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Cristina H. Amon

Carnegie Mellon University

Jay S. Nigen

Carnegie Mellon University. Engineering Design Research Center.

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EDRC 24-114-94

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Cristina H. Anton and Jay S. Nigen Engineering Design Research Center and Department of Mechanical Engineering Carnegie Mellon University Pittsburgh, PA 15213

Abstract

A time-dependent conjugate conduction/convection numerical study of four electronic component configurations that differ in material composition and distribution of internal heat generation is conducted in parallel PCBs (Printed Circuit Boards) for laminar and transitional Reynolds numbers. Both material composition and concentration of heat generation are found to affect the spatial distribution of temperature, heat flux, and Nusselt number along the solid-fluid interface. Furthermore, it is found that the distribution of internal heat generation strongly affects the convective resistance at the solid-fluid interface of the componient. This leads, for the configurations with local heat generation, to a non-monotonic relationship between the convective heat transport and the Reynolds number for the range of parameters investigated. It is found that conjugate heat transfer can significantly affect the temperature distribution.

1. Introduction

1.1 Thermal Design

Thermal phenomena have served as limiting constraints in the design and operation of equipment used in a variety of industries, such as aerospace, energy production, automotive, and recently, electronics. In such circumstances, the maximum temperature experienced by critical components is constrained to prevent thermally-induced failures that result from fatigue, melting, and variations in material properties. Should the naturally-present heat transport prove inadequate to prevent these failure modes, augmentation techniques or additional heat exchangers are employed. These heat exchangers can either be detached systems, such as the radiator in an automobile, or integrated into a component, such as cooling passages within turbine blades or heat spreaders within electronic packages. For these configurations, heat is generated internally and/or at solid-fluid interfaces and is then transferred to the environment by

a combination of heat transfer modes from and within the system or component A thermal resistance is associated with each transport mode, representing the induced temperature drop for a fixed energy flux. Therefore, the thermal design problem involves reducing the thermal resistance(s) associated with mode(s) of heat transfer to minimize the induced temperature drop(s) and thermal gradient(s).

The thermal resistance associated with heat conduction can be reduced by using more conductive materials and by improving the contact conductivity associated with any subcomponent interfaces. However, these approaches can result in prohibitively high manufacturing costs. Alternatively, the amount of convective transport can be increased through additional surface area, thinning of the boundary layers, and homogenization of the thermal distribution within the cooling fluid. The later can be achieved by increasing the Reynolds number to obtain transitional or turbulent flows and with turbulators or flow destabilizers. However, these approaches result in additional pressure drop that increases operating expenses.

The problem confronting the heat transfer engineer is to determine an adequate cooling design that balances performance with manufacturing and operating expenses. An ill-conceived thermal design can either be ineffective, thereby degrading the life span of a system, or over designed, adding unnecessary size, weight, and expense. It is therefore essential to accurately analyze the thermal performance of a system. However, the competitive environment of today's marketplace limits the time available for analysis and design. These stringent time constraints may require the thermal engineer to neglect less significant effects while developing system models.

Often, the thermal modeling procedure reduces analysis to solving the heat equation within the solid domain. Convective effects, associated with the environmental fluid, are imposed through the heat transfer coefficient at the solid-fluid boundaries. Correlations for heat transfer coefficients have been empirically generated for a variety of geometries and flow conditions. However, most correlations have been obtained with the use of either spatially-uniform temperature or heat flux boundary conditions. In essence, the effect of heat conduction within the solid is replaced by idealized boundary conditions, which presuppose the heat flow paths within the solid. Therefore, the resistances associated with conduction within the solid and convection within the fluid have been decoupled, an assumption that may not be appropriate for all systems.

12 Literature Review

The coupling of conduction within the solid and convection within the fluid, termed conjugation, is required in the analysis of systems that involve intense heat transfer,

multimaterial solid domains and localized heat generation, as described by Perelman [1]. In conjugate problems, neither the temperature nor the heat flux at solid-fluid interfaces can be prescribed a priori. Therefore, the convective boundary condition, as previously described, may not be accurate. The appropriate boundary conditions are continuity of heat flux and temperature at the solid-fluid interface and are termed boundary conditions of the fourth kind.

Analytical conjugate studies of external flows over flat plates have been conducted using either assumed velocity profiles or Blassius boundary layer solutions with uniform heat generation [1-4] and constant temperature along one surface of the plate [5]. Poiseuille flows in circular and planar pipes of finite thickness, accounting for viscous dissipation, have also been studied [2]. Furthermore, Luikov [5] developed analytic heat transfer correlations for conjugate problems that involve functions of a spatially-variable Biot number, called the Bran number. A more recent analytical work involves conjugate heat transfer for a single-material, uniformly heated block [6]. Conjugate heat transfer through a variable-thickness wall was analyzed using variation calculus, demonstrating that a minimum heat flux through the wall is obtained when the wall thickness diminished in the streamwise flow direction [7]. Unfortunately, all the resulting descriptions of temperature, heat flux, and convective transport distributions tend to be rather complex, rendering them difficult to implement in a design setting. Furthermore, most systems are not well modeled by single-material, uniform heat generating solid domains, thereby, limiting the applicability of these works.

Numerical studies provide an alternative and, sometimes, a unique approach for configurations with non-homogeneous solid domains. A two-dimensional steady conjugate study of a system with a multimaterial solid domain and a heat source at the solid-fluid interface was conducted using finite differences [8]. The time-dependent conjugate behavior of a semiinfinite slab [9] and slab-wall configuration [10] exposed to uniform surface heating was studied using the Unsteady Surface Element Method. The two-dimensional conjugate behavior of hydrodynamically fully-developed, laminar flow through a circular tube with thick walls and a finite heated length was investigated using a finite volume approach [11]. Recent interest in electronics cooling has fostered research on conjugate heat transfer from simulated electronic components. A finite-volume based approach was used to study the steady state, conjugate behavior of three single-material, uniform heat generating blocks [12] and one multimaterial, local heat generating electronic component [13]. A semi-analytical approach that utilizes an integral formulation for the fluid domain and a finite volume formulation for the solid domain was successfully developed to study plates with discrete heat sources, which model surfacemounted electronic packages [14]. Mixed laminar convection from multimaterial, local heat generating components was also studied using a Simpler-based approach [15]. A time-dependent

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study of a multimaterial, local heat generating configuration using the spectral element method was conducted by Nigen and Amon [16] for both laminar and transitional Reynolds numbers. This investigation contrasted thermal behavior characteristics for a conjugate and uniform-flux representation of a simulated electronic package.

13 Electronics Cooling

The electronics industry remains a strong and vibrant sector of the global economy. Its profit potential has fueled a rapid pace of technical innovation, leading to advancements in miniaturization, performance, and efficiency. However, this profit potential has also created a highly competitive marketplace, in which technical innovation must be carefully harnessed to insure success. As such, key limiting factors that inhibit future advancement have been identified by industry and focused on by researchers. One such limiting factor is the removal of heat Heat removal has been addressed by material scientists through the development of new materials, such as gallium arsenide, by electronic engineers with new circuit configurations, such as CMOS and BiCMOS, and by heat transfer specialists. In spite of their efforts, heat removal remains an essential enabling technology in the design of today's electronic systems.

Electronic systems are composed of a number of subcomponents that are commonly divided into levels. As shown in Figure 1, level one corresponds to the chip carrier or package, level two to the chip-to-chip interconnect, level three to the board-tb-board interconnect, and level four to the rack, housing, or cabinet. The design of each of these levels requires the contributions of a diverse development team because each level must accomplish multiple tasks. As an example, the package carrier serves as the conduit through which power and signals are transferred to and from the chip, as well as housing and protecting die chip from the environment [17]. Additionally, in order for a chip to function properly and reliably, the maximum temperature experienced must be below some specified operating temperature, frequently in the 90 to 100 C range [18].

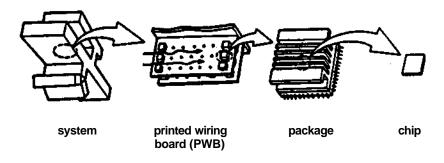


Figure 1: Schematic of component levels of a computer system

A lucid description as to why a CMOS chip needs to be kept below a prescribed temperature is presented in [19]. In a computer system, all information is represented by combinations of two varieties of bits, 0 and 1. Information is processed by the working of switches, each switch having only two states that correspond to the bits, 0 and 1. A mainframe computer of the present generation has approximately 10^7 binary switches in the central processing unit (CPU), and 10^9 - 10^{10} switches in the main memory unit A microprocessor, which is a complete system implemented on a single chip, has around 10^6 switches [19].

One of the essential requirements for such systems is the absolute reliability of individual switching operations. The state of the switch is defined by its output voltage; when it is higher than a certain threshold voltage, the state of the switch is defined as 1, and when it is lower, the state corresponds to 0. The threshold voltage can vary within a certain range from switch to switch. However, the states of the individual switches have to be unambiguously defined. Figure 2 is a conceptual sketch of a binary switch. The vertical axis represents the electric potential for the outputs and the threshold. The horizontal axis is a potential scale defining the states 0 and 1. A circular mass, depicted in the well of state 0, represents a group of electric charge carriers. Switching corresponds to shifting the circular mass across the hump of electric potential between the two wells. Once inside either well, the mass has to be kept there resisting excitations from disturbances for a state to be established. Therefore, the potential energy hump AE has to be set higher than the level of agitations associated with noise sources in the system. A primary source of noise is the electromagnetic waves generated by simultaneous operations of switches, the magnitude of which is temperature dependent

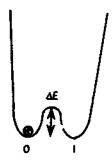


Figure 2: Sketch of a binary switch; horizontal axis: states 0 and 1, and vertical axis: energy potential

Redefining the state of the switch requires moving the mass over the energy hump. This motion requires work, and the energy consumed in this work is converted to heat Unless heat is removed at a high enough rate, the environmental temperature increases, causing growth in thermal noise and other detrimental long-term effects. These long-term effects include the

promotion of chemical diffusion in the device material. Chemical diffusion leads to an eventual degradation of device characteristics, exemplified by a significant shift of the energy hump on the horizontal scale of Figure 2.

