Influence: A Quantitative Approach for Data Integrity

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Abstract

A number of systems employ dynamic taint analysis to detect overwrite attacks in commodity software. These systems are based on the premise that low-integrity inputs should not control values such as function pointers and return addresses. Unfortunately, there are several programming constructs that can cause false positives and false negatives in these systems, which are currently handled by manual annotation, ad-hoc rules, or not at all.

In this work we propose to use channel capacity, a quantitative measure of information flow, as a quantitative measure of control. When measuring control, we refer to this measure as influence. We use influence as a theoretical tool to formally investigate programming constructs known to be problematic for dynamic taint analysis.

While calculating influence in arbitrary programs is undecidable in the general case, we propose and implement practical techniques for automatically bounding and probabilistically estimating influence in x86 programs. We show that this tool is able to find useful influence bounds in code constructs known to be problematic in dynamic taint analysis. We also use it to analyze a dynamic taint analysis alert in Samba, showing that it is a false positive, and another alert in SQL Server, showing that it is a true positive.

1 Introduction

Dynamic taint analysis has lately been a popular technique for enforcing Biba low water-mark [4] data integrity policies in commodity software [7, 9, 20, 21, 23]. In this work, we refer to such systems as Dynamic Taint Analysis for Data Integrity, or DTADI, systems. The premise behind DTADI systems is that low-integrity inputs, such as data read from the network, should not exert control over high-integrity operations, such as dereferencing a function pointer. In such systems, low-integrity inputs are marked as tainted. The output of every program operation is marked as tainted if any operand is tainted, and untainted otherwise.

The systems then monitors high-integrity operations to detect when they are about to use tainted data. Such systems have been found to be useful for detecting overwrite attacks; for example when a buffer overflow allows an attacker to overwrite a function pointer, that function pointer will be marked as tainted, and the attack detected when the function pointer is dereferenced.

A challenge in implementing DTADI systems is that in real-world programs, low integrity inputs do legitimately exert some control over high-integrity operations. In such cases, the low integrity input is usually used to select from a relatively small set of legitimate values. If a DTADI system were to propagate the taint attribute for every operation where a tainted operand could affect the output value, a large number of integrity violations would be detected that are not actually attacks; i.e. the system would have many false positives. For example, a function pointer may be set to point to one of a few request-handling functions, depending on a request-type specified by a low-integrity input.

Current DTADI systems address this challenge by only propagating the taint attribute for operations where the input is deemed to have “a lot” of control over the output. Typically, this means direct assignment, i.e. data movement and arithmetic instructions. Indirect assignments, such as via if-then-else structures, are ignored because they typically give the input relatively little control over the value of the assignment. Assignment via indexing operations, such as loading data via a tainted pointer, are also sometimes ignored due to the prevalence of using an untrusted input to calculate an offset into a relatively small table. Considering again the case where a low-integrity input is allowed to select a function-pointer, these taint propagation policies can prevent false positives when the function-pointer is selected via an if-then-else statement or loaded from a table, while still detecting if the input is able to directly overwrite the function pointer via a buffer overrun.

There are two fundamental problems with the taint propagation policies in current DTADI systems. The first problem is that they are manually specified in an ad-hoc manner,
based on an intuitive understanding of which operands exert “a lot” of control over the result. The resulting policies do not work in every situation, and can grow complex as special cases and exceptions are added to improve accuracy. For example, most current DTADI systems recognize some common program operations where the output does not depend on the input, such as when a register is xored with itself, or bit-masked with zero. To our knowledge, such exceptions have been added to DTADI systems manually, in an on-demand basis when such operations are found to otherwise cause inaccuracy.

The second problem with the taint propagation policies in current DTADI systems is that they typically operate at a very fine-grained level; e.g. individual x86 instructions, or even individual micro-code instructions that the x86 instructions are first broken into. At this level, important interactions between instructions and cumulative effects of instructions are lost. For example, consider the program: if (a == 0) b := 0; if (a == 1) b := 1; ...; if (a == 255) b := 255. At the level of analyzing the individual conditional jump, jump, and move x86 instructions that this program would be compiled into, there is no interaction between a and b. At the level of examining an individual if structure, a appears to have little control over the value of b: a effectively selects one of two values for b. Only by looking at the whole sequence of if statements can we see that a is effectively copied to b.

