \Gamma, \text{skip} \cdot \text{id}; \mathcal{E}_1 = \mathcal{E}'_1 \)

\text{sub-case \text{i.} \( \ell \neq \kappa \)}

By \text{ExtCore1, EH}

(1) \( \text{ExtCore}_R_{\text{ctx}} \cdot \Gamma, \text{skip} \cdot \text{id} \downarrow \kappa = (\text{id}, (\text{\Gamma}), \text{cmd}, \text{EHs} \downarrow \kappa :: \text{eh}_{\text{ctx}}\text{[skip]} \downarrow \kappa), \ell) \)

(2) \( \text{eh}_{\text{ctx}}\text{[skip]} \downarrow \kappa = (\cdot, \text{eventType}, \text{x.cmd}, \mathcal{E} \downarrow \kappa :: \text{e}_1, \text{|id}_e, \text{blocking}, \text{return}) \)

(3) \( \text{ExtCore}_R_{\text{ctx}} \cdot \Gamma, \text{skip} \cdot \text{id} \downarrow \kappa \in \Sigma_1 \downarrow \kappa \)

By \( \Sigma_1 \downarrow \kappa \subseteq \Sigma_2 \downarrow \kappa \)

(4) \( \text{ExtCore}_R_1 \downarrow \kappa \subseteq \text{ExtCore}_R_2 \downarrow \kappa \)

(5) \( \Psi_1 \subseteq \Psi_2 \)

By \text{ExtCoreR1, s.t., ExtCoreR2 = ExtCoreRs'2 :: ExtCoreR2}

(6) \( \text{ExtCore}_R_2 \downarrow \kappa \subseteq \text{ExtCore}_R_2 \downarrow \kappa \)

(7) \( \exists \text{ExtCoreR}_2, \text{st.}, \text{ExtCoreR}_2 = \text{ExtCoreRs}_2'' :: \text{ExtCoreR}_2 \)

\[ \text{eh}_{\text{ctx}}_2 \text{[skip]} = (\cdot, \text{eventType}, \text{x.cmd}, \mathcal{E}' :: \text{e}_2, \text{|id}_e, \text{blocking}, \text{return}) \]

\[ \text{ExtCoreR}_{\text{ctx}}' \cdot \Gamma, \text{skip} \cdot \text{id} \downarrow \kappa \subseteq \text{ExtCoreR}_{\text{ctx}} \cdot \Gamma, \text{skip} \cdot \text{id} \downarrow \kappa \]

\[ \text{ExtCoreR}_{\text{ctx}} \cdot \Gamma, \text{skip} \cdot \text{id} = (\text{id}, (\text{\Gamma}), \text{cmd}, \text{EHs} :: \text{eh}_{\text{ctx}}2\text{[skip]}), \ell), \text{EHs} \downarrow \kappa \subseteq \text{EHs}_2 \downarrow \kappa \]

\[ \text{eh}_{\text{ctx}}2\text{[skip]} = (\cdot, \text{eventType}, \text{x.cmd}, \mathcal{E}' :: \text{e}_2, \text{|id}_e, \text{blocking}, \text{return}) \]

(8) \( \text{labOf}(e_2) \subseteq \kappa, \text{id}_e \downarrow \kappa = \text{id}_1, \text{e}_1 = \text{e}_2 \)

By \text{labOf(e_2) = labOf(e_1) = \ell, apply EventDequeueCoreBlocking1 to \Sigma_2, let \Sigma_2 = \Sigma_{\text{ctx}} \cdot \Gamma, \text{skip} \cdot \text{id}}

(11) \( \text{eh}_{\text{ctx}}2\text{[skip]} = (\cdot, \text{eventType}, \text{x.cmd}, \mathcal{E}' :: \text{skip}), \text{|id}_e, \text{blocking}, \text{return}) \)

(12) \( \text{ExtCoreR}_{\text{ctx}}^2 \cdot \Gamma, \text{skip} \cdot \text{id} \downarrow \kappa \subseteq \text{eh}_{\text{ctx}}2\text{[skip]} \)

(13) \( \text{ExtCoreR}_{\text{ctx}} \cdot \Gamma, \text{skip} \cdot \text{id} \downarrow \kappa \subseteq \text{ExtCoreR}_{\text{ctx}} \cdot \Gamma, \text{skip} \cdot \text{id} \downarrow \kappa \)

(14) \( \Sigma_{\text{ctx}}' \cdot \Gamma, \text{skip} \cdot \text{id}; \mathcal{E}_2 \xrightarrow{\tau} \Sigma'_{\text{ctx}} \cdot \Gamma, \text{skip} \cdot \text{id}; \mathcal{E}_2 = \mathcal{E}_2 \)

By \text{(A5), (7), (11)}

(16) \( \text{eh}_{\text{ctx}}'\text{[skip]} \downarrow \kappa \subseteq \text{eh}_{\text{ctx}_2} \cdot \text{skip} \downarrow \kappa \)
By (16), Lemma 6

(17) \( ExtCoreR'_{ctx}(\Gamma, \text{skip}(id)) \leq ExtCoreR'_{ctx}(\Gamma, \text{skip}(id)) \)
(18) \( ExtCoreR'_{ctx}(\Gamma, \text{skip}(id)) \leq ExtCoreR'_{ctx}(\Gamma, \text{skip}(id)) \)

As \( ch_{ctx}[\text{skip}] \) in \( ExtCoreR_1 \) and \( ch_{ctx2}[\text{skip}] \) in \( ExtCoreR_2 \) dequeue the same event, other eventhandlers are not changed

(19) \( ExtCoreR'_{ctx}(\Gamma, \text{skip}(id)) \leq_{e} ExtCoreR'_{ctx}(\Gamma, \text{skip}(id)) \)

(20) for all blocking handler \( e \), \( ExtCoreR'_{ctx}(\Gamma, \text{skip}(id)) \leq_{e,e} ExtCoreR'_{ctx}(\Gamma, \text{skip}(id)) \)

By (19), (20)

(21) \( ExtCoreR'_{ctx}(\Gamma, \text{skip}(id)) \leq_{e} ExtCoreR'_{ctx}(\Gamma, \text{skip}(id)) \)

By (21), state

(22) \( \Sigma'_{ctx}(id) \leq \Sigma'_{ctx}(id) \), that is \( \Sigma'_{1} \leq \Sigma'_{2} \)

By \( \Sigma' \leq \Sigma'_{1} \leq \Sigma'_{2} \leq \Sigma' \)

By \( \Sigma' \leq \Sigma'_{1} \leq \Sigma'_{2} \leq \Sigma' \)

sub-case ii. \( \ell \leq \kappa, e_{1} \neq \kappa \)

By \( ExtCore_1, EH \)

(1) \( ExtCoreR_{ctx}(\Gamma, \text{skip}(id)) \leq \Sigma'_{ctx}(id) \), that is \( \Sigma'_{1} \leq \Sigma'_{2} \)

By \( \Sigma'_{1} \leq \Sigma'_{2} \leq \Sigma' \)

By \( \Sigma'_{1} \leq \Sigma'_{2} \leq \Sigma' \)

sub-case iii. \( \ell \leq \kappa \)

By \( ExtCore_2 \)

(1) \( ExtCoreR_{ctx}(\Gamma, \text{skip}(id)) \leq \Sigma'_{ctx}(id) \), that is \( \Sigma'_{1} \leq \Sigma'_{2} \)

By \( \Sigma'_{1} \leq \Sigma'_{2} \leq \Sigma' \)

By assumption

(4) \( \Sigma'_{1} \leq \Sigma'_{2} \leq \Sigma' \)

case: EventDequeueCoreBlocking2

\[ \Sigma'_{ctx}(id) = (\Psi, Tabs, ExtCoreR_{ctx}(id), \ldots) \]

\( ExtCoreR_{ctx}(id) \in ExtCoreR_{ctx}(id) \)

\( ExtCoreR_{ctx}(id) = (id, \ldots, EventHandlers :: eh_{ctx}, \ell) \)

\( eh_{ctx} = (\ell, \text{eventType}, x, \text{cmd}, e :: \text{E} \psi :: \text{E}, \text{blocking}, \text{return}) \)

\( e = (id, \text{eventType}, \text{return}, \ldots, \kappa) \)

\( \kappa = \ell \)

\( \psi = \text{ProcBltEvtState}(\kappa, id, e) \)

\( eh'_{ctx} = (\ell, \text{eventType}, x, \text{cmd}, E \psi :: \text{E}, \text{blocking}, \text{some}(e, id)) \)

EventDequeueCoreBlocking2

Let \( \Sigma_1 = (\Psi_1, Tabs_1, ExtCoreR_1, \text{progInjCSs}_1, Exts_1, \text{Cookies}_1, \text{MBookmarks}_1, \text{histories}_1, \text{UI}_1) \)

\( \Sigma_2 = (\Psi_2, Tabs_2, ExtCoreR_2, \text{progInjCSs}_2, Exts_2, \text{Cookies}_2, \text{MBookmarks}_2, \text{histories}_2, \text{UI}_2) \)

By assumptions
(A1) $\Sigma_1 = \Sigma_{ctx}[\Gamma, skip][id]_R, ExtCoreRs_1' = ExtCoreRs_1'' :: ExtCoreR$

(A2) $ExtCoreR = ExtCoreR_{ctx}[\Gamma, skip][id] = (id, ([\Gamma], cmd, EHs :: eh_{ctx}[skip]), \ell)$

(A3) $eh_{ctx}[skip] = (\cdot, eventType, x, cmd, E :: e_1, [skip], id_e, blocking, return)$

(A4) $e_1 = (id_e, eventType, return, \ldots, \kappa_e), \kappa_e = \ell^-$

(A5) fresh(id_e)

(A6) $eh'_{ctx}[cmd[e_1/x]] = (\cdot, eventType, x, cmd, E :: cmd[e_1/x], id_e', blocking, some(e_1, id_e))$

(A7) $ExtCoreR_{ctx}(id) = ExtCoreR_{ctx}(id)[eh_{ctx} \leftarrow eh'_{ctx}]$

(A8) $ExtCoreRs' = ExtCoreRs_{ctx}(id)[ExtCoreR_{ctx}(id) \leftarrow ExtCoreRs_{ctx}(id)]$

(A9) $\psi_1 = ProcBnkEvState(\kappa_e, id_e, e_1), \Psi_1' = \Psi_1 :: \psi_1$

(A10) $\Sigma''_{ctx}(id) = \Sigma_{ctx}(id)[ExtCoreR_{ctx}(id) \leftarrow ExtCoreRs_{ctx}(id)] \leftarrow \Psi_1 \leftarrow \Psi_1'$

(A11) $\Sigma''_{ctx}(id)$

(A12) $\Sigma_{ctx}[\Gamma, skip][id; E_1 \uparrow \text{updLab}(e_1, \ell^-)] \Sigma''_{ctx}[\Gamma, cmd[e_1/x]]_R; E_1', E_1' = E_1$

sub-subcase i. $\ell^- \subseteq \kappa$

By ExtCore1, EH

(1) $ExtCoreR_{ctx}[\Gamma, skip][id]_R \downarrow \kappa = (id, ([\Gamma], cmd, EHs \downarrow \kappa :: eh_{ctx}[skip] \downarrow \kappa), \ell)$

(2) $eh_{ctx}[skip] \downarrow \kappa = (\cdot, eventType, x, cmd, E \downarrow \kappa :: e_1, [skip], id_e, blocking, return)$