A mathematical representation of the above description is given by $t_g = \frac{V(CAV)}{p_g}$. The product CAV corresponds to the mass of the charge carriers, and the source voltage V is proportional to the height of the energy hump AE. The power-delay product, Pgtg, represents the work required to raise the mass of charge carriers to the top of the energy hump. It also embodies a primary goal of the electronics industry, namely, the decreasing of gate delay time, tg. This can be accomplished by adopting a more efficient means of cooling that permits a larger Pg , decreasing the voltages V and AV to reduce the power consumption and miniaturizing the circuit, which results in smaller capacitance, C. The thermal designer has and must continue to increase the amount of heat removed to reduce gate delay time, t_g .

Thermal phenomena also adversely affect electronics at a macro-scale Thermal gradients within packages induce stresses in chip-to-package and package-to-board interconnects, which can cause catastrophic failures in signal and power transmission. Furthermore, chip timing is affected by temperature, necessitating that systems function within relatively narrow temperature ranges to insure proper operation, frequently 10 to IS C. This is why the Cray II supercomputer is cooled using direct immersion in a dielectric fluid [20]. Therefore, at both the micro-scale and macro-scale, maintenance of a satisfactory thermal environment is essential for proper and reliable operation of an electronic system and for the development of faster systems in the future.

Recent trends within the computer market are causing the challenges of cooling today's systems to be quite different than those of the 1980's. The trend towards smaller machines that operate in the workplace strictly limits noise production, making forced convective cooling undesirable. This problem is further exacerbated in portable machines because of power consumption constraints. These trends have resulted in increased interest in cooling systems by natural convection or, if necessary, low velocity forced convection.

An alternate approach, motivated by the stringent design constraints associated with portable systems, employs conduction-augmented cooling strategies [21]. These conjugate cooling methods use system size heat spreaders or flexible heat pipes to cool essential components [22,23]. A design based on these cooling strategies is complicated by the degree of concentrated heat generation and the multimaterial/multicomponent nature of electronic systems. Futhermore, the recent success in miniaturization has resulted in fewer heat producing components and boards within a system. These systems contain localized heat sources that exhibit higher heat fluxes at fewer locations than in previous systems. Therefore, the nature of

tomorrow's electronic systems and associated cooling strategies will require conjugate analyses to insure an adequate and cost effective thermal design and, ultimately, success in the marketplace.

1.4 Motivation

In previous studies, conjugation was found to affect thermal performance characteristics. However, only parameters such as material composition and Reynolds number were independently varied to *assess* their relative effect upon temperature, flux and heat transport. The purpose of this study is to explore the fundamental effect of the distribution of internal heat generation, as well as multimaterial composition on conjugate heat transfer in grooved channels over a range of laminar and transitional Reynolds numbers. It is important for thermal analysts to understand the relative importance of non-homogeneity within the solid domain to be capable of developing accurate thermal models. Furthermore, some systems may require combined reduction of thermal resistances associated with multiple modes of heat transfer to achieve optimum, or near optimum, cooling designs. Therefore, the following four representative configurations will be investigated: (i) local heat generation with single-material composition (LS), (ii) local heat generation with multimaterial composition, (LM) (iii) uniform heat generation with single-material composition (US), and (iv) uniform heat generation with multimaterial composition (UM).

2. Problem Formulation

The mathematical model of a conjugate conduction/convection problem with incompressible flow involves a system of partial differential equations for the solid and fluid domains (Eqs. 1-3). The fluid properties are assumed constant and buoyancy forces, viscous dissipation and radiation are all neglected.

$$\frac{d\vec{v}}{\partial t} = \vec{V} \vec{X} \vec{G}) \vec{P} \vec{V} \left(p + *j - \vec{J} + \vec{W}^2 \vec{V} \right)$$
(1)

$$\mathbf{V}\mathbf{v} = 0 \tag{2}$$

$$\frac{\partial T}{\partial t} = \alpha \nabla^2 T - \vec{v} \cdot \nabla T + \frac{u'''}{\rho c_p}$$
 (3)

The boundary conditions for the momentum equation are no slip along the solid-fluid interfaces and periodicity in the strearawise direction (Fig. 3). For the energy equation, the top surface of the upper wall and the bottom surface of the lower wall are adiabatic, and periodicity is imposed in the streamwise direction by subtracting the calculated rise in mixed-mean temperature on a point-by-point basis at each streamwise location.

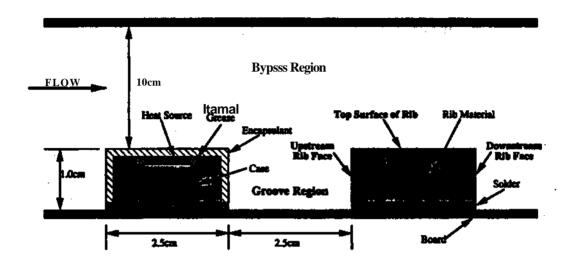


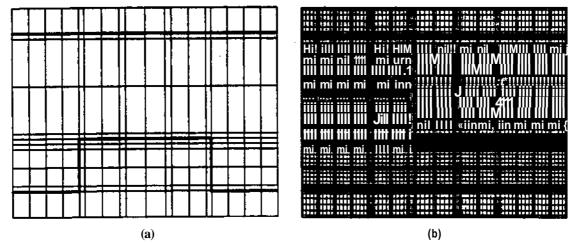
Figure 3: Schematic of ctectrontecomp^ents and material configurations

The numerical procedure employed for the spatial discretization is the spectral element technique [24, 25]. The spatial domain is decomposed into macro-elements upon which tensor products of high-order Legendre polynomials are projected. The elemental discretization used is shown in Fig. 4a, and the mesh indicating the distribution of internal nodes is shown in Fig. 4b. The control of spatial resolution and the high degree of accuracy associated with this technique makes it well suited for studying time-dependent conjugate problems with localized heat generation and multimaterial solid domains, especially those with large disparities in material properties.

The accuracy of the spectral element solution may be affected either by increasing the total number of macro-elements, obtaining algebraic convergence, or by increasing the order of the local expansions, achieving nearly-exponential convergence. Adequate resolution was verified by comparing the flow characteristics using both 7th and 9th order local expansions, as well as using different macro-elemental discretizations. The results from the simulations for the macro-elemental discretization used in this study with 7th and 9th order expansions yielded virtually identical results, indicating that the lower resolution was adequate for this investigation.

The numerical approach is to integrate the continuity and momentum equations for the fluid domain and then the energy equation for both the solid and fluid domains. This procedure is iterated in time, using a three-step, semi-implicit, time-splitting scheme, until either a steady state or time-periodic state is reached. A typical mesh consisting of 198 elements, each containing 49 degrees of freedom, requires 3.14 CPU seconds per time step on a Cray Y-MP.

The dimensions and composition of the solid domain, as shown in Fig. 3, represent a typical electronic package. The material properties and, when appropriate, the associated amount of heat generation, are displayed in Table 1. The thermal conductivities displayed in Table 1 include contact resistance, which is modeled by modifying the conductivity such that the effective thermal resistance obtained is commensurate with empirical data from Yovanovich and Antonetti [26].



Figure* Spatial discretization showing (a) macroelements and (b) collocation points. Daifcer lines indicate solid-fluid interfaces

Component	k (W/cm °C)	pc _p (KJ/cm3 «C)	u~ (W/cm3)
Case	2.04x10-!	3.47	
Heat Source	1.25×10^{-2}	1.74	5.1842
Encapsulate	6.99 x 10-3	3.16	
Board	7.4 x 10-3	2.27	
Rib Material	1.25 x 10-2	1.74	1.558 x 10'' ¹
Solder	1.0x10-3	1.47	
Thermal Grease	9.614 x 10-3	1.7 1	
Air	2.851×10^{-4}	1.534×10^{-4}	

Table 1: Material properties of the solid domain.

It should be noted that because buoyancy effects are neglected, the resulting flow patterns are independent of the solid-fluid interface temperature and heat flux distributions. Therefore, for a specific Reynolds number, the variations present in the distributions of surface temperature, heat flux, and Nusselt number are only attributable to the composition of the solid domain and the distribution of heat generation. It is this combination, along with the local-fluid characteristics, which determines the heat flow paths and, ultimately, the thermal performance characteristics of the configuration.