The result of these problems is that current DTADI systems suffer from both false positives and false negatives. False positives occur when data used in a high-integrity operation is derived from low-integrity inputs, after being constrained by arithmetic manipulation or sanity checks to ensure the resulting value is within an expected range. False negatives occur when low-integrity inputs effectively control the value of another variable, but in an indirect way such as via implicit data flows. The previous example using if-then-else statements is such an example.

In this work we show that channel capacity, a measure used to formally quantify how much information flows from one object to another within a program, is also a useful tool for formally quantifying how much control one object has over another within a program. In the context of measuring control we refer to this measure as influence. As a theoretical tool, influence provides a formal basis for thinking about and evaluating current DTADI taint propagation policies. In Section 4, we use influence to formally reason about program structures that are difficult to reason about with current DTADI taint propagation policies.

We also demonstrate methods for automatically reasoning about influence in binary x86 programs. Unfortunately, calculating the exact influence of one object over another in an arbitrary x86 program is undecidable in the general case, and computationally expensive for large programs. However, we build a tool that can exactly measure influence in small loop-free programs, and on general x86 programs can be used to calculate useful lower bounds, upper bounds, and probabilistic estimates of influence. This tool does not suffer from the problems of DTADI taint propagation policies of requiring ad-hoc manual propagation rules, and it can in theory be evaluated over arbitrarily large program structures instead of operating at the per-instruction level. The current tool is too computationally expensive to calculate the influence of every low-integrity input over every high-integrity operation in a real-world program, and does not aim to replace DTADI systems. However, it is practical for performing a deeper analysis of alerts generated by DTADI systems. We use it to examine two alerts generated by a DTADI tool on real-world x86 programs, confirming an alert in SQL Server as an integrity violation, and showing that an alert in Samba is likely a false positive. In Section 8 we suggest future directions for using our techniques to improve the accuracy and performance of DTADI systems.

The contributions of this work are:

- We propose channel capacity as a formal quantitative measure of control. In this context, we refer to channel capacity as influence.
- We use influence to formally investigate program structures that are problematic for systems that use dynamic taint analysis to enforce data integrity (DTADI).
- We build a tool that can automatically reason about influence (and equivalently, channel capacity) in binary x86-programs.
- We use our influence measurement tool to analyze alerts generated by a DTADI system on real-world software. We find that one is a false positive, and verify the other as a true positive.

2 Related Work

2.1 Dynamic taint analysis for data integrity

A number of systems have been proposed to perform dynamic taint analysis to enforce Biba low-water-mark data integrity policies on x86 binary programs, for the purpose of detecting overwrite attacks [7, 9, 20, 21, 23]. While these approaches work well for many programs, they propagate the taint attribute at the instruction level, using ad-hoc rules about which operands exert “a lot” of control over the result of each operation. As a result, none employ general solutions for handling sanity checks, implicit flows, or identity functions. These systems do recognize and handle some common-cases of these problems.
Xu et al. [26] implement a system to rewrite the C source code of a program to perform dynamic taint analysis. They detect implicit flows that occur in some C-level if-then-else structures.

2.2 Dynamic taint analysis for data confidentiality

Dynamic taint analysis has also been used by several systems to enforce Bell-LaPadula [3] data confidentiality policies [6, 14, 17, 27]. The implementations of these systems are similar to taint analysis systems used to enforce data integrity. Instead of marking low-integrity inputs as tainted, these systems mark confidential data as tainted, and check whether tainted data is written to untrusted outputs. These systems propagate the taint attribute based on whether an operand leaks “a lot” of information to the result of an operation. In practice, the taint propagation policies in these systems are very similar to those in DTADI systems, though they are often tuned to propagate the taint more aggressively. The implementations of these systems proposed by Egele et al. [14] and by McCamant et al. [17] also employ some static analysis to account for positive implicit flows, but do not handle negative implicit flows without manual annotation.

McCamant et al. [17] use taint analysis to quantitatively bound how much information about a secret input may have leaked. They track the taint attribute at the bit level, as well as keeping a global leakage counter. The global leakage counter is used in several ways; in particular it is incremented when a branch depends on a tainted input, thus accurately bounding leakage due to positive implicit flows. They calculate the upper bound of the number of bits leaked as the number of tainted bits sent to the output, plus the global leakage counter. Negative implicit flows are not accounted for, unless annotations are added to increment the global leakage counter. The total information leakage bound is kept reasonable using some manual annotations to pre-emptively mark bits as leaked at certain program points before their taint attribute can be propagated to a larger number of bits.