By definition

(3) $\Sigma_1 \downarrow \kappa \subseteq \Sigma_2 \downarrow \kappa$

(4) $ExtCoreRs_1 \downarrow \kappa \subseteq ExtCoreRs_2 \downarrow \kappa$

(5) $\Psi_1 \downarrow \kappa \subseteq \Psi_2 \downarrow \kappa$

By ExtCoreRs_1 \downarrow \kappa \subseteq ExtCoreRs_2 \downarrow \kappa

(6) $ExtCoreRs_1 \downarrow \kappa \subseteq ExtCoreRs_2 \downarrow \kappa$

(7) $\exists ExtCoreR_{ctx}[\Gamma, skip][id] \in ExtCoreRs_2 \downarrow \kappa \text{ s.t., ExtCoreR}_{ctx}[\Gamma, skip][id] \downarrow \kappa = ExtCoreR_{ctx}[\Gamma, skip][id] \downarrow \kappa$

By labOf(e_1) = \ell^-, apply EVENTDEQUEUECOREBLOCKING2 to \Sigma_2, let \Sigma_2 = \Sigma_{ctx2}[\Gamma, skip][id]

(11) fresh(id_e'), \psi_2 = ProcBnkEvState(\kappa_e, id_e', e_2), \psi_2 = \psi_1, \Psi_2' = \Psi_2 :: \psi_2$

(12) $eh'_{ctx2}[cmd[e_2/x]] = (\cdot, eventType, x, cmd, E' :: cmd[e_2/x], id_e', blocking, some(e_2, id_e'))$

(13) $ExtCoreR_{ctx2}[\Gamma, skip][id] = ExtCoreR_{ctx2}[\Gamma, skip][id][eh_{ctx2}[cmd[e_2/x]] \leftarrow eh'_{ctx2}[cmd[e_2/x]]]$

(14) $ExtCoreRs_{ctx2}[id] = ExtCoreRs_{ctx2}[id][ExtCoreR_{ctx2}[\Gamma, skip][id] \leftarrow ExtCoreR_{ctx2}[\Gamma, skip][id]]$

(15) $\Sigma'_{ctx2}(id) = \Sigma_{ctx2}(id)[ExtCoreRs_{ctx2}(id) \leftarrow ExtCoreRs_{ctx2}(id)] \leftarrow \Psi_2 \leftarrow \Psi_2'$

(16) $\Sigma'_{ctx2}[\Gamma, skip][id; \Sigma'_{ctx2}[\Gamma, cmd[e_2/x]]_R; E_2', E_2' = E_2$

By (12)

(17) $eh'_{ctx2}[skip] \downarrow \kappa \subseteq eh'_{ctx2}[skip] \downarrow \kappa$

By (17), Lemma 6

(18) $ExtCoreR_{ctx2}(id) \subseteq ExtCoreR_{ctx2}(id)$

(19) $ExtCoreRs_{ctx2}(id) \subseteq ExtCoreRs_{ctx2}(id)$

As both of ExtCoreR_1 and ExtCoreR_2 dequeue the same event without changing other parts

(20) $ExtCoreRs_{ctx2}[\Gamma, skip][id][id] \subseteq ExtCoreRs_{ctx2}[\Gamma, skip][id]$

By (5), $e_1 = e_2$

(21) $\psi_1 \downarrow \kappa = \psi :: \psi_1 :: \psi_12 :: \psi_13$

$\psi \sim e_1$

$\psi_11$ contains states of the form ProcBnkEvState(\cdot, \cdot, e_1)$
The proofs for reading APIs and DOM.NODE.WRITE are straightforward as the structure of the tree does not change by these APIs. The equivalence relation can be established easily. The interesting APIs are the ones that change the tree structure.

**Case: DOM.APPEND.CHILDREN(1A)**

DOM.APPEND.CHILDREN(A)

\[ \Sigma_{ctx}(id) = (\Psi, Tabs \uplus t_{ctx}(id), \cdots) \]

\[ \ell_1 = \text{ctxOfId}(\Sigma_{ctx} \upharpoonright \Gamma \downarrow \chi, \text{let } x = \text{domAPI.appendChild}(id_1, id_d, id_n, node_1, \ell_1) \text{ in cmd } \chi x \downarrow \chi \]

\[ \chi = \ell_1 \quad t = (id_1, \ldots, \text{Docs } :: \ell_1, \cdots) \]

\[ \text{Doc} = (id_1, \ldots, \text{nodes}, \ldots) \quad \text{node} \in \text{nodes} \quad \text{node} = (id_n, \ldots, \ell_{children}, \ldots, \ell_{\text{children}_{\text{pre}}}, \ldots) \]

\[ \ell_{pre} \in \ell_{children}^* \quad \ell_{\text{parents}} \in \ell_{\text{parents}}^* \quad \ell_{\text{success}} = \text{nextSibleOf(last(nodes1))} \quad \ell_{\text{success}} \in \ell_{\text{success}}^* \]

\[ \text{Doc}' = \text{Doc}[\text{node } \leftarrow \text{append}(\text{node}, \text{node}_1)] \quad t' = t[D, \text{let } \text{Doc} = \text{Doc}' \text{ in } \Sigma_{ctx}(\text{id})[t \leftarrow t'] \]

\[ \Sigma_{ctx} \upharpoonright \Gamma, \text{let } x = \text{domAPI.appendChild}(id_1, id_d, id_n, node_1, \ell_1) \text{ in cmd } \chi x \downarrow \chi \]

**Subcase:** the script is a content script handler.

By assumptions

(A1) \[ \Sigma_1 = \Sigma_{ctx}(id) = (\Psi, Tabs \uplus t_{ctx}(id), \cdots) \]

(A2) \[ \ell_1 = \text{ctxOfId}(\Sigma_{ctx} \upharpoonright \Gamma, \text{let } x = \text{domAPI.appendChild}(id_1, id_d, id_n, node_1, \ell_1) \text{ in cmd } \chi x \downarrow \chi \]

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There are two cases here. One is that such append float some labels, the other is not. In the latter case, the update does not affect the projection and less than relation. In the former case, the projection of the dom will sever links between nodes. In this case, the less than relation can be re-established using a different set of rules that take into consideration the missing links.

Sub-case 1. The script’s label $\ell_1 \not\subseteq \kappa_a$.

Let $\Sigma_2 = \Sigma_{ctx}(id) \not\subseteq \kappa_a$.

Here, no labels are tainted due to the addition of new node.

The resulting state still relation to each other using the same derivation.

Sub-case 2. The script’s label $\ell_1 \subseteq \kappa$.

Let $\Sigma_2 = \Sigma_{ctx}(id) \subseteq \kappa_a$.

Here, labels are painted due to the addition of new node.

The resulting state still relation to each other using the same derivation.
5.3 Proof of Lemma 14

case: BookmarkGet

\[
\Sigma = (\Psi, \ldots, MBookmarks, \ldots) \quad \Psi = \Psi' :: \text{chrome.bookmarks.get}(\kappa, id_{cb}, ids)
\]

books = selectBookmark(MBookmarks, \kappa)

result = bookmarkQuery(books, chrome.bookmarks.get, ids)

e = \text{fresh(id}_{e\})

nextStateC(\Sigma, \text{chrome.bookmarks.get}(\kappa, id_{cb}, ids)) = \Sigma'\rangle e

Let \(\Sigma_1 = (\Psi_1, Tabs_1, ExtCoreRs_1, progInjCSs_1, Extss_1, Cookies_1, MBookmarks_1, histories_1, UI_1)\)

\(\Sigma_2 = (\Psi_2, Tabs_2, ExtCoreRs_2, progInjCSs_2, Extss_2, Cookies_2, MBookmarks_2, histories_2, UI_2)\)

By assumptions

(A1) \(\Psi_1 = \Psi'_1 :: \psi_1\)

(A2) \(\psi_1 = \text{chrome.bookmarks.get}(\kappa_1, id_{cb}, ids)\)

(A3) \(\text{books}_1 = \text{selectBookmark}(\text{MBookmarks}_1, \kappa)\)

(A4) \(\text{result}_1 = \text{bookmarkQuery}(\text{books}_1, \text{chrome.bookmarks.get}, ids)\)

(A5) \(\text{fresh(id}_{e\})\)

(A6) \(e_1 = (id_{e\}, id_{cb}, \text{none}, \text{result}_1, \kappa)\)

(A7) \(\Sigma'_1 = \Sigma_1[\Psi_1 \leftarrow \Psi'_1]\)

sub-case sub-case i. \(\kappa_1 \subseteq \kappa\)

By BrowserState1

(1) \(\psi_1 \downarrow_{\kappa} = \psi_1\)

By \(\Sigma_1 \downarrow_{\kappa} \leq \Sigma_2 \downarrow_{\kappa}, \) Lemma 11, and (1)

(2) \(\Psi_1 \downarrow_{\kappa} \leq \Psi_2 \downarrow_{\kappa}\)

(3) \(\exists \psi_2 \in \Psi_2 \text{ s.t. } \psi_1 \downarrow_{\kappa} \leq \psi_2 \downarrow_{\kappa}, \) that is \(\psi_2 = \psi_1 = \text{chrome.bookmarks.get}(\kappa_1, id_{cb}, ids), \)

\(\Psi_2 = \Psi'_2 :: \psi_2, \Psi'_2 \downarrow_{\kappa} \leq \Psi'_2 \downarrow_{\kappa}\)

Apply BookmarkGet to \(\Sigma_2\)

(4) \(\text{books}_2 = \text{selectBookmark}(\text{MBookmarks}_2, \kappa_1)\)

(5) \(\text{result}_2 = \text{bookmarkQuery}(\text{books}_2, \text{chrome.bookmarks.get}, ids)\)

(6) \(\text{fresh(id}_{e\})\)

(7) \(e_2 = (id_{e\}, id_{cb}, \text{none}, \text{result}_2, \kappa)\)

(8) \(\Sigma'_2 = \Sigma_2[\Psi_2 \leftarrow \Psi'_2]\)

By MBookmarks \(\downarrow_{\kappa} \leq \text{bbm} \) MBookmarks \(\downarrow_{\kappa}, \kappa_1 \subseteq \kappa, \) and the definition of selectBookmark

(9) \(\text{books}_2 = \text{books}_1\)

(10) \(\text{result}_2 = \text{result}_1\)

(11) \(e_2 = e_1\)

By EVENT1, (11)

(12) \(e_1 \downarrow_{\kappa} = e_2 \downarrow_{\kappa}\)

By STATE, (A7), (8), (3)

(13) \(\Sigma'_1 \downarrow_{\kappa} \leq \Sigma'_2 \downarrow_{\kappa}\)

sub-case sub-case ii. \(\kappa_1 \not\subseteq \kappa\)

By BrowserState2, Lemma 12

(1) \(\psi_1 \downarrow_{\kappa} = \cdot\)

(2) \(\Psi'_1 \downarrow_{\kappa} \leq \Psi_1 \downarrow_{\kappa}\)

By (A6), EVENT2

(3) \(e_1 \downarrow_{\kappa} = \cdot\)

By STATE, (A7), (2), \(\Sigma_1 \downarrow_{\kappa} \leq \Sigma_2 \downarrow_{\kappa}\)

(4) \(\Sigma'_1 \downarrow_{\kappa} \leq \Sigma_1 \downarrow_{\kappa}\)
(5) $\Sigma'_1 \downarrow_\kappa \leq \Sigma_2 \downarrow_\kappa$

The proofs for `bookmarkGetChildren`, `bookmarkGetRecent`, `bookmarkGetTree`, `bookmarkGetSubTree`, `bookmarkSearch` are similar to the proofs for this rule.