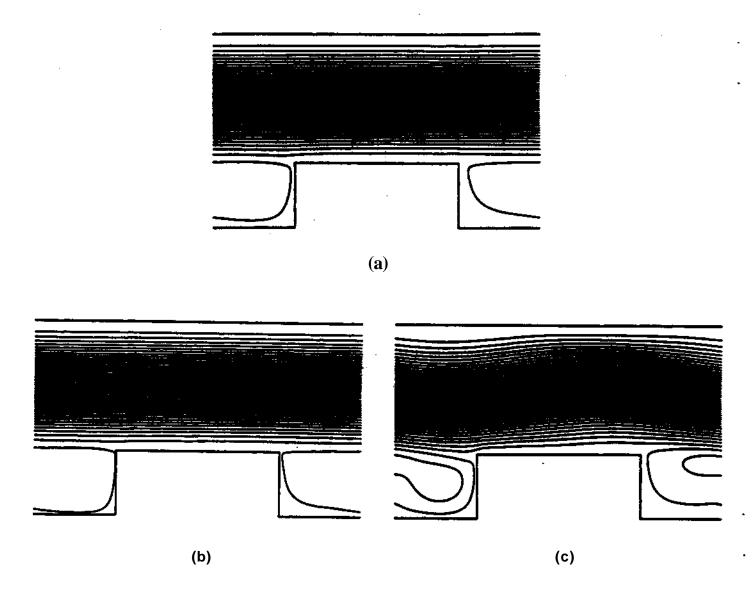


Figure 5: Contours of the streamfunction for (a) laminar, (b) slightly-transitional, and (c) transitional flow regimes

3. Flow Patterns

Three Reynolds numbers are considered for this investigation: low, middle and high. The low Reynolds number case corresponds to a laminar flow field, wherein, the fluid in the channel is separated by a shear layer from the recirculating fluid within the groove [16]. Fig. 5a displays the contours of the streamfunction corresponding to the laminar flow regime at Re=270 and a maximum streamwise velocity of 36.5 cra/s. Convective transport from the upstream and downstream rib faces is hampered by the shear layer, which inhibits direct exchange of heated groove with cooler channel fluid. Additionally, the Poiseuille-like nature of the flow in the channel results in larger shear stresses along the top of the rib than along the upstieam or downstream rib faces [27]. These effects cause greater convective resistances along the upstieam and downstream faces than along the top surface of the rib.

The middle Reynolds number case corresponds to a slightly transitional flow field. Figure 5b displays the contours of the streamfunction for this flow regime at Re=640 and a maximum streamwise velocity of 86.4 cm/s. Small amplitude oscillations, corresponding to Tollmien-Schlichting waves [28] are present within the channel flow. The amplitude of the velocity components associated with the oscillations is approximately two orders of magnitude smaller than the average streamwise velocity of the channel flow. In spite of the small amplitude of the fluctuations, the nature of the transitional flow pattern results in larger shear stresses along the surfaces of the rib [27]. However, the small magnitude of transverse momentum associated with the traveling waves is insufficient to disrupt the shear layer. Therefore, diffusion remains the dominant mode of energy exchange between the heated groove fluid and cooler channel fluid.

The flow field at the high Reynolds number is very different from either the middle or low Reynolds numbers. Figure 5c displays the instantaneous contours of the streamfunction corresponding to the transitional flow regime at Re=700 and a maximum streamwise velocity of 94.5 cm/s. This time-periodic flow contains large amplitude Tollmien-Schlichting waves in the channel. The magnitude of the velocity fluctuations is approximately one order of magnitude smaller than the average streamwise velocity of the channel flow. The increased transverse momentum of the channel flow results in the shear layer being periodically disrupted. Therefore, heated groove fluid can convect into the channel and be replaced by cooler fluid. Additionally, the shear stress along all of the rib surfaces increases significantly, which reduces the convective resistance, particularly near the upstream rib corner [27].

4. Spatial Distributions at the Solid-Fluid Interface

4.1 Temperature

Firstly, the local temperatures along the solid-fluid interface of the grooved surface are presented for each of the four configurations and for the three Reynolds numbers studied. The data presented for the middle and high Reynolds number cases are the time-average difference between the solid-fluid interface and bulk-mean temperatures, corresponding to the passing of one Tollmien-Schlichting wave. Additionally, the application of periodic boundary conditions emulates studying the thermal characteristics of heated ribs within the periodic fully-developed region. In this region, the difference between the solid-fluid interface and bulk-mean temperatures remains periodically invariant. It should be noted that periodic fully-developed behavior has been experimentally observed in similar geometries, e.g. ribbed channels, after the third or fourth component [29,30].

The interface temperature distributions for all of the cases and configurations exhibit effects associated with both rib material composition and distribution of heat generation, as shown in Figs. 6a-c. For the configurations containing local heat generation, the heat source is positioned near the top of the rib. This results in a local rise of surface temperature directly above the location of the chip.

As the Reynolds number is increased, the convective resistance is lowered near the upstream corner of the rib. However, because of conduction within the solid, variations in the interface temperature distribution are visible along portions of the top and upstream rib faces (Figs. 4b, c). The configurations corresponding to single-material composition have lower conductive resistance and exhibit a more asymmetric surface temperature distribution than those with multimaterial composition. This larger conductive resistance localizes convective effects, resulting in larger gradients, but more symmetric overall temperature distributions.

For the high Reynolds number case (Fig. 6c), the magnitude of convective transport is large enough to strongly affect the surface temperature distribution for the single-material rib configurations. In fact, the higher rate of convective transport at the leading edge of the rib results in a decrease of surface temperature along nearly sixty percent of the top surface of the rib for the uniform heat generating, single-material (US) configuration.

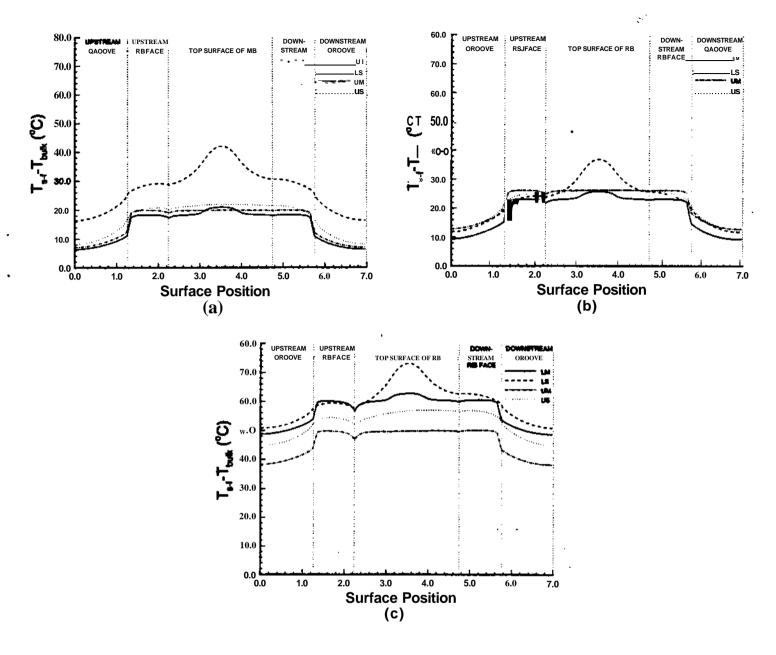


Figure 6: Solid-fluid interface and bulk-mean temperature difference versus surface position for (a) low, (b) middle, and (c) high Reynolds number cases. LM: local heat generation, multimaterial configuration; LS: local beat generation, single-material configuration, uniform beat generation, multimaterial configuration, and US: uniform beat generation, single-material configuration

4.2 Heat Flux

The local heat flux distributions are now considered for the same configurations and Reynolds numbers previously examined. As with the interface temperature distributions, the local heat flux data presented for the middle and high Reynolds number cases are time averaged over one wave cycle. Additionally, a sign convention is adopted such that heat flux leaving the solid domain at the solid-fluid interface is positive, while heat flux entering is negative.

The spatial distributions of heat flux for the three Reynolds number cases are displayed in Figs. 7a-c. As previously demonstrated, both material composition and distribution of heat generation affect the resulting patterns. All the configurations display the classical pattern associated with boundary layer growth along the top surface of the rib. However, the configurations with local heat generation display increased heat flux over the location of the heat source. This increase is especially significant for the single-material configuration (LS).

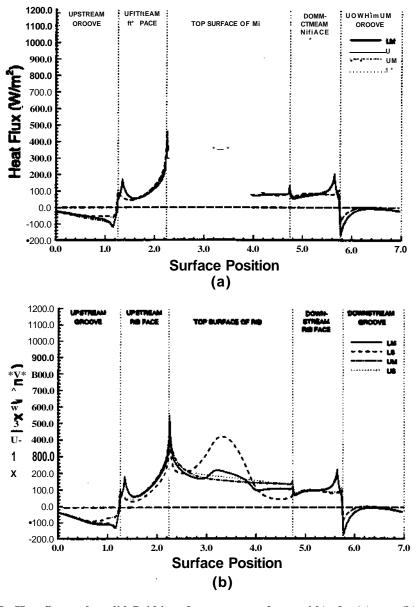


Figure 7: Heat flux at the solid-fluid interface versus surface positk)o for (a) tow, (b) mkklk, md (c) Wgh Reynolds i sumber cases

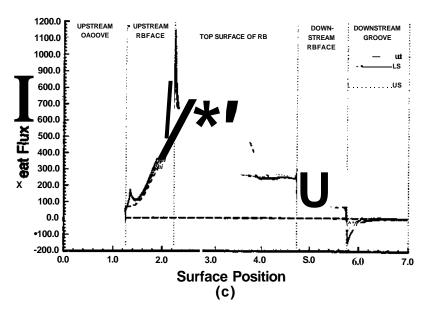


Figure 7 coot.

A local increase in heat flux for the multimaterial configurations (LM, UM) occurs along both the upstream and downstream rib faces corresponding to the location of the solder. This is attributable to the larger conductive resistance associated with the solder. The relative convective resistance from the rib face decreases with respect to the conductive resistance into the board, resulting in a local increase of heat flux.