2.3 Information flow

There is a large body of work on information-flow security. Sabelfeld et al. provide a good survey of the field [22].

Most prior work seeks to detect or prevent any flow of sensitive data to an insecure output. Vachharajani et al. [24] propose and implement a system to dynamically detect unpermitted information flows in binary programs. Venkatakrishnan et al. [25] propose a provably correct system to enforce non-interference for a small well-structured language; they are able to track implicit flows using the structure of their proposed language.

Denning first proposed to quantitatively measure information flow [12], defining the amount of information transferred in a flow as the reduction in uncertainty (entropy) of a random variable. Other seminal work in quantitative information flow was done by Millen [18] and by Gray [15]. Clark et al. [10, 11] and Malacaria [16] propose frameworks for measuring how much information is leaked by programs written in simple imperative languages.

3 Influence: quantifying control

Our first step is to formally define a useful quantitative measure of control. We begin by defining a measure we call influence, based on an intuitive understanding of control. We then show that the influence of one variable over another is exactly equal to the maximum information flow, or channel capacity, between those two variables.

3.1 Program model

Let \( P \) be a program, or program structure, that takes a set of inputs, and deterministically computes a set of outputs. We partition the inputs into two sets: \( \text{LOW} \), which is the set of (low integrity) inputs which we wish to track, and \( \text{HI} \), which is the set of all other inputs that the program takes. Formally, we have: \( P(\text{LOW}, \text{HI}) = \text{OUT} \). While we allow the domains of \( \text{LOW} \) and \( \text{HI} \) to be infinite, we assume that the domain of \( \text{OUT} \) is finite. Our goal is to characterize how much control \( \text{LOW} \) has over \( \text{OUT} \).

For simplicity, we represent \( \text{LOW} \), \( \text{HI} \), and \( \text{OUT} \), each as a single scalar variable that \( P \) reads from or writes to. Other forms of input and output can be transformed to fit this model; e.g. socket reads and writes can be represented as reading some range of bytes from \( \text{LOW} \) and writing to some range of bytes in \( \text{OUT} \).

3.2 Influence

Intuitively, how much control \( \text{LOW} \) has over \( \text{OUT} \) is related to the number of different values that \( \text{LOW} \) can cause \( \text{OUT} \) to take on. If \( \text{OUT} \) always takes on the same value, regardless of the value of \( \text{LOW} \), then \( \text{LOW} \) has no control over \( \text{OUT} \). At the other extreme, if selecting an appropriate value of \( \text{LOW} \) can cause \( \text{OUT} \) to take on any value in the codomain of \( P \), then \( \text{LOW} \) has maximal control over \( \text{OUT} \).

We propose to measure the control that \( \text{LOW} \) has over \( \text{OUT} \) as influence, which we denote \( C \). We define the influence of \( \text{LOW} \) over \( \text{OUT} \), given a particular assignment of \( \text{HI} \), as the log of the size of the range of \( P \) for the given assignment of \( \text{HI} \). For convenience, we take the log base 2, which allows us to measure influence in bits. Formally:
\( C(\text{LOW} \rightarrow \text{OUT}|\text{HI} = \text{hi}) = \log \{ \text{out}|\text{low} : P(\text{low}, \text{hi}) = \text{out} \} \).

To show that this is intuitively a useful measure for control, we consider a few simple examples. If \( \text{OUT} \) takes on the same value regardless of \( \text{LOW} \), the influence is zero bits. If selecting \( \text{LOW} \) can cause \( \text{OUT} \) to take on any value in the codomain of \( P \), then the influence is exactly the number of bits needed to represent \( \text{OUT} \). In cases where \( \text{LOW} \) is able to freely overwrite \( n \) bits of \( \text{OUT} \), then \( \text{LOW} \) has \( n \) bits of influence over \( \text{OUT} \).

Note however that influence is more informative than tracking a binary attribute for each bit of whether \( \text{LOW} \) can affect that bit, because it takes dependencies between bits into account. For example, suppose that \( \text{LOW} \) can cause a 32-bit \( \text{OUT} \) to have a value of all zero-bits or all one-bits, but no other values. Although \( \text{LOW} \) can affect the value of all 32 bits of \( \text{OUT} \), it has much less control over \( \text{OUT} \) as a whole than if \( \text{LOW} \) could cause \( \text{OUT} \) to take on all \( 2^{32} \) combinations of ones and zeroes. The influence measure reflects this; since \( \text{LOW} \) can only cause \( \text{OUT} \) to take on one of two different values, the influence is only \( \log 2 = 1 \) bit.