**case:** `BookmarkCreate(1)`

$\Sigma = (\Psi, \cdots, MBookmarks, \cdots)$

$\Psi = \Psi' :: {\text{chrome.bookmarks.create}}(\kappa, id_{cb}, (id_{parent}, positionIndex, title, url))$

$MBookmarks = MBookmarks'' :: {\text{bookmarks}}(\kappa)$

$(\text{bookmarks}', result) = \text{bookmarkWrite}(\text{bookmarks}, \text{chrome.bookmarks.create}, (id_{parent}, positionIndex, title, url))$

$fresh(id_{e})$

$e = (id_{e}, id_{cb}, \text{none}, result, \kappa) \quad MBookmarks' = MBookmarks'' :: (\text{bookmark}', \kappa)$

$\Sigma' = \Sigma'[\Psi 
\Rightarrow \Psi'][MBookmarks \leftarrow MBookmarks']$

`nextStateC(\Sigma, \text{chrome.bookmarks.create}(\kappa, id_{cb}, (id_{parent}, positionIndex, title, url))) = \Sigma'; e`

Let $\Sigma_1 = (\Psi_1, Tabs_1, ExtCoreRs_1, progInjCSs_1, Extss_1, Cookies_1, MBookmarks_1, histories_1, UI_1)$

$\Sigma_2 = (\Psi_2, Tabs_2, ExtCoreRs_2, progInjCSs_2, Extss_2, Cookies_2, MBookmarks_2, histories_2, UI_2)$

By assumptions

(A1) $\Psi_1 = \Psi'_1 :: \psi_1$

(A2) $\psi_1 = \text{chrome.bookmarks.create}(\kappa_1, id_{cb}, (id_{parent}, positionIndex, title, url))$

(A3) $MBookmarks_1 = MBookmarks'' :: MBookmark_1$

(A4) $MBookmark_1 = (\text{bookmarks}_1, \kappa_1)$

(A5) $(\text{bookmarks}_1, \text{result}_1) = \text{bookmarkWrite}(\text{bookmarks}_1, \text{chrome.bookmarks.create}, (id_{parent}, positionIndex, title, url))$

(A6) $\text{bookmarkWrite}(\text{bookmarks}_1, \text{chrome.bookmarks.create}, (id_{parent}, positionIndex, title, url))$

(A7) $fresh(id_{e1})$

(A8) $e_1 = (id_{e1}, id_{cb}, \text{none}, result_1, \kappa_1)$

(A9) $MBookmarks'_1 = MBookmarks_1[\text{bookmark}_1 \leftarrow \text{bookmark}'_1]$

(A10) $MBookmarks'_1 = MBookmarks_1[\text{bookmark}_1 \leftarrow \text{bookmark}'_1]$

(A11) $\Sigma'_1 = \Sigma'[\Psi_1 \leftarrow \Psi'_1][MBookmarks_1 \leftarrow MBookmarks'_1]$

**sub-subcase i. $\kappa_1 \subseteq \kappa$**

By `BrowserState1`

(1) $\psi_1 \downarrow_\kappa = \psi_1$

By $\Sigma_1 \downarrow_\kappa \leq \Sigma_2 \downarrow_\kappa$, Lemma 11, and (1)

(2) $\Psi_1 \downarrow_\kappa \leq \Psi_2 \downarrow_\kappa$

(3) $\exists \psi_2 \in \Psi_2 \text{ s.t. } \psi_1 \downarrow_\kappa \leq \psi_2 \downarrow_\kappa$,

that is $\psi_2 = \psi_1 = \text{chrome.bookmarks.create}(\kappa_1, id_{cb}, (id_{parent}, positionIndex, title, url))$, $\Psi_2 = \psi'_2 :: \psi_2, \Psi'_1 \downarrow_\kappa \leq \Psi'_2 \downarrow_\kappa$

By `Bookmark1`

(4) $MBookmark_1 \downarrow_\kappa = MBookmark_1$

By $MBookmarks_1 \downarrow_\kappa \leq bkm MBookmarks_2 \downarrow_\kappa$, (4), `MBookmarks`

(5) $\exists MBookmark_2 \in MBookmarks_2\text{, s.t. } MBookmark_1 \downarrow_\kappa \leq MBookmark_2 \downarrow_\kappa$,

that is $MBookmark_2 = MBookmark_1$

(6) $MBookmarks_2 = MBookmarks'' :: MBookmark_2$

(7) $MBookmarks_2 \downarrow_\kappa = MBookmarks'' \downarrow_\kappa$

By (3), (5), apply `BookmarkCreate(1)` to $\Sigma_2$

(8) $MBookmark_2 = (\text{bookmarks}_1, \kappa_1)$

(9) $(\text{bookmarks}_1', \text{result}_1) = \text{bookmarkWrite}(\text{bookmarks}_1, \text{chrome.bookmarks.create}, \text{...})$

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(10) fresh($id_{e_2}$)

(11) $e_2 = (id_{e_2}, id_{cb}, none, result_1, \kappa_1)$

(12) $MBookmarks'_2 = MBookmarks_2[bookmark_1 \leftarrow bookmark'_1]$

(13) $MBookmarks'_2 = MBookmarks_2[MBookmark_2 \leftarrow MBookmarks'_2]$

(14) $\Sigma'_2 = \Sigma_2[\Psi_2 \leftarrow \Psi'_2][MBookmarks_2 \leftarrow MBookmarks'_2]$

By $MBookmarks_1 \downarrow_{\kappa} \leq_b km MBookmarks_2 \downarrow_{\kappa}, \kappa_1 \subseteq \kappa,$ and the definition of selectBookmark

(15) bookmarks_2 = bookmarks_1

(16) $MBookmarks'_2 = MBookmarks'_1$

By (A10), (7), (13), (16), BOOKMARKS

(17) $MBookmarks'_1 \leq_{bkm} MBookmarks_2$

By EVENT1, (A8)

(18) $e_1 \downarrow_{\kappa} \leq_e \downarrow_{\kappa}$

By STATE, (A11), (3), (14), (17)

(19) $\Sigma'_1 \downarrow_{\kappa} \leq \Sigma'_2 \downarrow_{\kappa}$

sub-subcase ii. $\kappa_1 \nsubseteq \kappa$

By BROWSERSTATE2, Lemma 12

(1) $\psi_1 \downarrow_{\kappa} = \cdot$

(2) $\Psi'_1 \downarrow_{\kappa} \leq_e \downarrow_{\kappa}$

By MBOOKMARK2

(3) $MBookmark_1 \downarrow_{\kappa} = MBookmark'_1 \downarrow_{\kappa} = \cdot$

By (A3), (A10), (3)

(4) $MBookmarks_1 \downarrow_{\kappa} = MBookmarks'_1 \downarrow_{\kappa}$

By STATE, (A11), (2), (4), $\Sigma_1 \downarrow_{\kappa} \leq \Sigma_2 \downarrow_{\kappa}$

(5) $\Sigma'_1 \downarrow_{\kappa} \leq \Sigma_1 \downarrow_{\kappa}$

(6) $\Sigma'_1 \downarrow_{\kappa} \leq \Sigma_2 \downarrow_{\kappa}$

By (A8), EVENT2

(7) $e_1 \downarrow_{\kappa} = \cdot$

The proofs for BOOKMARKMOVE(1), BOOKMARKUPDATE(1), BOOKMARKREMOVE(1), BOOKMARKREMOVE-TREE(1) are similar to the proofs for the rule BOOKMARKCREATE(1).

case: BOOKMARKCREATE(2)

\[ \Sigma = (\Psi, \ldots, MBookmarks, \ldots) \]

\[ \Psi = \Psi' :: \text{chrome.bookmarks.create}(\kappa, id_{cb}, (id_{parent}, positionIndex, title, url)) \]

\[ \not\exists MBookmark \in MBookmarks \text{ s.t. labOf(MBookmark) =}\kappa \]

bookmarks_1 = selectBookmark(MBookmarks, \kappa)

(bookmarks'_1, result) = bookmarkWrite(bookmarks_1, \text{chrome.bookmarks.create},

(id_{parent}, positionIndex, title, url))

\[ fresh(id_c) \]

\[ e = (id_e, id_{cb}, none, result, \kappa) \quad MBookmarks'_1 = MBookmarks :: (bookmarks'_1, \kappa) \]

\[ \Sigma' = \Sigma[\Psi \leftarrow \Psi'][MBookmarks \leftarrow MBookmarks'] \]

nextStateC($\Sigma, \text{chrome.bookmarks.create}(\kappa, id_{cb}, (id_{parent}, positionIndex, title, url))) = \Sigma'; e$

Let $\Sigma_1 = (\Psi_1, Tabs_1, ExtCoreRs_1, prog\text{InjCSS}_1, Ext_1, Cookies_1, MBookmarks_1, histories_1, UI_1)$

$\Sigma_2 = (\Psi_2, Tabs_2, ExtCoreRs_2, prog\text{InjCSS}_2, Ext_2, Cookies_2, MBookmarks_2, histories_2, UI_2)$

By assumptions

(A1) $\Psi_1 = \Psi'_1 :: \psi_1$
(A2) $\psi_1 = \text{chrome.bookmarks.create}(\kappa_1, id_ch, (id\_parent, positionIndex, title, url))$

(A3) $\not{\exists} M\text{Bookmark} \in M\text{Bookmarks}_1 \text{ s.t. } \text{labOf}(M\text{Bookmark}_1) = \kappa_1$

(A4) $\text{bookmarks}_1 = \text{selectBookmark}(M\text{Bookmarks}, \kappa_1)$

(A5) $(\text{bookmarks}_1, \text{result}_1) = \text{bookmarkWrite}(\text{bookmarks}_1, \text{chrome.bookmarks.create},$

(A6) $(\text{id}\_parent, \text{positionIndex}, \text{title}, \text{url}))$

(A7) $M\text{Bookmark}_1 = (\text{bookmarks}_1', \kappa_1)$

(A8) $M\text{Bookmarks}_1' = M\text{Bookmarks}_1 :: M\text{Bookmark}_1$

(A9) $\text{fresh}(\text{id}_b)$

(A10) $e_1 = (\text{id}_b, \text{id}_c, \text{none}, \text{result}_1, \kappa_1)$

(A11) $\Sigma'_1 = \Sigma_1[\Psi_1 \leftarrow \Psi'_1][M\text{Bookmarks}_1' \leftarrow M\text{Bookmarks}_1]\$

**sub-subcase i. $\kappa_1 \subseteq \kappa$**

By BROWSERSTATE1

(1) $\psi_1 \downarrow_{\kappa} = \psi_1$

By $\Sigma_1 \downarrow^\kappa \leq \Sigma_2 \downarrow^\kappa$, Lemma 11, and (1)

(2) $\Psi_1 \downarrow^\kappa \leq \Psi_2 \downarrow^\kappa$

(3) $\exists \psi_2 \in \Psi_2 \text{ s.t. } \psi_1 \downarrow^\kappa \leq \psi_2 \downarrow^\kappa$

that is $\psi_2 = \psi_1 = \text{chrome.bookmarks.create}(\kappa_1, id_ch, (id\_parent, positionIndex, title, url))$

$\Psi_2 = \Psi'_2:: \psi_2, \Psi'_2 \downarrow^\kappa \leq \psi'_2 \downarrow^\kappa$

By MBOOKMARK1

(4) $\forall M\text{Bookmark} \in M\text{Bookmarks}_1,$
if $\text{labOf}(M\text{Bookmark}) = \kappa_1, M\text{Bookmark} \downarrow^\kappa = M\text{Bookmark}$
$M\text{Bookmark} \in M\text{Bookmarks}_1 \downarrow^\kappa$

(5) $\forall M\text{Bookmark} \in M\text{Bookmarks}_2,$
if $\text{labOf}(M\text{Bookmark}) = \kappa_1, M\text{Bookmark} \downarrow^\kappa = M\text{Bookmark}$
$M\text{Bookmark} \in M\text{Bookmarks}_2 \downarrow^\kappa$

By (A3), (4)

(6) $\not{\exists} M\text{Bookmark} \in M\text{Bookmarks}_1 \downarrow^\kappa \text{ s.t. } \text{labOf}(M\text{Bookmark}) = \kappa_1$