At the low Reynolds number, there is an intact shear layer separating the groove fluid from the channel fluid. The recirculating fluid within the groove is heated along both the upstream and downstream rib faces, but the shear layer prohibits convective exchange of the heated groove fluid with cooler channel fluid. The heated groove fluid becomes hotter than the adjacent surface (board), leading to heat transfer into, rather than out of, the solid domain. However, as the flow becomes transitional and the shear layer is disrupted, some of the heated groove fluid is replaced by cooler channel fluid. This convective exchange of fluid between the groove and channel reduces the magnitude of the temperature gradient along the groove, leading to less heat flux into the solid domain for the higher Reynolds number case. An important observation is that the spatial distribution of flux along the groove surface is affected more by the distribution of heat generation than by the material composition of the rib.

As the Reynolds number increases (Figs. 7b, c), the peak value of heat flux at the leading edge of the rib increases for all conflgurations. However, the magnitude of heat flux along the latter portion of the top surface of the rib is reduced for the local heat generating conflgurations. The increased heat flux along the top of the rib, from the upstream corner to the location of the heat source, raises the temperature of the fluid in the thermal boundary layer. This increases the convective resistance in the streamwise direction, resulting in a reduction of heat flux from the later portion of the rib.

43 Nusselt Number

A classical measure of convective heat transfer is the Nusselt number, which can be interpreted as representing either the nondimensional temperature gradient at the solid-fluid interface or the magnitude of the convective heat transfer scaled by the equivalent conductive heat transfer in the fluid. However, for conjugate problems, the former interpretation is preferable because it more easily accommodates the presence of both positive and negative heat fluxes along a surface.

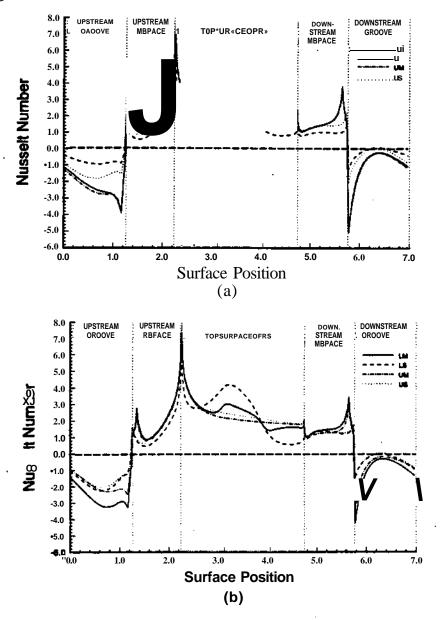


Figure 8: Nusselt number at the solid-fluid interface versus surface position for (a) low, (b) middle, and (c) high Reynolds number cases

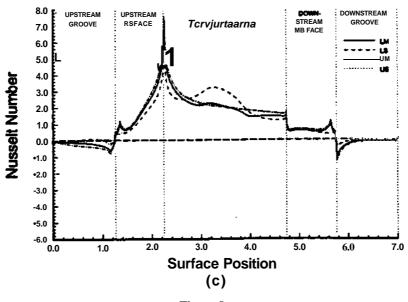


Figure 8 coot

The spatial distributions of Nusselt numbers are shown in Figs. 8a-c. Unlike the interface temperature or heat flux distributions, the magnitudes of the Nusselt number for all of the configurations are similar, but the spatial distributions are slightly different. The local heat generating configurations (LS, LM) display increases in Nusselt number above the location of the heat source. Likewise, along the upstream and downstream rib faces, the multimaterial configurations (LM, UM) display increases in Nusselt number over the regions corresponding to the location of the solder. However, there is some disparity in the distribution along the groove. The distributions corresponding to the multimaterial configurations (LM, UM) closely follow one another, particularly along the downstream portion of the groove. However, the singlematerial configurations (LS, US) do not correlate well along the upstream portion of the groove for the high Reynolds number case. The poor correspondence is associated with the larger amount of heat flux removed from the upstream rib face for the uniform heat generating case (US), after the shear layer is disrupted.

A closer inspection of the distribution along the top surface of the rib reveals a degradation in performance for the local heat generating configurations (LS, LM) after the location of the heat source, especially so for the single-material configuration (LS). As previously described, the fluid within the near-wall portion of the thermal boundary layer is heated along the rib, increasing its convective resistance, as evidenced in the Nusselt number distribution.

Although greater amounts of heat flux are achieved as the Reynolds number is increased, no comparable increases are reflected in the Nusselt number distribution (Figs. 8b, c). Furthermore, the variations in spatial distributions along the rib diminish such that the only significant difference for all, save the uniform heat generating single-material rib configuration (US), occurs above the location of the solder and the heat source. However, even the magnitude of these

differences is minimized. With increasing Reynolds number, the fluid becomes better mixed resulting in a more homogeneous thermal distribution within the flow. Therefore, differences in thermal performance caused by upstream variations in heat flux would decrease in significance.

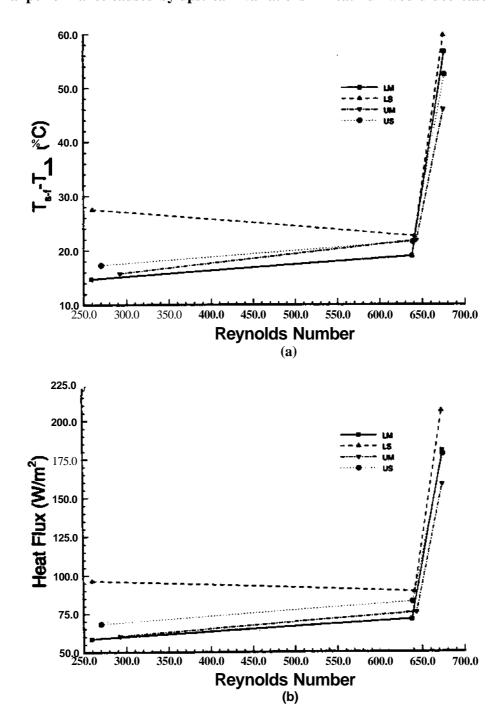


Figure 9: Time- and space-average (a) difference between the solid-fluid interface and bulk-mean temperatures and (b) beat flux at the solid-fluid interface versus Reynolds number

5. Discussion

Although there are distinct spatial variations of surface temperature, heat flux, and Nusselt number within and between the four configurations, more general behavior differences become apparent when spatially-averaged values are examined.

The averaged difference between the local solid-fluid interface and bulk-mean temperatures, as a function of Reynolds number, is shown in Fig. 9a. The temperature difference for the local heat generating, single-material rib (LS) decreases with Reynolds number in the subcritical regime. At the high Reynolds number case, the flow becomes more homogeneous and the temperature difference increases. However, the temperature difference for the other configurations continuously increases with Reynolds number, regardless of the flow regime. The key to understanding this behavior is the recognition of the relationship between the temperature rise of the fluid and the heat flux for conjugate problems.

An order of magnitude analysis of the convective boundary condition corresponding to a uniform heat flux at the solid-fluid interface yields an inverse relationship between the heat transfer coefficient and the temperature difference.

$$h(T_{s-f} - T_{bulk}) = -k, |k|_{\vec{n}} = Q$$
 (4a)

$$\mathbf{h} \propto \frac{1}{(T.-_f-T_{\text{bulk}})} \tag{4b}$$

The well-known solution for convective heat transfer over a flat plate, with an imposed uniform heat flux boundary condition, states that the heat transfer coefficient is proportional to the Reynolds number to the one-half power. Therefore, the inverse relationship shown in Eq. 4b implies that as the Reynolds number is increased, the wall temperature approaches the bulk-mean temperature. This behavior has also been demonstrated for convective heat transfer from a grooved channel with an imposed uniform heat flux boundary condition [16]. However, an order of magnitude analysis for the conjugate boundary condition reveals a different relationship.

$$Q = -k_{s} \frac{\partial T_{s}}{\partial \tilde{n}} - \frac{\partial T_{f}}{\partial H} (5a)$$

$$Q = -k_{s} \frac{\partial T_{s}}{\partial \tilde{n}} - \frac{k_{f}}{H} (T_{s-f} - T_{bulk})$$

$$Q \propto (T_{s-f} - T_{bulk})$$
(5b)

Namely, the difference between the solid-fluid interface and bulk-mean temperatures is directly proportional to the heat flux (Eq. 5c). As predicted, the spatially-averaged heat flux, displayed in Fig. 9b, exhibits the same behavior characteristics as the temperature difference.

Physically, energy converted from the rib surface into the fluid increases its bulk-mean temperature. However, when there is little transverse mixing in the flow, the heat removed from the rib results in a nonhomogeneous temperature distribution. Therefore, the temperature distribution within the fluid depends upon the spatial distribution of heat flux along the solid-fluid interface and the flow patterns. The local heat generating, single-material configuration (LS, Figs. 7 and 9b) exhibits significantly higher heat flux from the top surface of the rib than the other configurations. This distribution of heat flux raises the fluid temperature within the boundary layer above the rib more than for the other configurations. The thermal wake that extends from the preceding rib increases the convective resistance along the top surface of the rib, reducing convective rates. Therefore, until the local flow patterns produce a more homogeneous temperature distribution within the fluid, the difference between the solid-fluid interface and bulk-mean temperatures will be larger for this configuration than for the others.

For the high Reynolds number case, the channel flow becomes non-parallel and the shear layer is disrupted, increasing significantly the heat flux along the upstream and downstream rib faces, especially for the uniform heat generating configurations (US, UM). The periodic disruption of the shear layer converts the heated fluid from the groove into the channel. This heated fluid is converted further into the channel, resulting in a lower temperature rise in the fluid directly adjacent to the rib. However, the increased conductive resistance within the multimaterial configurations (LM, UM) reduces the amount of flux removed from the upstream and downstream rib faces. Therefore, the distribution of heat generation dictates the qualitative behavior while the material composition dictates the quantitative performance.