### 3.3 Equivalence to channel capacity

We now show that the influence of \( \text{LOW} \) over \( P \) when \( \text{HI} \) is \( \text{hi} \) is exactly the maximum information flow, or channel capacity, from \( \text{LOW} \) to \( P \), given that \( \text{HI} \) is \( \text{hi} \), and that the fact that \( \text{HI} = \text{hi} \) is known. Intuitively, the concepts of control and information flow are tightly linked. As we describe in Section 2, dynamic taint analysis has been used both to propagate the flow of control and the flow of information. Hence, it is unsurprising that a quantitative measure of control turns out to be a well known quantitative measure of information flow.

Using Denning’s definition of quantitative information flow [12], the amount of information that flows from \( \text{LOW} \) to \( \text{OUT} \), given the known assignment \( \text{HI} = \text{hi} \), is the expected reduction of entropy of \( \text{LOW} \), given \( \text{OUT} \), or given the known assignment of \( \text{HI} \):

\[
I(\text{LOW} \rightarrow \text{OUT}|\text{HI} = \text{hi}) = H(\text{LOW}|\text{HI} = \text{hi}) - H(\text{LOW}|\text{OUT}, \text{HI} = \text{hi}).
\]

This in turn is equivalent to the mutual information of \( \text{LOW} \) and \( \text{OUT} \) given \( \text{HI} \), which can be expressed as \( H(\text{OUT}|\text{HI} = \text{hi}) - H(\text{OUT}|\text{LOW}, \text{HI} = \text{hi}) \). Using these relationships, and the fact that the entropy of \( \text{OUT} \) given \( \text{LOW} \) and \( \text{HI} \) is zero (because \( P \) is a deterministic function), we find that the information flow is simply the entropy of \( \text{OUT} \), given the assignment of \( \text{HI} \):

\[
I(\text{LOW} \rightarrow \text{OUT}|\text{HI} = \text{hi}) = H(\text{OUT}|\text{HI} = \text{hi}) - H(\text{OUT}|\text{LOW}, \text{HI} = \text{hi}) = H(\text{OUT}|\text{HI} = \text{hi})
\]

Channel capacity is the maximum information flow for all probability distributions of \( \text{LOW} \) [12]. In this case, the probability distribution of \( \text{LOW} \) that maximizes information flow is the distribution that maximizes the entropy of \( \text{OUT} \).

Given the standard definition of entropy of a random variable \( X \) as \( H(X) = \sum p(X = x) \log \frac{1}{p(X = x)} \), the entropy of \( \text{OUT} \) is maximized when all possible values of \( \text{OUT} \) are equally likely. In that case, the entropy of \( \text{OUT} \) is equal to the log of the number of values that \( \text{OUT} \) can take on, which is exactly the influence of \( \text{LOW} \) over \( \text{OUT} \).

Therefore the channel capacity of the information flow from \( \text{LOW} \) to \( \text{OUT} \) is exactly equal to the influence of \( \text{LOW} \) over \( \text{OUT} \):

\[
\max \forall \mu : I((\text{LOW} \sim \mu) \rightarrow \text{OUT}|\text{HI} = \text{hi}) = C(\text{LOW} \rightarrow \text{OUT}|\text{HI} = \text{hi})
\]

### 3.4 Influence variations

We next consider some useful variations of influence.

#### 3.4.1 Partial influence

There are several cases where it is useful to consider influence considering a subset of possible values of \( \text{LOW} \), rather than over the entire domain of \( \text{LOW} \). The range of \( P \) when considering only a subset of its domain is, of course, a subset of the actual range. Therefore, the influence calculated over a partial domain is a lower bound of the actual influence. We refer to the influence calculated over a partial domain as partial influence.

The most obvious reason to use partial influence is in cases where it is difficult or impossible to calculate the influence over the entire domain of \( \text{LOW} \), such as some cases where the domain of \( \text{LOW} \) is of infinite size. We use this technique in Section 6 to reason about influence in large x86 programs.

Partial influence can also be used to reason about a particular value of \( \text{LOW} \), or a particular class of values of \( \text{LOW} \). As we have defined it, influence is independent of any actual value of \( \text{LOW} \); it is a property of the program \( P \) itself. In Section 5.2 we show how partial influence can be used to help classify whether a particular value of \( \text{LOW} \) exploits an overwrite vulnerability.