By $M\text{Bookmarks}_1 \downarrow^\kappa \leq \text{bkm} M\text{Bookmarks}_2 \downarrow^\kappa, M\text{BOOKMARKS}, (5), (6)$

(7) $M\text{Bookmarks}_2 \downarrow^\kappa = M\text{Bookmarks}_1 \downarrow^\kappa$

(8) $\not{\exists} M\text{Bookmark} \in M\text{Bookmarks}_2 \text{ s.t. } \text{labOf}(M\text{Bookmark}) = \kappa_1$

Proof: if $M\text{Bookmark} \in M\text{Bookmarks}_2 \text{ s.t. labOf}(M\text{Bookmark}) = \kappa_1$
then $M\text{Bookmark} \in M\text{Bookmarks}_2 \downarrow^\kappa$ which conflicts with (7)

By (3), (8), apply BOOKMARKCREATE(2) to $\Sigma_2$

(9) $\text{bookmarks}_2 = \text{selectBookmark}(M\text{Bookmarks}_2, \kappa_1)$

(10) $(\text{bookmarks}_2, \text{result}_2) = \text{bookmarkWrite}(\text{bookmarks}_2, \text{chrome.bookmarks.create},$

(11) $(\text{id}\_parent, \text{positionIndex}, \text{title}, \text{url}))$

(12) $M\text{Bookmark}_2 = (\text{bookmarks}_2', \kappa_1)$

(13) $M\text{Bookmarks}_2' = M\text{Bookmarks}_2 :: M\text{Bookmark}_2$

(14) $\text{fresh}(\text{id}_b)$

(15) $e_2 = (\text{id}_b, \text{id}_c, \text{none}, \text{result}_2, \kappa_1)$

(16) $\Sigma'_2 = \Sigma_2[\Psi_2 \leftarrow \Psi'_2][M\text{Bookmarks}_2' \leftarrow M\text{Bookmarks}_2']$

By $M\text{Bookmarks}_1 \downarrow^\kappa \leq \text{bkm} M\text{Bookmarks}_2 \downarrow^\kappa, \kappa_1 \subseteq \kappa,$ and the definition of selectBookmark, (4), (5)

(17) $\text{bookmarks}_2 = \text{bookmarks}_1$

By (A5), (10), (17)

(18) $\text{bookmarks}_2' = \text{bookmarks}_1'$

(19) $\text{result}_2 = \text{result}_1$

By (17), (A7), (12)

(20) $M\text{Bookmark}_2 = M\text{Bookmark}_2$
By (A8), (7), (13), (20), BOOKMARKS
(21) \( M\text{bookmarks}'_1 = M\text{bookmarks}'_2 \)
(22) \( M\text{bookmarks}'_1 \leq_{bkm} M\text{bookmarks}'_2 \)

By STATE, (A11), (3), (16), (22)
(23) \( \Sigma'_1 \downarrow_{\kappa} \leq \Sigma'_2 \downarrow_{\kappa} \)

By EVENT1, (A8), (15), (19)
(24) \( e_1 \downarrow_{\kappa} \leq e_2 \downarrow_{\kappa} \)

sub-subcase ii. \( \kappa_1 \not\subseteq \kappa \)

By BROWSERSTATE2, Lemma 12
(1) \( \psi_1 \downarrow_{\kappa} = \cdot \)
(2) \( \Psi' \downarrow_{\kappa} \leq_{c} \Psi_1 \downarrow_{\kappa} \)

By MBOOKMARK2, (A7)
(3) \( M\text{bookmark}_1 \downarrow_{\kappa} = \cdot \)

By (A8), (3)
(4) \( M\text{bookmarks}_1 \downarrow_{\kappa} = M\text{bookmarks}'_1 \downarrow_{\kappa} \)
(5) \( M\text{bookmarks}_1 \downarrow_{\kappa} \leq_{bkm} M\text{bookmarks}_1 \downarrow_{\kappa} \)

By STATE, (A11), (2), (5), \( \Sigma_1 \downarrow_{\kappa} \leq \Sigma_2 \downarrow_{\kappa} \)
(5) \( \Sigma'_1 \downarrow_{\kappa} \leq \Sigma_1 \downarrow_{\kappa} \)
(6) \( \Sigma'_2 \downarrow_{\kappa} \leq \Sigma_2 \downarrow_{\kappa} \)

By (A10), EVENT2
(7) \( e_1 \downarrow_{\kappa} = \cdot \)

The proofs for BOOKMARKMOVE(2), BOOKMARKUPDATE(2), BOOKMARKREMOVE(2), BOOKMARKREMOVE TREE(2) are similar to the rule BOOKMARKCREATE(2).

case: CookieWebsiteSet(1)

\[
\Sigma = (\Psi, \cdots, \text{Cookies}, \cdots) \\
\Psi = \Psi' :: \text{website.cookieSet}(\kappa, \text{id}_{cb}, (\text{name}, \text{value}, \text{url})) \quad \text{Cookie} \in \text{Cookies} \\
\text{Cookie} = (\text{name}, \text{value}_1, \text{url}, \kappa) \quad \text{Cookie}' = \text{Cookie}[\text{value}_1 \Leftarrow \text{value}] \\
\text{Cookies}' = \text{Cookies}[\text{Cookie} \Leftarrow \text{Cookie}'] \quad \Sigma' = \Sigma[\Psi \Leftarrow \Psi'][\text{Cookies} \Leftarrow \text{Cookies}'] \\
\text{fresh}(\text{id}_e) \quad e = (\text{id}_e, \text{id}_{cb}, \text{none}, \text{info}(\text{Cookie}', \kappa)) \\
\text{CookieWebsiteSet}(1) \\
\text{nextStateC}(\Sigma', \text{website.cookieSet}(\kappa, \text{id}_{cb}, (\text{name}, \text{value}, \text{url}))) = \Sigma'; e \\
\]

Let \( \Sigma_1 = (\Psi_1, \text{Tabs}_1, \text{ExtCoreRs}_1, \text{progInjCSs}_1, \text{Extss}_1, \text{Cookies}_1, M\text{bookmarks}_1, \text{histories}_1, \text{UI}_1) \)
\( \Sigma_2 = (\Psi_2, \text{Tabs}_2, \text{ExtCoreRs}_2, \text{progInjCSs}_2, \text{Extss}_2, \text{Cookies}_2, M\text{bookmarks}_2, \text{histories}_2, \text{UI}_2) \)

By assumptions
(A1) \( \Psi_1 = \Psi'_1 :: \psi_1 \)
(A2) \( \psi_1 = \text{website.cookieSet}(\kappa_1, \text{id}_{cb}, (\text{name}, \text{value}, \text{url})) \)
(A3) \( \text{Cookie}_1 \in \text{Cookies}_1 \)
(A4) \( \text{Cookie}_1 = (\text{name}, \text{value}_1, \text{url}, \kappa_1) \)
(A5) \( \text{Cookie}'_1 = \text{Cookie}_1[\text{value}_1 \Leftarrow \text{value}] \)
(A6) \( \text{Cookies}'_1 = \text{Cookies}_1[\text{Cookie}_1 \Leftarrow \text{Cookie}'_1] \)
(A7) \( \text{fresh}(\text{id}_{e_1}) \)
(A8) \( e_1 = (\text{id}_{e_1}, \text{id}_{cb}, \text{none}, \text{info}(\text{Cookie}'_1), \kappa) \)
(A9) \( \Sigma'_1 = \Sigma_1[\Psi_1 \Leftarrow \Psi'_1][\text{Cookies}_1 \Leftarrow \text{Cookies}'_1] \)

sub-subcase i. \( \kappa_1 \not\subseteq \kappa \)

By BROWSERSTATE1
(1) \( \psi_1 \downarrow_{\kappa} = \psi_1 \)
By $\Sigma_1 \downarrow_{\kappa} \leq \Sigma_2 \downarrow_{\kappa}$, Lemma 11, and (1)

(2) $\Psi_1 \downarrow_{\kappa} \leq_c \Psi_2 \downarrow_{\kappa}$

(3) $\exists \psi_2 \in \Psi_2 \downarrow_{\kappa}$ s.t. $\psi_1 \downarrow_{\kappa} \leq \psi_2 \downarrow_{\kappa}$,

that is $\psi_2 = \psi_1 = \text{website.cookieSet}((\kappa_1, id, c, (\text{name}, \text{value}, \text{url})))$,

$\Psi_2 = \Psi_2' \bowtie \psi_2, \Psi_1 \downarrow_{\kappa} \leq_c \Psi_2' \downarrow_{\kappa}$

By \text{COOKIE 1}

(4) $\text{Cookie}_1 \downarrow_{\kappa} = \text{Cookie}_1$

By $\text{COOKIES}_1 \downarrow_{\kappa} \leq \text{COOKIES}_2 \downarrow_{\kappa}$, (4)

(5) $\exists \text{COOKIES}_2 \in \text{COOKIES}_2 \downarrow_{\kappa}$ s.t. $\text{Cookie}_1 \downarrow_{\kappa} \leq \text{COOKIES}_2 \downarrow_{\kappa}$,

that is $\text{COOKIES}_2 = \text{COOKIES}_1 = (\text{name}, \text{value}_1, \text{url}, \kappa_1)$

By (3), (5), apply \text{COOKIE\_WEBSITE\_SET(1)} to $\Sigma_2$

(6) $\text{Cookie}_2' = \text{COOKIES}_2[\text{value}_1 \leftarrow \text{value}]$

(7) $\text{COOKIES}_2' = \text{COOKIES}_2[\text{Cookie}_2 \leftarrow \text{Cookie}_2']$

(8) fresh(id$_{c_2}$)

(9) $c_2 = (id_{c_2}, id_c, \text{none, info}($Cookie$_2'), \kappa_1)$

(10) $\Sigma_2' = \Sigma_2[\Psi_1 \leftarrow \Psi_1'][\text{COOKIES}_1 \leftarrow \text{COOKIES}_1']$

By (5), (6)

(11) $\text{COOKIES}_2' = \text{COOKIES}_1'$

By (A6), (7), Lemma 6

(12) $\text{COOKIES}_2' = \text{COOKIES}_1'$

By \text{STATE}, (A9), (3), (10), (12)

(13) $\Sigma_1' \downarrow_{\kappa} \leq \Sigma_2' \downarrow_{\kappa}$

By \text{EVENT 1}, (A8), (9), (11)

(14) $e_1 \downarrow_{\kappa} \leq e_2 \downarrow_{\kappa}$

\text{sub-case ii.} $\kappa_1 \not\subseteq \kappa$

By \text{BROWSER\_STATE 2}, Lemma 12

(1) $\psi_1 \downarrow_{\kappa} = \cdot$

(2) $\Psi_1 \downarrow_{\kappa} \leq_c \Psi_1 \downarrow_{\kappa}$

By \text{COOKIE 2}, (A4), (A5)

(3) $\text{Cookie}_1 \downarrow_{\kappa} = \text{Cookie}_1' \downarrow_{\kappa}$

By (A6), Lemma 6

(4) $\text{COOKIES}_1' = \text{COOKIES}_1$

By \text{STATE}, (A9), (3), (4)

(5) $\Sigma_1' \downarrow_{\kappa} \leq \Sigma_1 \downarrow_{\kappa}$

By (A8) \text{, EVENT 2}

(6) $e_1 \downarrow_{\kappa} = \cdot$

The proofs for \text{COOKIE\_WEBSITE\_SET(2), COOKIE\_SCRIPT\_SET(1)} are similar to the proofs for \text{COOKIE\_WEBSITE\_SET(1)}.