Next, the spatially-averaged Nusselt number is considered as a function of the Reynolds number in Fig. 10. The effect of convective resistance along the top surface of the rib is visible in the spatially-averaged Nusselt number. The spatially-averaged Nusselt number for the local heat generating configurations (LS, LM) decreases with Reynolds number in the subcritical regime and then increases, once the flow becomes supercritical and better mixed. However, the spatially-averaged Nusselt number for the uniform heat generating configurations (US, UM) continuously increases with Reynolds number due to the spatial distribution of heat flux, as previously described.

The uniform heat generating, single-material configuration (US) displays the closest behavior to a non-conjugate analysis, followed by the uniform heat generating, multimaterial configuration (UM). Qualitatively, problems which involve complex flow behavior, including time- and spatially-dependent separation and reattachment, as well as intense heat transfer, multimaterial solid domains and localized heat generation [1], require conjugate formulations. This insight is required for the successful construction of heat transfer correlations for conjugate

heat transfer problems. It also indicates that the construction of such correlations might be an exceedingly difficult task for systems that exhibit strong conjugate effects and non-monotonic relationships with respect to Reynolds number.

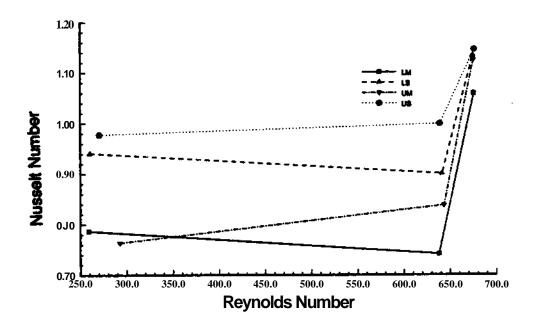


Figure 10: Time- and space-average Nusselt number versus Reynolds number

Conclusions

Conjugate conduction/convection heat transport in electronic cooling configurations is investigated for single and multimaterial components, as well as for local and uniform distributions of heat generation. At the solid-fluid interface of the components, the spatial distributions of temperature, heat flux and Nusselt number demonstrate variations associated with both material composition and distribution of heat generation. Furthermore, negative heat fluxes and Nusselt numbers are obtained along portions of the groove surfaces for all the configurations and Reynolds numbers explored.

Thermal energy converted from the top surface of the rib creates a thermal wake that extends downstream. The lack of small scale mixing within the fluid, in these flow regimes, results in incomplete homogenization of the thermal wake causing increased convective resistance along the top surface of the following rib. This resistance is found to be more strongly influenced by the distribution of internal heat generation than by the material composition.

The resulting spatially-averaged convective characteristics indicate that a thermal analyst should account for concentrations of heat generation within systems such as electronic packages, while multi-material composition is not as essential. This is an important consideration when large systems are being analyzed that tax current computational capabilities.

It has been demonstrated that conjugation produces significant variations in thermal characteristics for the configurations studied, especially for those involving spatial variations in both material composition and internal heat generation. Therefore, conjugation can significantly alter thermal behavior and should be considered in problems involving spatial variations in material composition and heat generation.

Acknowledgments

This work has been supported by the Engineering Design Research Center, a National Science Foundation Engineering Research Center and NSF grant CTS-9311072. Additionally, some of the simulations contained herein were conducted on the NASA Lewis Research Center CrayY-MP.

Symbols

c_p specific heat

h heat transfer coefficient = $Q/(T_{s \cdot f} - T_{bu}ik)$

H half-channel height

k thermal conductivity

ii outward normal with respect to solid surface

 $Nu \quad \ \ Nusselt \ number = (hH)/k_f$

P pressure

O heat flux

Re Reynolds number = (3VH)/(2v)

t time

T temperature

velocity

u'" internal heat generation

V channel-averaged velocity

Greek Symbols

- v kinematic viscosity
- a thermal diffusivity
- (O vorticity
- p density

Subscripts

bulk bulk-mean temperature at leading edge of the rib

- f fluid
- s solid
- s-f solid-fluid interface

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A lucid description as to why a CMOS chip needs to be kept below a prescribed temperature is presented in [19]. In a computer system, all information is represented by combinations of two varieties of bits, 0 and 1. Information is processed by the working of switches, each switch having only two states that correspond to the bits, 0 and 1. A mainframe computer of the present generation has approximately 10^7 binary switches in the central processing unit (CPU), and 10^9 - 10^{10} switches in the main memory unit A microprocessor, which is a complete system implemented on a single chip, has around 10^6 switches [19].

One of the essential requirements for such systems is the absolute reliability of individual switching operations. The state of the switch is defined by its output voltage; when it is higher than a certain threshold voltage, the state of the switch is defined as 1, and when it is lower, the state corresponds to 0. The threshold voltage can vary within a certain range from switch to switch. However, the states of the individual switches have to be unambiguously defined. Figure 2 is a conceptual sketch of a binary switch. The vertical axis represents the electric potential for the outputs and the threshold. The horizontal axis is a potential scale defining the states 0 and 1. A circular mass, depicted in the well of state 0, represents a group of electric charge carriers. Switching corresponds to shifting the circular mass across the hump of electric potential between the two wells. Once inside either well, the mass has to be kept there resisting excitations from disturbances for a state to be established. Therefore, the potential energy hump AE has to be set higher than the level of agitations associated with noise sources in the system. A primary source of noise is the electromagnetic waves generated by simultaneous operations of switches, the magnitude of which is temperature dependent

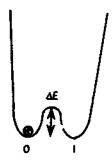


Figure 2: Sketch of a binary switch; horizontal axis: states 0 and 1, and vertical axis: energy potential

Redefining the state of the switch requires moving the mass over the energy hump. This motion requires work, and the energy consumed in this work is converted to heat Unless heat is removed at a high enough rate, the environmental temperature increases, causing growth in thermal noise and other detrimental long-term effects. These long-term effects include the

promotion of chemical diffusion in the device material. Chemical diffusion leads to an eventual degradation of device characteristics, exemplified by a significant shift of the energy hump on the horizontal scale of Figure 2.

A mathematical representation of the above description is given by $t_g = \frac{V(CAV)}{p_g}$. The product CAV corresponds to the mass of the charge carriers, and the source voltage V is proportional to the height of the energy hump AE. The power-delay product, Pgtg, represents the work required to raise the mass of charge carriers to the top of the energy hump. It also embodies a primary goal of the electronics industry, namely, the decreasing of gate delay time, tg. This can be accomplished by adopting a more efficient means of cooling that permits a larger Pg , decreasing the voltages V and AV to reduce the power consumption and miniaturizing the circuit, which results in smaller capacitance, C. The thermal designer has and must continue to increase the amount of heat removed to reduce gate delay time, t_g .

Thermal phenomena also adversely affect electronics at a macro-scale Thermal gradients within packages induce stresses in chip-to-package and package-to-board interconnects, which can cause catastrophic failures in signal and power transmission. Furthermore, chip timing is affected by temperature, necessitating that systems function within relatively narrow temperature ranges to insure proper operation, frequently 10 to IS C. This is why the Cray II supercomputer is cooled using direct immersion in a dielectric fluid [20]. Therefore, at both the micro-scale and macro-scale, maintenance of a satisfactory thermal environment is essential for proper and reliable operation of an electronic system and for the development of faster systems in the future.

Recent trends within the computer market are causing the challenges of cooling today's systems to be quite different than those of the 1980's. The trend towards smaller machines that operate in the workplace strictly limits noise production, making forced convective cooling undesirable. This problem is further exacerbated in portable machines because of power consumption constraints. These trends have resulted in increased interest in cooling systems by natural convection or, if necessary, low velocity forced convection.

An alternate approach, motivated by the stringent design constraints associated with portable systems, employs conduction-augmented cooling strategies [21]. These conjugate cooling methods use system size heat spreaders or flexible heat pipes to cool essential components [22,23]. A design based on these cooling strategies is complicated by the degree of concentrated heat generation and the multimaterial/multicomponent nature of electronic systems. Futhermore, the recent success in miniaturization has resulted in fewer heat producing components and boards within a system. These systems contain localized heat sources that exhibit higher heat fluxes at fewer locations than in previous systems. Therefore, the nature of

tomorrow's electronic systems and associated cooling strategies will require conjugate analyses to insure an adequate and cost effective thermal design and, ultimately, success in the marketplace.

1.4 Motivation

In previous studies, conjugation was found to affect thermal performance characteristics. However, only parameters such as material composition and Reynolds number were independently varied to *assess* their relative effect upon temperature, flux and heat transport. The purpose of this study is to explore the fundamental effect of the distribution of internal heat generation, as well as multimaterial composition on conjugate heat transfer in grooved channels over a range of laminar and transitional Reynolds numbers. It is important for thermal analysts to understand the relative importance of non-homogeneity within the solid domain to be capable of developing accurate thermal models. Furthermore, some systems may require combined reduction of thermal resistances associated with multiple modes of heat transfer to achieve optimum, or near optimum, cooling designs. Therefore, the following four representative configurations will be investigated: (i) local heat generation with single-material composition (LS), (ii) local heat generation with multimaterial composition, (LM) (iii) uniform heat generation with single-material composition (US), and (iv) uniform heat generation with multimaterial composition (UM).