#### 3.4.2 Max influence

So far, we have only defined influence as parameterized for a particular value of \( \text{HI} \). This formulation is useful when \( \text{HI} \) is known, e.g., when dynamically determining the influence for a particular execution of the program in question.

For applications where \( \text{HI} \) is unknown, such as when performing static analysis, it would be useful to consider a variation of influence calculated over all possible values of
HI. Usually, it would be most useful to find the maximum influence over all values of HI. This is a measure of the most control that LOW could have over OUT.

4 Influence analysis of problematic program structures

In this section, we examine several program structures that can cause DTADI tools to give incorrect results. For each structure we give simple concrete examples, explanations of when they occur in real programs, explanations of why they are difficult for DTADI tools to handle, and finally we show how the influence measure handles each case. Note that the influence measures stated in this section are calculated by manual inspection. We describe methods for automatically calculating influence in Section 6, and use those methods to analyze these and other programs in Section 7.

In each concrete example, we examine the taint propagation from LOW to OUT, and the influence of LOW over OUT. LOW and OUT are both 8 bit unsigned integers. For simplicity, most of these examples do not depend on HI.

4.1 Sanity checks

We first examine sanity checks implemented by conditional execution: cases where OUT is only derived from LOW after LOW has been found to be within some acceptable range.

Example 1 Sanity check

```plaintext
if LOW < 16 then
  OUT := base + LOW
else
  OUT := base
end if
```

In Example 1, OUT is derived from LOW only when LOW has been verified to be less than 16. Taint analysis tools do not take such sanity checks into account, and OUT will be considered tainted.\(^\text{2}\)

To calculate influence, we observe that for any LOW, OUT can have one of 16 values, from (base+0) to (base+15). Therefore, the influence of LOW over OUT is 4 bits. While LOW has some control over OUT, it does not have a full 8 bits of control over the 8 bit OUT.

We have observed such structures in real programs. In particular, we have verified that the gcc C compiler compiles some switch statements by performing a check on the switch variable, and then using it to calculate an address, which is used in an indirect jump. While the sanity check makes this structure safe, DTADI tools detect this as a security violation when the switch variable is tainted.

As far as we are aware, the only way to work around such cases in current DTADI is to manually annotate the code structure, e.g. to force LOW to be untainted after the sanity check, or to ignore the specific integrity violations that are detected as a result of OUT being marked tainted. In addition to requiring manual intervention, care must be taken not to introduce other inaccuracies with such annotations.

4.2 Arithmetic restriction

Example 2 Arithmetic restriction: mask

```plaintext
OUT := base + (LOW & 0x0f)
```

A similar problem occurs when arithmetic is used to restrict the range of a calculation. Example 2 is equivalent to Example 1, but instead of restricting what inputs may be used via control-flow, it instead simply masks off the bits that could cause OUT to take on an undesired value. It is possible that some switch structures may be compiled in this way.

All DTADI tools that we are aware of would consider OUT to be tainted in this case, which could lead to false positives. As with Example 1, this problem can be addressed with manual annotations.

The influence of LOW over OUT in this example is again 4 bits, which is expected since the end result of this example is identical to Example 1.

Example 3 Arithmetic restriction: identity functions

```plaintext
OUT1 := LOW XOR LOW
OUT2 := LOW & 0
OUT3 := 0; OUT3 := OUT3 + LOW; ...; OUT3 := OUT3 - LOW
```

Example 3 shows several examples where, while a na"ive analysis may conclude that OUT is derived from LOW, the final value of OUT actually does not depend on LOW at all. In these examples, all three OUT variables have the value 0 at the end of the program. Hence, these kinds of structures can lead to false positives.

DTADI tools that we are aware of detect some of the common structures of this nature, using a precompiled list of idioms. In particular, many compilers exclusive-or a register with itself to initialize it to zero, and all the DTADI tools that we are aware of mark the result of this instruction as untainted.

\(^\text{2}\)DTADI tools may only consider OUT tainted when LOW passes the sanity check, since otherwise the derivation from LOW does not take place.
However, in the general case, detecting such cases is non-trivial. Especially consider OUT in the example above. In this case, examining either assignment in isolation makes it seem that OUT is derived from LOW. It is only by examining the higher-level structure of the program that we can determine that the final value of OUT does not depend on LOW at all. We further examine this challenge in Section 6.1.