\text{case: COOKIE\_CORE\_GET\_ALL}

Let $\Sigma_1 = (\Psi_1, \text{Tabs}_1, \text{ExtCoreRs}_1, \text{progInjCSs}_1, \text{Exts}_1, \text{Cookies}_1, \text{MBookmarks}_1, \text{histories}_1, \text{UI}_1)$

$\Sigma_2 = (\Psi_2, \text{Tabs}_2, \text{ExtCoreRs}_2, \text{progInjCSs}_2, \text{Exts}_2, \text{Cookies}_2, \text{MBookmarks}_2, \text{histories}_2, \text{UI}_2)$

By assumptions

(A1) $\Psi_1 = \Psi_1' \bowtie \psi_1$

(A2) $\psi_1 = \text{chrome.cookies.getAll}(\kappa_1, id_{c_2}, \text{filter})$

(A3) $\forall \text{Cookie} \in \text{Cookies}_1$, $\text{Cookie} = (\cdot \cdots, \kappa_c)$

if matchFilter($\text{Cookie}, \text{filter}$) = true \wedge $\kappa_c \subseteq \kappa_1$

Add $\text{Cookie}$ to $\text{Cookies}_{\text{results}}$
(A4) \( fresh(id_{c1}) \)
\( e_1 = (id_{c1}, id_{cb}, none, Cookies_{\text{results}}, \kappa_1) \)

(A5) \( \Sigma'_1 = \Sigma_1[\Psi_1 \leftarrow \Psi'_1] \)

**sub-subcase i. \( \kappa_1 \subseteq \kappa \)**

By **BROWSERSTATE1**

(1) \( \psi_1 \downarrow_\kappa = \psi_1 \)

By \( \Sigma_1 \downarrow_\kappa \leq \Sigma_2 \downarrow_\kappa \), Lemma 11, and (1)

(2) \( \Psi_1 \downarrow_\kappa \leq \Psi_2 \downarrow_\kappa \)

(3) \( \exists \psi_2 \in \Psi_2 \) s.t. \( \psi_1 \downarrow_\kappa \leq \psi_2 \downarrow_\kappa \),
that is \( \psi_2 = \psi_1 = \text{chrome.cookies.getAll}(\kappa_1, id_{cb}, \text{filter}) \),
\( \Psi_2 = \Psi'_2 :: \psi_2, \Psi'_2 \downarrow_\kappa \leq \kappa \)

By **COOKIE1**, \( Cookies_1 \downarrow_\kappa \leq Cookies_2 \downarrow_\kappa \)

(4) \( \forall \text{Cookie} \in \text{Cookie}_{\text{results}}, \text{Cookie} \downarrow_\kappa = \text{Cookie} \)
\( \exists \text{Cookie}' \in \text{Cookies}_2 \) s.t. \( \text{Cookie} \downarrow_\kappa \leq \text{Cookie}' \downarrow_\kappa \),
that is \( \text{Cookie}' = \text{Cookie} \)

By (3), apply **COOKIECOREGETALL(2)** to \( \Sigma_2 \)

(5) \( \forall \text{Cookie} \in \text{Cookies}_2, \text{Cookie} = (\ldots, \kappa_\alpha) \)
if \( \text{matchFilter}(\text{Cookie}, \text{filter}) = \text{true} \wedge \kappa_\alpha \not\subseteq \kappa_1 \)
Add **Cookie** to **Cookies_{results2}**

(6) \( fresh(id_{c2}) \)
\( e_2 = (id_{c2}, id_{cb}, none, Cookies_{\text{results}2}, \kappa_1) \)

(7) \( \Sigma'_2 = \Sigma_2[\Psi_2 \leftarrow \Psi'_2] \)

By (A4), (3), (6)

(8) \( e_1 \downarrow_\kappa \leq e_2 \downarrow_\kappa \)

By **STATE**, (A5), (3)

(9) \( \Sigma'_1 \downarrow_\kappa \leq \Sigma'_2 \downarrow_\kappa \)

**sub-subcase ii. \( \kappa_1 \not\subseteq \kappa \)**

By **BROWSERSTATE2**, Lemma 12

(1) \( \psi_1 \downarrow_\kappa = \cdot \)

(2) \( \Psi'_1 \downarrow_\kappa \leq \Psi_1 \downarrow_\kappa \)

By **STATE**, (A5), (2)

(3) \( \Sigma'_1 \downarrow_\kappa \leq \Sigma_1 \downarrow_\kappa \)

By (A4), **EVENT2**

(4) \( e_1 \downarrow_\kappa = \cdot \)

**case: COOKIECOREREMOVE(1)**

**CookieCoreRemove(1)**  Extension core removes a cookie with name and url. The callback function can access the removed cookie.

\[
\Sigma = (\Psi, \ldots, Cookies, \ldots) \quad \Psi = \Psi' :: \text{chrome.cookies.remove}(\kappa, id_{cb}, (\text{name}, \text{url}))
\]

Cookies = Cookies' :: Cookie

Cookie = (name, url, \kappa_c) \quad \kappa \not\subseteq \kappa_c \quad \Sigma' = \Sigma[\Psi \leftarrow \Psi'][\text{Cookies} \leftarrow \text{Cookies}']

\( fresh(id_e) \) \( e = (id_e, id_{cb}, none, \text{Cookie}, \kappa_e) \)

\[\text{nextStateC}(\Sigma, \text{chrome.cookies.remove}(\kappa, id_{cb}, (\text{name}, \text{url}))) = \Sigma'; e \]

CookieCoreRemove(1)

Let \( \Sigma_1 = (\Psi_1, Tabs_1, ExtCoreRs_1, progInjCSs_1, Extz_1, Cookies_1, MBookmarks_1, \text{histories}_1, UI_1) \)
\( \Sigma_2 = (\Psi_2, Tabs_2, ExtCoreRs_2, progInjCSs_2, Extz_2, Cookies_2, MBookmarks_2, \text{histories}_2, UI_2) \)

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By assumptions
(A1) \( \Psi_1 = \Psi'_1 \::= \psi_1 \)
(A2) \( \psi_1 = \text{chrome.cookies.remove}(\kappa_1, \text{id}_c, (\text{name}, \text{url})) \)
(A3) \( \text{Cookies}_1 = \text{Cookies}'_1 \::= \text{Cookie}_1 \)
(A4) \( \text{Cookie}_1 = (\text{name}, \cdot, \text{url}, \kappa_c) \)
(A5) \( \kappa_1 \subseteq \kappa \)
(A6) \( \Sigma'_1 = \Sigma_1[\Psi_1 \Leftarrow \Psi'_1][\text{Cookies}_1 \Leftarrow \text{Cookies}'_1] \)
(A7) \( \text{fresh}(\text{id}_c) \)
(A8) \( e_1 = (\text{id}_c, \text{id}_e, \text{none}, \text{Cookie}_1, \kappa_c) \)

sub-subcase i. \( \kappa_1 \subseteq \kappa \)

By BROWSERSTATE1

(1) \( \psi_1 \downarrow_{\kappa} = \psi_1 \)
(2) \( \Sigma_1 \downarrow_{\kappa} \leq \Sigma_2 \downarrow_{\kappa} \), Lemma 11, and (1)
(3) \( \exists \psi_2 \in \Psi_2 \) s.t. \( \psi_1 \downarrow_{\kappa} \leq \psi_2 \downarrow_{\kappa} \),
that is \( \psi_2 = \psi_1 = \text{chrome.cookies.remove}(\kappa_1, \text{id}_c, (\text{name}, \text{url})) \),
\( \Psi_2 = \Psi'_2 :: \psi_2, \Psi'_1 \downarrow_{\kappa} \leq \Psi'_2 \downarrow_{\kappa} \)
case 1: \( \kappa_c \leq \kappa \)

By COOKIE1. \( \text{Cookies}_1 \downarrow_{\kappa} \leq \text{Cookies}_2 \downarrow_{\kappa} \)
(4) \( \exists \text{Cookie}_2 \in \text{Cookies}_2 \) s.t. \( \text{Cookie}_1 \downarrow_{\kappa} \leq \text{Cookie}_2 \downarrow_{\kappa} \),
that is \( \text{Cookie}_1 = \text{Cookie}_2 \)
(5) \( \text{Cookies}_2 = \text{Cookies}'_2 :: \text{Cookie}_2 \)
(6) \( \text{Cookies}'_1 \downarrow_{\kappa} \leq \text{Cookies}'_2 \downarrow_{\kappa} \)

By (3), (4), apply COOKIECOREREMOVE(1) to \( \Sigma_2 \)
(7) \( \text{Cookies}_2 = \text{Cookies}'_2 :: \text{Cookie}_2 \)
(8) \( \Sigma'_2 = \Sigma_2[\Psi_2 \Leftarrow \Psi'_2][\text{Cookies}_2 \Leftarrow \text{Cookies}'_2] \)
(9) \( \text{fresh}(\text{id}_e) \)
(10) \( e_2 = (\text{id}_e, \text{id}_c, \text{none}, \text{Cookie}_2, \kappa_c) \)

By (A8), (4), (10)
(11) \( e_1 \downarrow_{\kappa} \leq e_2 \downarrow_{\kappa} \)

By STATE, (A6), (3), (6), (8)
(12) \( \Sigma'_1 \downarrow_{\kappa} \leq \Sigma'_2 \downarrow_{\kappa} \)

case 2: \( \kappa_c \not\leq \kappa \)

By COOKIE2.
(13) \( \text{Cookie}_1 \downarrow_{\kappa} = \cdot \)
(14) \( \text{Cookies}'_1 \downarrow_{\kappa} = \text{Cookies}_1 \downarrow_{\kappa} \)

By STATE, (A6), (3), (14)
(15) \( \Sigma'_1 \downarrow_{\kappa} \leq \Sigma_1 \downarrow_{\kappa} \)

By (A8), EVENT2
(16) \( e_1 \downarrow_{\kappa} = \cdot \)

sub-subcase ii. \( \kappa_1 \not\leq \kappa \)

By BROWSERSTATE2, Lemma 12
(1) \( \psi_1 \downarrow_{\kappa} = \cdot \)
(2) \( \Psi'_1 \downarrow_{\kappa} \leq \psi_1 \downarrow_{\kappa} \)

By \( \kappa_1 \not\subseteq \kappa \), (A5)
(3) \( \kappa_c \not\subseteq \kappa \)

By (3), COOKIE2.
(5) \( \text{Cookie}_1 \downarrow_{\kappa} = \cdot \)
(6) \( \text{Cookies}_1 \downarrow \kappa \leq \text{Cookies}_1 \downarrow \kappa \)

By \text{state}, (A6), (2), (6)

(7) \( \Sigma'_1 \downarrow \kappa \leq \Sigma_1 \downarrow \kappa \)

By (A8), (3), \text{EVENT2}

(8) \( e_1 \downarrow \kappa = \cdot \)

case: \text{HistorySearch}

\[ \Sigma = (\Psi, \cdots, \text{histories}, \cdots) \]

\[ \Psi = \Psi' :: \text{chrome.history.search}(\kappa, \text{id}_c, \text{query}) \quad \text{histories} = \text{histories}_1 :: \text{histories}_2 \]

\( \forall \text{history} \in \text{histories}_1, \text{history} = (\text{id}, \text{url}, \text{name}, \text{visitTime}, \text{visitType}, \kappa_h) \)

\[ \text{matchQuery(history, query)} = \text{true} \]

\[ \kappa_h \subseteq \kappa \]

\[ \exists \text{history}' \in \text{histories}, \text{history}' = (\text{id}', \text{url}, \text{name}, \text{visitTime}', \text{visitType}', \kappa'_h), \text{history}' \neq \text{history} \]

s.t. \( \text{visitTime}' \) is later than \( \text{visitTime} \wedge \kappa'_h \subseteq \kappa \)