2. Problem Formulation

The mathematical model of a conjugate conduction/convection problem with incompressible flow involves a system of partial differential equations for the solid and fluid domains (Eqs. 1-3). The fluid properties are assumed constant and buoyancy forces, viscous dissipation and radiation are all neglected.

$$\frac{d\vec{v}}{\partial t} = \vec{V} \vec{X} \vec{G}) \vec{P} \vec{V} \left(p + *j - \vec{J} + \vec{W}^2 \vec{V} \right)$$
(1)

$$\mathbf{V}\mathbf{v} = 0 \tag{2}$$

$$\frac{\partial T}{\partial t} = \alpha \nabla^2 T - \vec{v} \cdot \nabla T + \frac{u'''}{\rho c_p}$$
 (3)

The boundary conditions for the momentum equation are no slip along the solid-fluid interfaces and periodicity in the strearawise direction (Fig. 3). For the energy equation, the top surface of the upper wall and the bottom surface of the lower wall are adiabatic, and periodicity is imposed in the streamwise direction by subtracting the calculated rise in mixed-mean temperature on a point-by-point basis at each streamwise location.

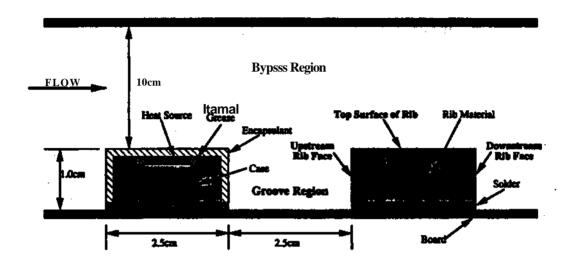


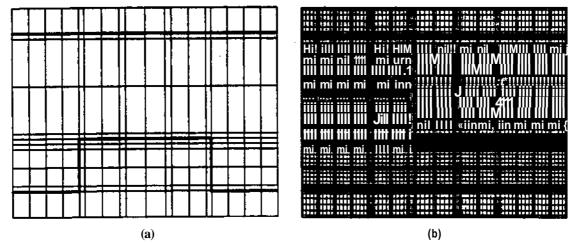
Figure 3: Schematic of ctectrontecomp^ents and material configurations

The numerical procedure employed for the spatial discretization is the spectral element technique [24, 25]. The spatial domain is decomposed into macro-elements upon which tensor products of high-order Legendre polynomials are projected. The elemental discretization used is shown in Fig. 4a, and the mesh indicating the distribution of internal nodes is shown in Fig. 4b. The control of spatial resolution and the high degree of accuracy associated with this technique makes it well suited for studying time-dependent conjugate problems with localized heat generation and multimaterial solid domains, especially those with large disparities in material properties.

The accuracy of the spectral element solution may be affected either by increasing the total number of macro-elements, obtaining algebraic convergence, or by increasing the order of the local expansions, achieving nearly-exponential convergence. Adequate resolution was verified by comparing the flow characteristics using both 7th and 9th order local expansions, as well as using different macro-elemental discretizations. The results from the simulations for the macro-elemental discretization used in this study with 7th and 9th order expansions yielded virtually identical results, indicating that the lower resolution was adequate for this investigation.

The numerical approach is to integrate the continuity and momentum equations for the fluid domain and then the energy equation for both the solid and fluid domains. This procedure is iterated in time, using a three-step, semi-implicit, time-splitting scheme, until either a steady state or time-periodic state is reached. A typical mesh consisting of 198 elements, each containing 49 degrees of freedom, requires 3.14 CPU seconds per time step on a Cray Y-MP.

The dimensions and composition of the solid domain, as shown in Fig. 3, represent a typical electronic package. The material properties and, when appropriate, the associated amount of heat generation, are displayed in Table 1. The thermal conductivities displayed in Table 1 include contact resistance, which is modeled by modifying the conductivity such that the effective thermal resistance obtained is commensurate with empirical data from Yovanovich and Antonetti [26].



Figure* Spatial discretization showing (a) macroelements and (b) collocation points. Daifcer lines indicate solid-fluid interfaces

Component	k (W/cm °C)	pc _p (KJ/cm3 «C)	u~ (W/cm3)
Case	2.04x10-!	3.47	
Heat Source	1.25×10^{-2}	1.74	5.1842
Encapsulate	6.99 x 10-3	3.16	
Board	7.4 x 10-3	2.27	
Rib Material	1.25 x 10-2	1.74	1.558 x 10'' ¹
Solder	1.0x10-3	1.47	
Thermal Grease	9.614 x 10-3	1.7 1	
Air	2.851×10^{-4}	1.534×10^{-4}	

Table 1: Material properties of the solid domain.

It should be noted that because buoyancy effects are neglected, the resulting flow patterns are independent of the solid-fluid interface temperature and heat flux distributions. Therefore, for a specific Reynolds number, the variations present in the distributions of surface temperature, heat flux, and Nusselt number are only attributable to the composition of the solid domain and the distribution of heat generation. It is this combination, along with the local-fluid characteristics, which determines the heat flow paths and, ultimately, the thermal performance characteristics of the configuration.

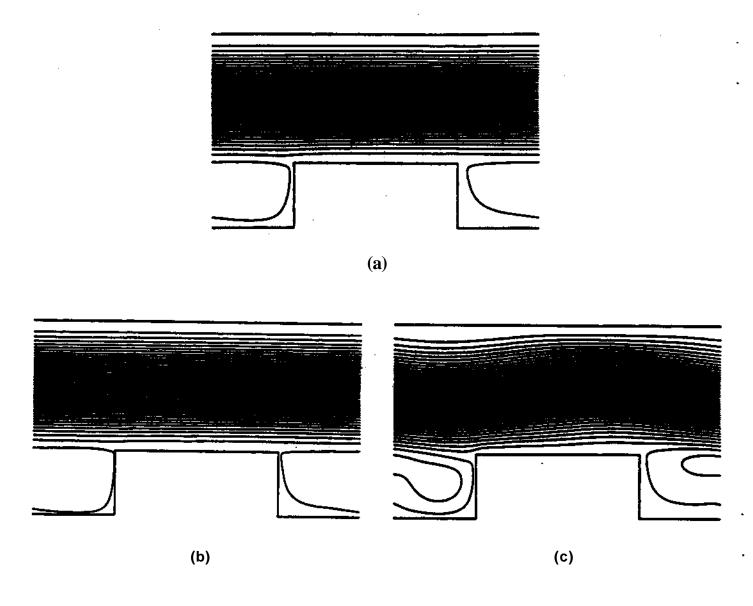


Figure 5: Contours of the streamfunction for (a) laminar, (b) slightly-transitional, and (c) transitional flow regimes

3. Flow Patterns

Three Reynolds numbers are considered for this investigation: low, middle and high. The low Reynolds number case corresponds to a laminar flow field, wherein, the fluid in the channel is separated by a shear layer from the recirculating fluid within the groove [16]. Fig. 5a displays the contours of the streamfunction corresponding to the laminar flow regime at Re=270 and a maximum streamwise velocity of 36.5 cra/s. Convective transport from the upstream and downstream rib faces is hampered by the shear layer, which inhibits direct exchange of heated groove with cooler channel fluid. Additionally, the Poiseuille-like nature of the flow in the channel results in larger shear stresses along the top of the rib than along the upstieam or downstream rib faces [27]. These effects cause greater convective resistances along the upstieam and downstream faces than along the top surface of the rib.

The middle Reynolds number case corresponds to a slightly transitional flow field. Figure 5b displays the contours of the streamfunction for this flow regime at Re=640 and a maximum streamwise velocity of 86.4 cm/s. Small amplitude oscillations, corresponding to Tollmien-Schlichting waves [28] are present within the channel flow. The amplitude of the velocity components associated with the oscillations is approximately two orders of magnitude smaller than the average streamwise velocity of the channel flow. In spite of the small amplitude of the fluctuations, the nature of the transitional flow pattern results in larger shear stresses along the surfaces of the rib [27]. However, the small magnitude of transverse momentum associated with the traveling waves is insufficient to disrupt the shear layer. Therefore, diffusion remains the dominant mode of energy exchange between the heated groove fluid and cooler channel fluid.

The flow field at the high Reynolds number is very different from either the middle or low Reynolds numbers. Figure 5c displays the instantaneous contours of the streamfunction corresponding to the transitional flow regime at Re=700 and a maximum streamwise velocity of 94.5 cm/s. This time-periodic flow contains large amplitude Tollmien-Schlichting waves in the channel. The magnitude of the velocity fluctuations is approximately one order of magnitude smaller than the average streamwise velocity of the channel flow. The increased transverse momentum of the channel flow results in the shear layer being periodically disrupted. Therefore, heated groove fluid can convect into the channel and be replaced by cooler fluid. Additionally, the shear stress along all of the rib surfaces increases significantly, which reduces the convective resistance, particularly near the upstream rib corner [27].

4. Spatial Distributions at the Solid-Fluid Interface

4.1 Temperature

Firstly, the local temperatures along the solid-fluid interface of the grooved surface are presented for each of the four configurations and for the three Reynolds numbers studied. The data presented for the middle and high Reynolds number cases are the time-average difference between the solid-fluid interface and bulk-mean temperatures, corresponding to the passing of one Tollmien-Schlichting wave. Additionally, the application of periodic boundary conditions emulates studying the thermal characteristics of heated ribs within the periodic fully-developed region. In this region, the difference between the solid-fluid interface and bulk-mean temperatures remains periodically invariant. It should be noted that periodic fully-developed behavior has been experimentally observed in similar geometries, e.g. ribbed channels, after the third or fourth component [29,30].