The influence of LOW over each OUT variable is 0 bits, since each OUT can take on exactly 1 value, regardless of the value of LOW.

### 4.3 Table lookup

There are several ways in which low integrity inputs can be used to select other data. One of the most ubiquitous ways is via a table lookup.

**Example 4 Table lookup**

\[
\text{OUT} := \text{table}[	ext{LOW}]
\]

In Example 4, LOW is used as an index into a table. We assume for the sake of this example that the contents of this table are untainted. DTADI tools that we are aware of optionnally mark OUT tainted in this case, using a rule that data loaded via a tainted pointer is also tainted. As we demonstrate in Section 7.1.3, enabling this rule can cause taint analysis to have false positives, and disabling this rule can cause taint analysis to have false negatives.

The actual influence depends on the contents of the table, which is not shown. For example, if each entry in the table is unique, then OUT can take on 256 unique values, and the influence is 8 bits. Otherwise, the influence is less than 8 bits. In the extreme case where every table entry contains the same value, the influence is 0 bits. In programs where the contents of the table are not constant, the table can be considered to be part of HI.

This case occurs frequently in real programs. This technique is often used to translate input from one character set to another. We have observed functions such as toupper and tolower implemented in this way. We have also observed this technique used to select a request-handling function pointer in samba (see Section 7.1.3).

### 4.4 Implicit flows

Another way that tainted data can be used to select untainted data is via control flow.

In Example 5, the final value of OUT is equal to LOW (assuming LOW is 8 bits), yet there was never a direct assignment from LOW to OUT. In the information flow and taint analysis literature, this is referred to as an implicit flow.

**Example 5 Implicit flow**

```plaintext
if LOW == 0 then
  OUT := 0
else if LOW == 1 then
  ...
else if LOW == 255 then
  OUT := 255
end if
```

The influence of LOW over OUT in this example is 8 bits, since OUT can take on 256 unique values.

DTADI tools do not track implicit flows, and would consider OUT to be untainted, which could lead to false negatives. Some taint analysis tools that are used for confidentiality rather than integrity [14, 17] detect positive implicit flows, which are implicit flows that result from an executed assignment that is control-dependent on LOW. However, none that we are aware of detect negative implicit flows, which are implicit flows that result from an unexecuted assignment that is control-dependent on LOW, without the assistance of manual program annotations.

To clarify, suppose the program is executed with LOW set to 4. In that case, the assignment (OUT := 4) is a positive implicit flow, and all the other assignments are negative implicit flows. A bound calculated over the positive implicit flows would approximate that the previous 4 untaken branches could have each leaked at most 1 bit of LOW. However, because of the negative implicit flows (the other branches that are never reached) the influence over, and information leakage to, OUT is actually all 8 bits of LOW.

These types of structures can be used to translate input from one format to another. In particular, keyboard input is propagated via implicit flows in the Windows keyboard driver [6].

### 5 Using influence to identify attacks

As we have shown in Section 4, influence is a useful theoretical tool for reasoning about how much control LOW has over OUT. However, in the context of detecting integrity violations, there are two questions that must be addressed: how much influence signifies an integrity violation, and how do we use influence to determine whether a particular value of LOW is malicious?

#### 5.1 Quantitative integrity policies

As we discussed in sections 1 and 4, current DTADI systems propagate a binary taint attribute at a per-instruction granularity. Ad-hoc rules are used to specify which inputs of a particular instruction have enough control over each output of that instruction to justify propagating the
taint attribute. Using influence, it is possible to specify an integrity policy based on a quantitative threshold of how much influence low-integrity inputs may have over given high-integrity operations, rather than based on a collection of taint-propagation rules. Due to their simplicity, we believe that quantitative policies will be easier to create and understand. Additionally, sensitivity of such policies can be tuned by simply adjusting a numeric threshold rather than attempting to modify or create new qualitative taint-propagation rules.

As an example, we consider one of the types of attacks that DTADI systems are used to detect: when a low-integrity input overwrites a function pointer or return address. The policy used in current systems is specified roughly as “data derived from low-integrity inputs should not be loaded into the program counter,” where derived is defined by the collection of taint-propagation rules. Using influence, we can specify a quantitative policy such as “low-integrity inputs should not have more than $t$ bits of influence over a value loaded into the program counter,” where $t$ is a simple numeric threshold.