\( \forall \text{history} \in \text{histories}_2, \text{history} = (\text{id}, \text{url}, \text{name}, \text{visitTime}, \text{visitType}, \kappa_h) \)

\[ \text{matchQuery(history, query)} = \text{true} \]

\[ \kappa_h \subseteq \kappa \]

\[ \exists \text{history}' \in \text{histories}_1, \text{history}' = (\text{id}', \text{url}, \text{name}, \text{visitTime}', \text{visitType}', \kappa'_h), \]

s.t. \( \text{visitTime}' \) is later than \( \text{visitTime} \wedge \kappa'_h \subseteq \kappa \)

\[ \Sigma' = \Sigma[\Psi \leftarrow \Psi'] \quad \text{fresh}(\text{id}_e) \quad e = (\text{id}_e, \text{id}_c, \text{none}, \text{histories}_1, \kappa) \]

\[ \text{nextStateC}(\Sigma, \text{chrome.history.search}(\kappa, \text{id}_c, \text{query})) = \Sigma'; e \]

Let \( \Sigma_1 = (\Psi_1, \text{Tabs}_1, \text{ExtCoreRs}_1, \text{proglInjCSs}_1, \text{Exts}_1, \text{Cookies}_1, \text{MBookmarks}_1, \text{histories}_1, \text{UI}_1) \)

\( \Sigma_2 = (\Psi_2, \text{Tabs}_2, \text{ExtCoreRs}_2, \text{proglInjCSs}_2, \text{Exts}_2, \text{Cookies}_2, \text{MBookmarks}_2, \text{histories}_2, \text{UI}_2) \)

By assumptions

(A1) \( \Psi_1 = \Psi'_1 :: \psi_1 \)

(A2) \( \psi_1 = \text{chrome.history.search}(\kappa_1, \text{id}_c, \text{query}) \)

(A3) \( \text{histories}_1 = \text{histories}_{1a} :: \text{histories}_{1b} \)

(A4) \( \forall \text{history} \in \text{histories}_{1a}, \text{history} = (\text{id}, \text{url}, \text{name}, \text{visitTime}, \text{visitType}, \kappa_h) \)

\[ \text{matchQuery(history, query)} = \text{true} \]

\[ \kappa_h \subseteq \kappa \]

\[ \exists \text{history}' \in \text{histories}_1, \text{history}' = (\text{id}', \text{url}, \text{name}, \text{visitTime}', \text{visitType}', \kappa'_h), \text{history}' \neq \text{history} \]

s.t. \( \text{visitTime}' \) is later than \( \text{visitTime} \wedge \kappa'_h \subseteq \kappa \)

(A5) \( \forall \text{history} \in \text{histories}_{1b}, \text{history} = (\text{id}, \text{url}, \text{name}, \text{visitTime}, \text{visitType}, \kappa_h) \)

\[ \text{matchQuery(history, query)} = \text{true} \]

\[ \kappa_h \subseteq \kappa \]

\[ \exists \text{history}' \in \text{histories}_{1a}, \text{history}' = (\text{id}', \text{url}, \text{name}, \text{visitTime}', \text{visitType}', \kappa'_h), \]

s.t. \( \text{visitTime}' \) is later than \( \text{visitTime} \wedge \kappa'_h \subseteq \kappa \)

(A6) \( \Sigma'_1 = \Sigma_1[\Psi_1 \leftarrow \Psi'_1] \)

(A7) \( \text{fresh}(\text{id}_e_1), e_1 = (\text{id}_e_1, \text{id}_c, \text{none}, \text{histories}_{1a}, \kappa_1) \)

sub-subcase i. \( \kappa_1 \subseteq \kappa \)

By \text{BROWSERSTATE1}

(1) \( \psi_1 \downarrow \kappa = \psi_1 \)

By \( \Sigma_1 \downarrow \kappa \leq \Sigma_2 \downarrow \kappa \), Lemma 11, and (1)

(2) \( \Psi_1 \downarrow \kappa \leq \Sigma_2 \downarrow \kappa \)

(3) \( \exists \psi_2 \in \Psi_2 \text{ s.t. } \psi_1 \downarrow \kappa \leq \psi_2 \downarrow \kappa \),

that is \( \psi_2 = \psi_1 = \text{chrome.history.search}(\kappa_1, \text{id}_c, \text{query}) \)
\[ \Psi_2 = \Psi'_2 :: \psi_1 \downarrow \kappa \leq c \Psi_1 \downarrow \kappa \]

By (3), HISTORY1

(4) \( \forall \text{history} \in \text{histories}_1 \), s.t., matchQuery(history, query) = true,

\[
\text{labOf(history)} \sqsubseteq \kappa_1 \sqsubseteq \kappa \\
\text{history} \downarrow \kappa = \text{history} \\
\text{history} \in \text{histories}_1 \downarrow \kappa
\]

(5) \( \forall \text{history}' \in \text{histories}_2 \), s.t., matchQuery(history', query) = true,

\[
\text{labOf(history')} \sqsubseteq \kappa_1 \sqsubseteq \kappa \\
\text{history'} \downarrow \kappa = \text{history'} \\
\text{history'} \in \text{histories}_2 \downarrow \kappa
\]

By (4), (5), \( \text{histories}_1 \downarrow \kappa \leq \text{hstrs} \), \( \text{histories}_2 \downarrow \kappa \), HISTORY2

(6) \( \text{histories}_1 \downarrow \kappa = \text{histories}_2 \downarrow \kappa \)

By (3), apply HISTORYSEARCH to \( \Sigma_2 \)

(7) \( \text{histories}_2 = \text{histories}_{2a} :: \text{histories}_{2b} \)

(8) \( \forall \text{history} \in \text{histories}_{2a} \), history = (id, url, name, visitTime, visitType, \( \kappa_h \))

matchQuery(history, query) = true

\[
\kappa_h \sqsubseteq \kappa_1 \\
\exists \text{history}' \in \text{histories}_1, \text{history}' = (id', url, name, visitTime', visitType', \kappa'_h, \kappa'), \text{history'} \neq \text{history} \\
\text{s.t. visitTime'} is later than visitTime \wedge \kappa'_h \sqsubseteq \kappa
\]

(9) \( \forall \text{history} \in \text{histories}_{2b} \), history = (id, url, name, visitTime, visitType, \( \kappa_h \))

matchQuery(history, query) = true

\[
\kappa_h \sqsubseteq \kappa \\
\exists \text{history}' \in \text{histories}_{2a}, \text{history}' = (id', url, name, visitTime', visitType', \kappa'_h), \text{s.t. visitTime'} is later than visitTime \wedge \kappa'_h \sqsubseteq \kappa_1
\]

(10) \( \Sigma'_2 = \Sigma_2[\Psi_2 \leftarrow \Psi'_2] \)

(11) \( \text{fresh}(id_{e2}), e_2 = (id_{e2}, id_{cb}, \text{none}, \text{histories}_{2a}, \kappa_1) \)

By (A4), (A5), (8), (4), (5), and (6)

(12) \( \text{histories}_{1a} = \text{histories}_{2a} \)

By STATE, (A6), (10) and (3)

(13) \( \Sigma_1 \downarrow \kappa \leq \Sigma'_2 \downarrow \kappa \)

By (A7), (11), (12)

(14) \( e_1 \downarrow \kappa \leq e_2 \downarrow \kappa \)

\subsection{sub-subcase ii.} \( \kappa_1 \not\leq \kappa \)

By BROWSERSTATE2, Lemma 12

(1) \( \psi'_1 \downarrow \kappa = \cdot \)

(2) \( \Psi'_1 \downarrow \kappa \leq c \psi_1 \downarrow \kappa \)

By STATE, (A6), and (2)

(3) \( \Sigma' \downarrow \kappa \leq \Sigma_1 \downarrow \kappa \)

By (A7), EVENT2

(4) \( e_1 \downarrow \kappa = \cdot \)

The proofs for HISTORYGETVISITS are similar to the proofs for this rule.

\textbf{case: HISTORYADDURL}
\[ \Sigma = (\Psi, \ldots, \text{histories}, \ldots) \]

\[ \Psi = \Psi' :: \text{chrome.history.addUrl}(\kappa, \text{id}_{cb}, \text{name}, \text{url}, \text{visitTime}, \text{visitType}) \]

\[ \text{histories}' = \text{histories} :: \text{history} \]

\[ \text{fresh}(\text{id}) = \text{history} = (\text{id}, \text{url}, \text{name}, \text{visitTime}, \text{visitType}, \kappa) \]

\[ \Sigma' = \Sigma[\Psi \leftarrow \Psi'[\text{histories} \leftarrow \text{histories}'] \quad \text{fresh}(\text{id}_e) \quad e = (\text{id}_e, \text{id}_{cb}, \text{none}, \text{history}, \kappa) \]

\[ \text{nextStateC}(\Sigma, \text{chrome.history.addUrl}(\kappa, \text{id}_{cb}, \text{name}, \text{url}, \text{visitTime}, \text{visitType})) = \Sigma'; e \]

Let \( \Sigma_1 = (\Psi_1, \text{Tabs}_1, \text{ExtCoreRs}_1, \text{progInjCSs}_1, \text{Exts}_1, \text{Cookies}_1, \text{MBookmarks}_1, \text{histories}_1, \text{UI}_1) \)

\[ \Sigma_2 = (\Psi_2, \text{Tabs}_2, \text{ExtCoreRs}_2, \text{progInjCSs}_2, \text{Exts}_2, \text{Cookies}_2, \text{MBookmarks}_2, \text{histories}_2, \text{UI}_2) \]

By assumptions

(A1) \( \Psi_1 = \Psi_1' :: \psi_1 \)

(A2) \( \psi_1 = \text{chrome.history.addUrl}(\kappa_1, \text{id}_{cb}, \text{name}, \text{url}, \text{visitTime}, \text{visitType}) \)

(A3) \( \text{fresh}(\text{id}_1), \text{history}_1 = (\text{id}_1, \text{url}, \text{name}, \text{visitTime}, \text{visitType}, \kappa_1) \)

(A4) \( \text{histories}'_1 = \text{histories} :: \text{history}_1 \)

(A5) \( \Sigma'[1][\Psi_1 \leftarrow \Psi_1'[\text{histories} \leftarrow \text{histories}'_1] \)

(A6) \( \text{fresh}(\text{id}_{e_1}), e_1 = (\text{id}_{e_1}, \text{id}_{cb}, \text{none}, \text{history}_1, \kappa_1) \)

\textbf{sub-subcase i.} \( \kappa_1 \subseteq \kappa \)

By BROWSERSTATE1

(1) \( \psi_1 \downarrow_\kappa = \psi_1 \)

By \( \Sigma_1 \downarrow_\kappa \leq \Sigma_2 \downarrow_\kappa \), Lemma 11, and (1)

(2) \( \Psi_1 \downarrow_\kappa \leq \Psi_2 \downarrow_\kappa \)

(3) \( \exists \psi_2 \in \Psi_2 \text{ s.t. } \psi_1 \downarrow_\kappa \leq \psi_2 \downarrow_\kappa \),

that is \( \psi_2 = \psi_1 = \text{chrome.history.addUrl}(\kappa_1, \text{id}_{cb}, \text{name}, \text{url}, \text{visitTime}, \text{visitType}) \),

\( \Psi_2 = \Psi_2' :: \psi_2, \psi_1' \downarrow_\kappa \leq \psi_2 \downarrow_\kappa \)

By (A3), BROWSERSTATE1

(4) \( \text{history}_1 \downarrow_\kappa = \text{history}_1 \)

Apply HISTORYADDURL to \( \Sigma_2 \)

(5) \( \text{fresh}(\text{id}_2), \text{history}_2 = (\text{id}_2, \text{url}, \text{name}, \text{visitTime}, \text{visitType}, \kappa_1) \)