The interface temperature distributions for all of the cases and configurations exhibit effects associated with both rib material composition and distribution of heat generation, as shown in Figs. 6a-c. For the configurations containing local heat generation, the heat source is positioned near the top of the rib. This results in a local rise of surface temperature directly above the location of the chip.

As the Reynolds number is increased, the convective resistance is lowered near the upstream corner of the rib. However, because of conduction within the solid, variations in the interface temperature distribution are visible along portions of the top and upstream rib faces (Figs. 4b, c). The configurations corresponding to single-material composition have lower conductive resistance and exhibit a more asymmetric surface temperature distribution than those with multimaterial composition. This larger conductive resistance localizes convective effects, resulting in larger gradients, but more symmetric overall temperature distributions.

For the high Reynolds number case (Fig. 6c), the magnitude of convective transport is large enough to strongly affect the surface temperature distribution for the single-material rib configurations. In fact, the higher rate of convective transport at the leading edge of the rib results in a decrease of surface temperature along nearly sixty percent of the top surface of the rib for the uniform heat generating, single-material (US) configuration.

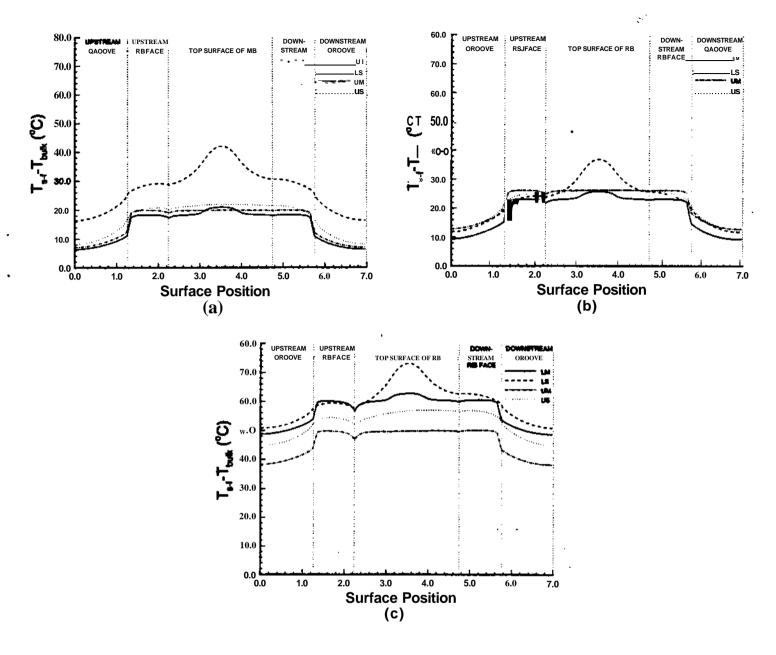


Figure 6: Solid-fluid interface and bulk-mean temperature difference versus surface position for (a) low, (b) middle, and (c) high Reynolds number cases. LM: local heat generation, multimaterial configuration; LS: local beat generation, single-material configuration, uniform beat generation, multimaterial configuration, and US: uniform beat generation, single-material configuration

4.2 Heat Flux

The local heat flux distributions are now considered for the same configurations and Reynolds numbers previously examined. As with the interface temperature distributions, the local heat flux data presented for the middle and high Reynolds number cases are time averaged over one wave cycle. Additionally, a sign convention is adopted such that heat flux leaving the solid domain at the solid-fluid interface is positive, while heat flux entering is negative.

The spatial distributions of heat flux for the three Reynolds number cases are displayed in Figs. 7a-c. As previously demonstrated, both material composition and distribution of heat generation affect the resulting patterns. All the configurations display the classical pattern associated with boundary layer growth along the top surface of the rib. However, the configurations with local heat generation display increased heat flux over the location of the heat source. This increase is especially significant for the single-material configuration (LS).

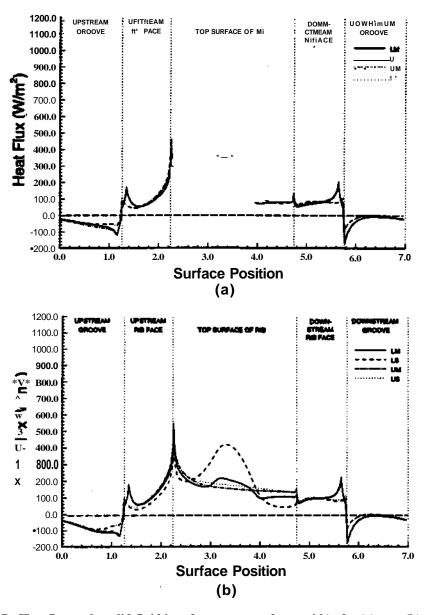


Figure 7: Heat flux at the solid-fluid interface versus surface positk)o for (a) tow, (b) mkklk, md (c) Wgh Reynolds in the cases

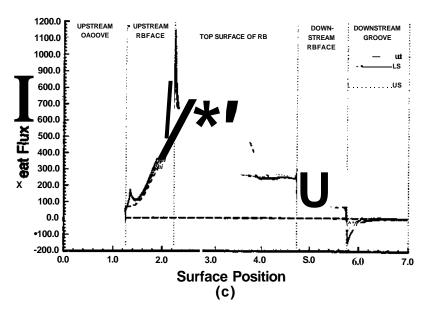


Figure 7 coot.

A local increase in heat flux for the multimaterial configurations (LM, UM) occurs along both the upstream and downstream rib faces corresponding to the location of the solder. This is attributable to the larger conductive resistance associated with the solder. The relative convective resistance from the rib face decreases with respect to the conductive resistance into the board, resulting in a local increase of heat flux.

At the low Reynolds number, there is an intact shear layer separating the groove fluid from the channel fluid. The recirculating fluid within the groove is heated along both the upstream and downstream rib faces, but the shear layer prohibits convective exchange of the heated groove fluid with cooler channel fluid. The heated groove fluid becomes hotter than the adjacent surface (board), leading to heat transfer into, rather than out of, the solid domain. However, as the flow becomes transitional and the shear layer is disrupted, some of the heated groove fluid is replaced by cooler channel fluid. This convective exchange of fluid between the groove and channel reduces the magnitude of the temperature gradient along the groove, leading to less heat flux into the solid domain for the higher Reynolds number case. An important observation is that the spatial distribution of flux along the groove surface is affected more by the distribution of heat generation than by the material composition of the rib.

As the Reynolds number increases (Figs. 7b, c), the peak value of heat flux at the leading edge of the rib increases for all conflgurations. However, the magnitude of heat flux along the latter portion of the top surface of the rib is reduced for the local heat generating conflgurations. The increased heat flux along the top of the rib, from the upstream corner to the location of the heat source, raises the temperature of the fluid in the thermal boundary layer. This increases the convective resistance in the streamwise direction, resulting in a reduction of heat flux from the later portion of the rib.

43 Nusselt Number

A classical measure of convective heat transfer is the Nusselt number, which can be interpreted as representing either the nondimensional temperature gradient at the solid-fluid interface or the magnitude of the convective heat transfer scaled by the equivalent conductive heat transfer in the fluid. However, for conjugate problems, the former interpretation is preferable because it more easily accommodates the presence of both positive and negative heat fluxes along a surface.

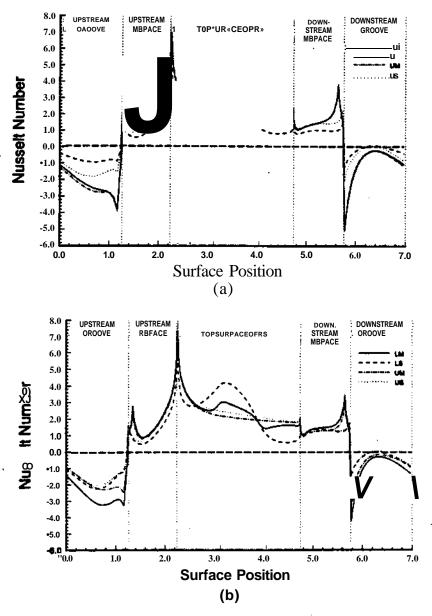


Figure 8: Nusselt number at the solid-fluid interface versus surface position for (a) low, (b) middle, and (c) high Reynolds number cases

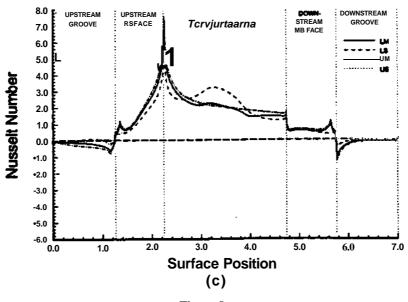


Figure 8 coot

The spatial distributions of Nusselt numbers are shown in Figs. 8a-c. Unlike the interface temperature or heat flux distributions, the magnitudes of the Nusselt number for all of the configurations are similar, but the spatial distributions are slightly different. The local heat generating configurations (LS, LM) display increases in Nusselt number above the location of the heat source. Likewise, along the upstream and downstream rib faces, the multimaterial configurations (LM, UM) display increases in Nusselt number over the regions corresponding to the location of the solder. However, there is some disparity in the distribution along the groove. The distributions corresponding to the multimaterial configurations (LM, UM) closely follow one another, particularly along the downstream portion of the groove. However, the singlematerial configurations (LS, US) do not correlate well along the upstream portion of the groove for the high Reynolds number case. The poor correspondence is associated with the larger amount of heat flux removed from the upstream rib face for the uniform heat generating case (US), after the shear layer is disrupted.