(6) \( \text{histories}'_2 = \text{histories} :: \text{history}_2 \)

(7) \( \Sigma_2' = \Sigma_2[\Psi_2 \leftarrow \Psi_2'[\text{histories} \leftarrow \text{histories}'_2] \)

(8) \( \text{fresh}(\text{id}_{e_2}), e_2 = (\text{id}_{e_2}, \text{id}_{cb}, \text{none}, \text{history}_2, \kappa_1) \)

By (A3), (5), (A4), (6), \( \text{histories}_1 \downarrow_\kappa \leq \text{histories}_2 \downarrow_\kappa \)

(9) \( \text{history}_1 = \text{history}_2 \)

(10) \( \text{histories}'_1 \leq \text{histories}'_2 \)

By STATE, (A5), (7), (3), and (10)

(11) \( \Sigma_1' \downarrow_\kappa \leq \Sigma_2' \downarrow_\kappa \)

By (A6), (8), (9), EVENT1

(12) \( e_1 \downarrow_\kappa \leq e_2 \downarrow_\kappa \)

\textbf{sub-subcase ii.} \( \kappa_1 \not\subseteq \kappa \)

By BROWSERSTATE2, Lemma 12

(1) \( \psi_1' \downarrow_\kappa = \cdot \)

(2) \( \Psi_1' \downarrow_\kappa \leq \psi_1' \downarrow_\kappa \)

By HISTORY2

(3) \( \text{history}_1' \downarrow_\kappa = \cdot \)

(4) \( \text{histories}'_1 \downarrow_\kappa \leq \text{histories}_1 \downarrow_\kappa \)

By STATE, (A5), (2), and (4)

(5) \( \Sigma_1' \downarrow_\kappa \leq \Sigma_1 \downarrow_\kappa \)
By (A6), EVENT
(6)  \( e_1 \downarrow_{\kappa} = \cdot \)

case: HISTORYDELETEURL

\[ \Sigma = (\Psi, \cdots, \text{histories}, \cdots) \]
\[ \Psi = \Psi' :: \text{chrome.history.deleteUrl}(\kappa, id_{cb}, url) \]
\[ \text{histories} = \text{histories}_1 :: \text{histories}_2 \]
\[ \forall \text{history} \in \text{histories}_1 \]
\[ \text{history} = (\cdot, \text{url}, \cdot, \cdot, \cdot, \cdot, \cdot, \kappa_h) \]
\[ \kappa \subseteq \kappa_h \]
\[[\text{history} \in \text{histories}_2, \text{s.t.} \text{history} = (\cdot, \text{url}, \cdot, \cdot, \cdot, \cdot, \kappa_h) \land \kappa \subseteq \kappa_h \]
\[ \Sigma' = \Sigma[\Psi \leftarrow \Psi'][\text{histories} \leftarrow \text{histories}_2] \]
\[ e = (id_{ec}, id_{cb}, \text{none}, \text{void}, \kappa) \]

\[ \text{nextStateC}(\Sigma', \text{chrome.history.deleteUrl}(\kappa, id_{cb}, url)) = \Sigma'; e \]

Let \( \Sigma_1 = (\Psi_1, \text{Tabs}_1, \text{ExtCoreRs}_1, \text{progInjCSs}_1, \text{Exts}_1, \text{Cookies}_1, \text{MBookmarks}_1, \text{histories}_1, \text{UI}_1) \)
\[ \Sigma_2 = (\Psi_2, \text{Tabs}_2, \text{ExtCoreRs}_2, \text{progInjCSs}_2, \text{Exts}_2, \text{Cookies}_2, \text{MBookmarks}_2, \text{histories}_2, \text{UI}_2) \]

By assumptions
(A1)  \( \Psi_1 = \Psi'_1 :: \psi_1 \)
(A2)  \( \psi_1 = \text{chrome.history.deleteUrl}(\kappa_1, id_{cb}, url) \)
(A3)  \( \text{histories}_1 = \text{histories}_{1a} :: \text{histories}_{1b} \)
(A4)  \( \forall \text{history} \in \text{histories}_{1a} \]
\[ \text{history} = (\cdot, \text{url}, \cdot, \cdot, \cdot, \cdot, \kappa_h) \]
\[ \kappa_1 \subseteq \kappa_h \]
(A5)  \[ \exists \text{history} \in \text{histories}_{1b}, \text{s.t.} \text{history} = (\cdot, \text{url}, \cdot, \cdot, \cdot, \cdot, \kappa_h) \land \kappa_1 \subseteq \kappa_h \]
(A6)  \[ \Sigma'_2 = \Sigma_1[\Psi_1 \leftarrow \Psi'_1][\text{histories}_1 \leftarrow \text{histories}_{1b}] \]
(A7)  \( \text{fresh}(id_{ec}), e_1 = (id_{ec}, id_{cb}, \text{none}, \text{void}, \kappa_1) \)

sub-case i. \( \kappa_1 \subseteq \kappa \)

By BROWSERSTATE1
(1)  \( \psi_1 \downarrow_{\kappa} = \psi_1 \)

By \( \Sigma_1 \downarrow_{\kappa} \preceq \Sigma_2 \downarrow_{\kappa} \), Lemma 11, and (1)
(2)  \( \Psi_1 \downarrow_{\kappa} \preceq \Psi_2 \downarrow_{\kappa} \)
(3)  \[ \exists \psi_2 \in \Psi_2 \text{s.t.} \psi_1 \downarrow_{\kappa} \preceq \psi_2 \downarrow_{\kappa}, \]
\[ \text{that is} \psi_2 = \psi_1 = \text{chrome.history.deleteUrl}(\kappa_1, id_{cb}, url), \]
\[ \Psi_2 = \Psi'_2 :: \psi_2, \Psi'_1 \downarrow_{\kappa} \preceq \Psi'_2 \downarrow_{\kappa} \]

Apply HISTORYDELETEURL to \( \Sigma_2 \)
(4)  \( \text{histories}_2 = \text{histories}_{2a} :: \text{histories}_{2b} \)
(5)  \( \forall \text{history} \in \text{histories}_{2a} \]
\[ \text{history} = (\cdot, \text{url}, \cdot, \cdot, \cdot, \cdot, \kappa_h) \]
\[ \kappa_1 \subseteq \kappa_h \]
(6)  \[ \exists \text{history} \in \text{histories}_{2b}, \text{s.t.} \text{history} = (\cdot, \text{url}, \cdot, \cdot, \cdot, \cdot, \kappa_h) \land \kappa_1 \subseteq \kappa_h \]
(7)  \[ \Sigma'_2 = \Sigma_2[\Psi_2 \leftarrow \Psi'_2][\text{histories}_2 \leftarrow \text{histories}_{2b}] \]
(8)  \( \text{fresh}(id_{ec}), e_2 = (id_{ec}, id_{cb}, \text{none}, \text{void}, \kappa_1) \)

By (A4), (5), HISTORY1, HISTORY2, \( \text{histories}_1 \downarrow_{\kappa} \preceq \text{histories}_2 \downarrow_{\kappa} \)
(9)  \( \text{histories}_1 \downarrow_{\kappa} = \text{histories}_2 \downarrow_{\kappa} \)
(10)  \( \forall \text{history} \in \text{histories}_{1a}, \text{s.t.} \text{labOf}(\text{history}) \subseteq \kappa \]
\[ \exists \text{history'} \in \text{histories}_{2a}, \text{s.t.} \text{history'} \downarrow_{\kappa} = \text{history'} \downarrow_{\kappa} \]
(11)  \( \forall \text{history} \in \text{histories}_{2a}, \text{s.t.} \text{labOf}(\text{history}) \subseteq \kappa \)

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∃history' ∈ histories_{1a}, s.t. history ↓κ = history' ↓κ

(12) histories_{1a} ↓κ = histories_{2a} ↓κ
(13) histories_{1b} ↓κ = histories_{2b} ↓κ
(14) histories_{1b} ↓κ ≤ histories_{2b} ↓κ

By STATE, (A6), (7), (3), and (14)
(11) Σ'_1 ↓κ ≤ Σ'_2 ↓κ

By (A7), (8), EVENT1
(12) e_1 ↓κ ≤ e_2 ↓κ

sub-subcase ii. κ_1 ⊈ κ

By BROWSERSTATE2, Lemma 12
(1) ψ'_1 ↓κ = ·
(2) Ψ'_1 ↓κ ≤ e_1 ↓κ

By HISTORY2, HISTORIES
(3) history_{1a} ↓κ = ·
(4) histories_{1b} ↓κ ≤ histories_{1a} ↓κ

By STATE, (A6), (2), and (4)
(5) Σ'_1 ↓κ ≤ Σ'_2 ↓κ

By (A7), EVENT2
(6) e_1 ↓κ = ·

case: NewTab

fresh(id_1, id_d, id_e, id_e2) → Σ = (Ψ, Tabs, · · ·)
Ψ = Ψ' :: chrome.tabs.create(κ, id_e, (id_w, positionIndex, url, activeFlag, pinnedBoolean, id_parentTab))
t = (id_e, · · ·, url, · · ·, κ FC)
ψ' = readyToFetchDoc(id_1, id_d, · · ·, id_d, url)
Σ' = Σ[Ψ ⇐ Ψ' :: ψ'][Tabs ⇐ Tabs :: t] → E = (id_e1, tabs.onCreated, none, info_1, κ)
:: (id_e2, id_eb, none, getInfo(t), κ)

nextStateC(Σ, chrome.tabs.create(κ, id_eb, (id_w, positionIndex, url, activeFlag, pinnedBoolean, id_parentTab))) = Σ', E

Let Σ_1 = (Ψ_1, Tabs_1, ExtCoreRs_1, prohInjCSs_1, Ext_1, Cookies_1, MBookmarks_1, histories_1, UI_1)
Σ_2 = (Ψ_2, Tabs_2, ExtCoreRs_2, prohInjCSs_2, Ext_2, Cookies_2, MBookmarks_2, histories_2, UI_2)

By assumptions
(A1) fresh(id_1, id_d, id_e, id_e2)
(A2) Ψ_1 = Ψ'_1 ⇐ ψ_1
ψ_1 = chrome.tabs.create(κ_1, id_e, (id_w, positionIndex, url, activeFlag, pinnedBoolean, id_parentTab))
(A3) t_1 = (id_e, · · ·, url, · · ·, κ FC)
(A4) ψ'_1 = readyToFetchDoc(κ, id_e, id_d, · · ·, id_d, url)
(A5) Σ'_1 = Σ_1[Ψ_1 ⇐ Ψ'_1 :: ψ'_1][Tabs_1 ⇐ Tabs_1 :: t_1]
(A6) Ε'_1 = (id_e1, tabs.onCreated, none, info_1, κ_1) :: (id_e2, id_eb, none, getInfo(t), κ_1)

sub-subcase i. κ_1 ⊈ κ

By BROWSERSTATE1
(1) ψ_1 ↓κ = ψ_1, ψ_1 ∈ Ψ_1 ↓κ

By Ψ_1 ↓κ ≤ Ψ_2 ↓κ, (1)
(2) ∃ψ_2 ∈ Ψ_2 ↓κ, s.t. ψ_1 ↓κ ≤ ψ_2 ↓κ, namely ψ_2 = ψ_1

Apply NewTab to Σ_2
(3) ψ_2 = ψ_1 = chrome.tabs.create(κ_1, id_e, (id_w, positionIndex, url, activeFlag, pinnedBoolean, id_parentTab))
(4) fresh(id_1, id_d, id_e, id_e', id_e1, id_e2') = fresh(id_1, id_d, id_e1, id_e2)
(5) t_2 = (id_e1, · · ·, url, · · ·, κ_1) = t_1
By Lemma 11
(9) \( \Psi'_1 \downarrow \kappa \leq \kappa \Psi'_2 \downarrow \kappa \)

By (6), (9), (10)
(10) \( (\Psi'_1 \downarrow \kappa) \downarrow \kappa \leq (\Psi'_2 \downarrow \kappa) \downarrow \kappa \)

By (5), \( \Psi'_1 \downarrow \kappa \leq \Psi'_2 \downarrow \kappa \)

By (10), (11), (A5), (7), STATE
(12) \( \Psi'_1 \downarrow \kappa \leq \Psi'_2 \downarrow \kappa \)

By (8)
(13) \( \varepsilon'_1 \downarrow \kappa \leq \varepsilon'_2 \downarrow \kappa \)

sub-subcase ii. \( \kappa_1 \notin \kappa \)

By (A3), TAB3
(1) \( t_1 \downarrow \kappa = \cdot \)
(2) \( \Psi'_1 \downarrow \kappa \leq \Psi'_2 \downarrow \kappa \)

By (A2), (A4), Lemma 11, Lemma 10
(3) \( \Psi''_1 \downarrow \kappa \leq \kappa \Psi_1 \downarrow \kappa \)

By (2), (3), (A5), STATE
(4) \( \Psi''_1 \downarrow \kappa \leq \Psi_1 \downarrow \kappa \)

By (A6), EVENT2
(5) \( \varepsilon_1 \downarrow \kappa = \cdot \)

case: ENABLEDISABLEEXT1(A)

\( \Sigma = (\Psi, \Psi', \Psi'') \)

By assumptions
(A1) \( \text{Exts} = (id_{ext}, ExtCoreRs, \cdots) \)
(A2) \( \text{Exts} \in \Sigma \)
(A3) \( \Psi_1 \equiv \Psi''_1 \equiv \Psi' \)
(A5) \( \kappa_1 \not\subseteq \ell' \)
(A6) \( \Sigma'_1 = \Sigma [\Psi_1 \leftarrow \Psi''_1] \)
(A7) \( \varepsilon'_1 = \cdot \)

sub-subcase i. \( \kappa_1 \subseteq \kappa, \ell'_1^- \subseteq \kappa \)

By BROWSERSTATE1
(1) \( \Psi_1 \downarrow \kappa = \psi_1, \psi_1 \in \Psi_1 \downarrow \kappa \)

By (A1), \( \text{Exts} \equiv (id_{ext}, ExtCoreRs, Storage, \chi, activeFlag, \ell) \)

Let \( \Sigma_1 = (\Psi_1, Tabs_1, ExtCoreRs_1, progInjCSs_1, Exts_1, Cookies_1, MBookmarks_1, histories_1, UI_1) \)

By (A6), EVENT2
(5) \( \varepsilon'_1 \downarrow \kappa = \cdot \)

\( \text{nextStateC} (\Sigma, \text{chrome.management.setEnabled} (\kappa, id_{cb}, (\text{string}, id_{ext}, \text{activeFlag}))) = \Sigma [\Psi \leftarrow \Psi'] \)
(4) \( \exists \text{Ext}_2 \in \text{Ext}_{s_2} \)
\[ \text{s.t. Ext}_2 = (id_{ext}, \text{ExtCore}_{s_2}, \ldots, \text{activeFlag}, \ell_1), \text{ExtCore}_{s_1} \leq \text{ExtCore}_{s_2} \]
By (2), (4), apply ENABLEDISABLE\text{Ext}1(a) to \( \Sigma_2 \)
(5) \( \Sigma'_2 = \Sigma_2[\Psi_2 \leftarrow \Psi''_2], E_2 \)
By (A3), (2), (3), \( \Psi_1 \downarrow_{\kappa} E_2 \downarrow_{\kappa} \), Lemma 11
(6) \( \Psi''_1 \downarrow_{\kappa} \leq \Psi''_2 \downarrow_{\kappa} \)
By STATE, (A6), (5)
(7) \( \Sigma_1 \downarrow_{\kappa} \leq \Sigma_2 \downarrow_{\kappa} \)
By (A7), (5)
(8) \( E_1 \downarrow_{\kappa} \leq E_2 \downarrow_{\kappa} \)

sub-subcase ii. \( \kappa_1 \subseteq \kappa, \ell_1 - \notin \kappa \)
By Lemma 11
(1) \( \Psi'_1 \downarrow_{\kappa} \leq \Psi_1 \downarrow_{\kappa} \)
By (A6),(1), and STATE
(2) \( \Sigma'_1 \downarrow_{\kappa} \leq \Sigma_1 \downarrow_{\kappa} \)
By (2) and \( \Sigma_1 \downarrow_{\kappa} \leq \Sigma_2 \downarrow_{\kappa} \)
(3) \( \Sigma'_1 \downarrow_{\kappa} \leq \Sigma_2 \downarrow_{\kappa} \)
By (A7)
(4) \( E'_1 \downarrow_{\kappa} \leq E_2 \downarrow_{\kappa} \)

sub-subcase iii. \( \kappa_1 \notin \kappa \)
By BROWSERSTATE2
(1) \( \psi_1 \downarrow_{\kappa} = \cdot \)
(2) \( \Psi_1 \downarrow_{\kappa} = \Psi'_1 \downarrow_{\kappa} \)
By (A6)
(3) \( \Sigma'_1 \downarrow_{\kappa} \leq \Sigma_1 \downarrow_{\kappa} \leq \Sigma_2 \downarrow_{\kappa} \)
By (A7)
(4) \( E'_1 \downarrow_{\kappa} \leq E_2 \downarrow_{\kappa} \)

case: ENABLEDISABLE\text{Ext}1(b)

\[ \Sigma = (\Psi, Tabs, Ext :: Ext, ExtCoreRs, \ldots) \]
\[ \Psi = \Psi' :: chrome\text{.management\text{.setEnabled}}(\kappa, id_{cb}, (\text{string, id, id}_{ext}, \text{activeFlag})) \]
\[ \text{Ext} = (id_{ext}, \text{ExtCore}, \ldots, \text{activeFlag}, \ell_1) \]
\[ \kappa \subseteq \ell_1^* \]
\[ \ell_2 = \kappa \uparrow_{\text{int}} \ell_1 \]
\[ \text{fresh}(id_e) \]
\[ e_1 = (id_e, id_{cb}, \text{none, getInfo}(Ext), \ell_2^\prime) \]

\[ \text{nextState}(\Sigma, \text{chrome\text{.management\text{.setEnabled}}}(\kappa, id_{cb}, (\text{string, id, id}_{ext}, \text{activeFlag}))) \]
\[ = \Sigma[\Psi \leftarrow \Psi'], e_1 \]

Let \( \Sigma_1 = (\Psi_1, Tabs_1, \text{ExtCore}_{s_1}, \text{progInjCS}_{s_1}, \text{Ext}_{s_1}, \text{Cookies}_{s_1}, \text{MBookmarks}_{s_1}, \text{histories}_{s_1}, UI_1) \)
\( \Sigma_2 = (\Psi_2, Tabs_2, \text{ExtCore}_{s_2}, \text{progInjCS}_{s_2}, \text{Ext}_{s_2}, \text{Cookies}_{s_2}, \text{MBookmarks}_{s_2}, \text{histories}_{s_2}, UI_2) \)
By assumptions
(A1) \( Ext_1 = (id_{ext}, \text{ExtCore}_{s_1}, \ldots, \text{activeFlag}, \ell_1) \)
(A2) \( Ext_1 \in \text{Ext}_{s_1} \)
(A3) \( \Psi_1 = \Psi'_1 :: \psi_1, \psi_1 = \text{chrome\text{.management\text{.setEnabled}}}(\kappa, id_{cb}, (\text{string, id, id}_{ext}, \text{activeFlag})) \)
(A4) \( \kappa \subseteq \ell_1^* \)
(A5) \( \ell'_1 = \kappa \uparrow_{\text{int}} \ell_1 \)
(A6) \( \text{fresh}(id_e) \)
(A7) \( e_1 = (id_e, id_{cb}, \text{none, getInfo}(Ext_1), \ell'_1^\prime) \)
(A8) \( \Sigma'_1 = \Sigma_1[\Psi_1 \leftarrow \Psi''_1] \)
(A9) \( E_1 = e_1 \)

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sub-subcase i. $\kappa_1 \sqsubseteq \kappa, \ell_1^- \sqsubseteq \kappa$

By BROWSERSTATE1

(1) $\psi_1 \downarrow_\kappa = \psi_1, \psi_1 \in \Psi_1 \downarrow_\kappa$

By $\Psi_1 \downarrow_\kappa \leq_c \Psi_2 \downarrow_\kappa, (1)$

(2) $\exists \psi_2 \in \Psi_2 \downarrow_\kappa, \text{s.t. } \psi_1 \downarrow_\kappa \leq \psi_2 \downarrow_\kappa$, namely $\psi_2 = \psi_1$

(3) $\Psi_2 = \Psi_2'' :: \psi_2$

By $\Psi_1 \downarrow_\kappa \leq_c \Psi_2 \downarrow_\kappa, \Psi_1 \downarrow_\kappa \leq \Psi_2 \downarrow_\kappa$,

(4) $\exists \text{Ext}_2 \in \text{Ext}_2$

s.t. $\text{Ext}_2 = (id_{ext}, \text{ExtCore}_2, \ell, \text{activeFlag}, \ell_1^-)$, $\text{ExtCore}_1 \leq \text{ExtCore}_2$

By (A4), (A5), (2), (4), apply ENABLEDISABLEEXT1(B) to $\Sigma_2$

(5) $\text{fresh}(id_{e''})$

(6) $e_2 = (id_{e'}, id_{cb}, \text{none}, \text{getInfo(Ext}_2), \ell_1^-) = e_1$

(7) $\Sigma_2' = \Sigma_2 \downarrow_\kappa \downarrow_\kappa$

(8) $\mathcal{E}_2 = \mathcal{E}_2$

By (A3), (2), (3), $\Psi_1 \downarrow_\kappa \leq_c \Psi_2 \downarrow_\kappa$, Lemma 11

By STATE, (A8), (7), (9)

(10) $\Sigma_1 \downarrow_\kappa \leq \Sigma_2 \downarrow_\kappa$

By (A9), (6), (8)

(11) $\mathcal{E}_1 \downarrow_\kappa \leq \mathcal{E}_2 \downarrow_\kappa$

sub-subcase ii. $\kappa_1 \sqsubseteq \kappa, \ell_1^- \nsubseteq \kappa$

By Lemma 11

(1) $\Psi_1'' \downarrow_\kappa \leq_c \Psi_1 \downarrow_\kappa$

By (A8), (1), and STATE

(2) $\Sigma_1' \downarrow_\kappa \leq \Sigma_1 \downarrow_\kappa$

By (2) and $\Sigma_1 \downarrow_\kappa \leq \Sigma_2 \downarrow_\kappa$

(3) $\Sigma_1' \downarrow_\kappa \leq \Sigma_2 \downarrow_\kappa$

By EVENT2, (A9)

(4) $\mathcal{E}_1 \downarrow_\kappa = \cdot$

sub-subcase iii. $\kappa_1 \nsubseteq \kappa$

By BROWSERSTATE2

(1) $\psi_1 \downarrow_\kappa = \cdot$

(2) $\Psi_1 \downarrow_\kappa = \Psi_1'' \downarrow_\kappa$

By (A4)

(3) $\Sigma_1' \downarrow_\kappa = \Sigma_1 \downarrow_\kappa \leq \Sigma_2 \downarrow_\kappa$

By (A5), $\kappa_1 \nsubseteq \kappa$, EVENT2

(4) $\ell_2^- \nsubseteq \kappa$

(5) $\mathcal{E}_1 \downarrow_\kappa = e_1 \downarrow_\kappa = \cdot$
References