A closer inspection of the distribution along the top surface of the rib reveals a degradation in performance for the local heat generating configurations (LS, LM) after the location of the heat source, especially so for the single-material configuration (LS). As previously described, the fluid within the near-wall portion of the thermal boundary layer is heated along the rib, increasing its convective resistance, as evidenced in the Nusselt number distribution.

Although greater amounts of heat flux are achieved as the Reynolds number is increased, no comparable increases are reflected in the Nusselt number distribution (Figs. 8b, c). Furthermore, the variations in spatial distributions along the rib diminish such that the only significant difference for all, save the uniform heat generating single-material rib configuration (US), occurs above the location of the solder and the heat source. However, even the magnitude of these

differences is minimized. With increasing Reynolds number, the fluid becomes better mixed resulting in a more homogeneous thermal distribution within the flow. Therefore, differences in thermal performance caused by upstream variations in heat flux would decrease in significance.

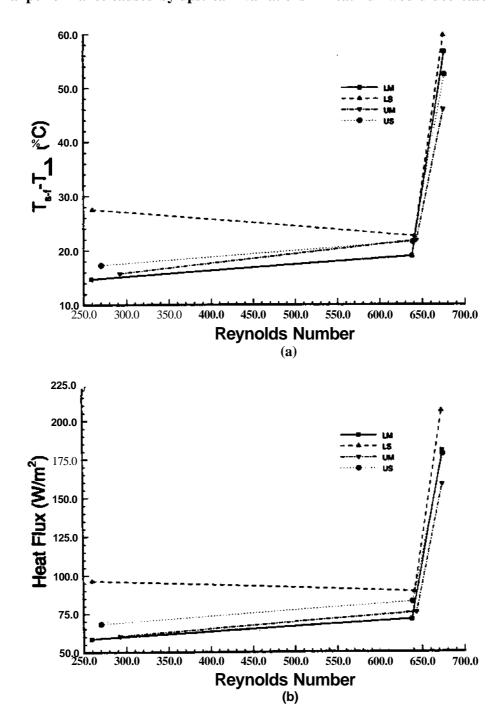


Figure 9: Time- and space-average (a) difference between the solid-fluid interface and bulk-mean temperatures and (b) beat flux at the solid-fluid interface versus Reynolds number

5. Discussion

Although there are distinct spatial variations of surface temperature, heat flux, and Nusselt number within and between the four configurations, more general behavior differences become apparent when spatially-averaged values are examined.

The averaged difference between the local solid-fluid interface and bulk-mean temperatures, as a function of Reynolds number, is shown in Fig. 9a. The temperature difference for the local heat generating, single-material rib (LS) decreases with Reynolds number in the subcritical regime. At the high Reynolds number case, the flow becomes more homogeneous and the temperature difference increases. However, the temperature difference for the other configurations continuously increases with Reynolds number, regardless of the flow regime. The key to understanding this behavior is the recognition of the relationship between the temperature rise of the fluid and the heat flux for conjugate problems.

An order of magnitude analysis of the convective boundary condition corresponding to a uniform heat flux at the solid-fluid interface yields an inverse relationship between the heat transfer coefficient and the temperature difference.

$$h(T_{s-f} - T_{bulk}) = -k, |k|_{\vec{n}} = Q$$
 (4a)

$$\mathbf{h} \propto \frac{1}{(T.-_f-T_{\text{bulk}})} \tag{4b}$$

The well-known solution for convective heat transfer over a flat plate, with an imposed uniform heat flux boundary condition, states that the heat transfer coefficient is proportional to the Reynolds number to the one-half power. Therefore, the inverse relationship shown in Eq. 4b implies that as the Reynolds number is increased, the wall temperature approaches the bulk-mean temperature. This behavior has also been demonstrated for convective heat transfer from a grooved channel with an imposed uniform heat flux boundary condition [16]. However, an order of magnitude analysis for the conjugate boundary condition reveals a different relationship.

$$Q = -k_{s} \frac{\partial T_{s}}{\partial \tilde{n}} - \frac{\partial T_{f}}{\partial H} (5a)$$

$$Q = -k_{s} \frac{\partial T_{s}}{\partial \tilde{n}} - \frac{k_{f}}{H} (T_{s-f} - T_{bulk})$$

$$Q \propto (T_{s-f} - T_{bulk})$$
(5b)
(5c)

Namely, the difference between the solid-fluid interface and bulk-mean temperatures is directly proportional to the heat flux (Eq. 5c). As predicted, the spatially-averaged heat flux, displayed in Fig. 9b, exhibits the same behavior characteristics as the temperature difference.

Physically, energy converted from the rib surface into the fluid increases its bulk-mean temperature. However, when there is little transverse mixing in the flow, the heat removed from the rib results in a nonhomogeneous temperature distribution. Therefore, the temperature distribution within the fluid depends upon the spatial distribution of heat flux along the solid-fluid interface and the flow patterns. The local heat generating, single-material configuration (LS, Figs. 7 and 9b) exhibits significantly higher heat flux from the top surface of the rib than the other configurations. This distribution of heat flux raises the fluid temperature within the boundary layer above the rib more than for the other configurations. The thermal wake that extends from the preceding rib increases the convective resistance along the top surface of the rib, reducing convective rates. Therefore, until the local flow patterns produce a more homogeneous temperature distribution within the fluid, the difference between the solid-fluid interface and bulk-mean temperatures will be larger for this configuration than for the others.

For the high Reynolds number case, the channel flow becomes non-parallel and the shear layer is disrupted, increasing significantly the heat flux along the upstream and downstream rib faces, especially for the uniform heat generating configurations (US, UM). The periodic disruption of the shear layer converts the heated fluid from the groove into the channel. This heated fluid is converted further into the channel, resulting in a lower temperature rise in the fluid directly adjacent to the rib. However, the increased conductive resistance within the multimaterial configurations (LM, UM) reduces the amount of flux removed from the upstream and downstream rib faces. Therefore, the distribution of heat generation dictates the qualitative behavior while the material composition dictates the quantitative performance.

Next, the spatially-averaged Nusselt number is considered as a function of the Reynolds number in Fig. 10. The effect of convective resistance along the top surface of the rib is visible in the spatially-averaged Nusselt number. The spatially-averaged Nusselt number for the local heat generating configurations (LS, LM) decreases with Reynolds number in the subcritical regime and then increases, once the flow becomes supercritical and better mixed. However, the spatially-averaged Nusselt number for the uniform heat generating configurations (US, UM) continuously increases with Reynolds number due to the spatial distribution of heat flux, as previously described.

The uniform heat generating, single-material configuration (US) displays the closest behavior to a non-conjugate analysis, followed by the uniform heat generating, multimaterial configuration (UM). Qualitatively, problems which involve complex flow behavior, including time- and spatially-dependent separation and reattachment, as well as intense heat transfer, multimaterial solid domains and localized heat generation [1], require conjugate formulations. This insight is required for the successful construction of heat transfer correlations for conjugate

heat transfer problems. It also indicates that the construction of such correlations might be an exceedingly difficult task for systems that exhibit strong conjugate effects and non-monotonic relationships with respect to Reynolds number.

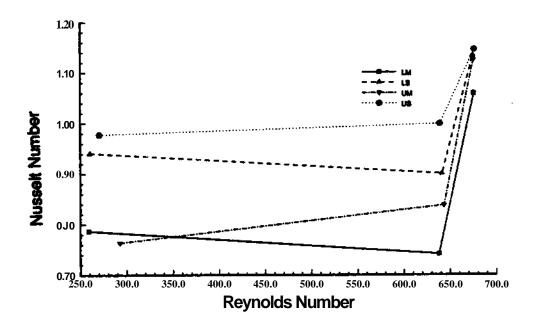


Figure 10: Time- and space-average Nusselt number versus Reynolds number

Conclusions

Conjugate conduction/convection heat transport in electronic cooling configurations is investigated for single and multimaterial components, as well as for local and uniform distributions of heat generation. At the solid-fluid interface of the components, the spatial distributions of temperature, heat flux and Nusselt number demonstrate variations associated with both material composition and distribution of heat generation. Furthermore, negative heat fluxes and Nusselt numbers are obtained along portions of the groove surfaces for all the configurations and Reynolds numbers explored.

Thermal energy converted from the top surface of the rib creates a thermal wake that extends downstream. The lack of small scale mixing within the fluid, in these flow regimes, results in incomplete homogenization of the thermal wake causing increased convective resistance along the top surface of the following rib. This resistance is found to be more strongly influenced by the distribution of internal heat generation than by the material composition.

The resulting spatially-averaged convective characteristics indicate that a thermal analyst should account for concentrations of heat generation within systems such as electronic packages, while multi-material composition is not as essential. This is an important consideration when large systems are being analyzed that tax current computational capabilities.

It has been demonstrated that conjugation produces significant variations in thermal characteristics for the configurations studied, especially for those involving spatial variations in both material composition and internal heat generation. Therefore, conjugation can significantly alter thermal behavior and should be considered in problems involving spatial variations in material composition and heat generation.

Acknowledgments

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Symbols

c_p specific heat

h heat transfer coefficient = $Q/(T_{s \cdot f} - T_{bu}ik)$

H half-channel height

k thermal conductivity

ii outward normal with respect to solid surface

 $Nu \quad \ \ Nusselt \ number = (hH)/k_f$

P pressure

O heat flux

Re Reynolds number = (3VH)/(2v)

t time

T temperature

velocity

u'" internal heat generation

V channel-averaged velocity

Greek Symbols

- v kinematic viscosity
- a thermal diffusivity
- (O vorticity
- p density

Subscripts

bulk bulk-mean temperature at leading edge of the rib

- f fluid
- s solid
- s-f solid-fluid interface

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