Selecting a threshold $t$ for this policy is fairly straightforward. It is common for untrusted inputs to be able to specify a function pointer from a small set of valid values (e.g., handlers for different request types), so setting $t$ to zero would certainly result in false positives. To our knowledge, though, situations where a low integrity input is able to legitimately choose from more than a handful of pointers are rare. Hence, setting $t$ to a small value such as 6 bits (allowing the low integrity input to select from up to $2^6 = 64$ different choices), would likely result in few false positives. In theory, any non-zero value for $t$ could result in false negatives if a vulnerability allowed the input to overwrite only a few bits of the target pointer. However, we are unaware of any such vulnerabilities, and such a vulnerability would be relatively challenging to exploit in a useful way.

Another advantage of using a threshold-based integrity policy is that different thresholds may be set for different high integrity operations. For example, while it is common for a low integrity input to legitimately have a few bits of influence over a function pointer, a low integrity input should never have any influence over a return address.

### 5.2 Identifying malicious values of low-integrity inputs

Influence is a property of a program, not a property of a particular input value. Hence, in the general case, influence can be used to identify a vulnerability, but does not indicate whether a particular value $\text{LOW}$ of $\text{LOW}$ is an attack.

One way to use influence to determine whether a particular value of $\text{LOW}$ is an attack is to calculate the influence over $\text{OUT}$ for some class of value of $\text{LOW}$, to which $\text{LOW}$ belongs. This is done by calculating the the influence for a partial domain of $\text{LOW}$, as described in Section 3.4.1.

For example, the security violation in most overwrite attacks is that a calculated pointer used in a memory-store operation points to an unintended destination; e.g., outside of the intended buffer in the case of a buffer overflow. Leveraging this observation, we can determine whether the value $\text{LOW}$ results in a buffer overflow by calculating the influence over $\text{OUT}$ for the set of values of $\text{LOW}$ that would cause all memory store operations to write to the same address as $\text{LOW}$ does. When $\text{LOW}$ is a value that results in a buffer overflow, this influence measure will be high. When $\text{LOW}$ is a value that does not result in a buffer overflow, inputs that write outside of the intended buffer will not be considered in the influence calculation, and the calculated influence will be low (or zero).

### 6 Measuring influence in binary programs

We next investigate how to automatically measure influence in real binary programs. We show that while it is possible to leverage previous work in taint analysis and information flow analysis, all previous approaches we are aware of are forced to over-approximate, and in practice require manual annotation to calculate useful bounds. We propose a new approach, which is the first that can calculate a sound lower-bound of influence. It can also calculate an upper-bound that is sound for certain cases and useful in practice, and in some cases can soundly calculate the exact influence.

#### 6.1 Transfer-functions are forced to over-approximate

Recall again that influence is defined as the log of the size of the range of a program $P$, for some particular assignment to high-integrity inputs $\text{HI}$. We briefly discuss several possible approaches for calculating influence, using Example 6 as a motivating example. In this example, $\text{OUT}$ can only take on one possible value: 0x0. As a result, the influence of $\text{LOW}$ over $\text{OUT}$ is 0 bits.

**Example 6** Inter-dependent operands

```c
if predicate(LOW) then
    a := 0x01; b := 0x10
else
    a := 0x10; b := 0x01
end if
\text{OUT} := a \& b
```

We first consider the approach of using transfer functions, which is the approach of all previous mechanisms of which we are aware for calculating taint or information flow. In these approaches, a transfer function is defined for
each statement in the language, which defines how execution of the statement affects the tracked attribute for each variable. One way of utilizing this approach, which is the most analogous to previous approaches for quantitative information flow tracking, is to track the number of different values that each variable can take on. In Example 6, analysis of the if-then-else structure would determine that \( a \) and \( b \) can each take on two different values. With only this knowledge, a transfer-function of the final assignment to \( \text{OUT} \) is forced to over-approximate that \( \text{OUT} \) could take on \( 2 \times 2 = 4 \) different values, which would in turn over-approximate the influence as 2 bits.

Greater accuracy can be achieved by tracking the actual set of values that each variable can take on, rather than only the size of the set. One implementation of such an approach is value-set analysis [2], which is a method for calculating memory-alias relationships in binary programs. Unfortunately, this approach is still forced to over-approximate. In this example, analysis of the if-then-else structure would determine that \( a \) and \( b \) can each take on the values 0x01 and 0x10. A transfer-function analysis of the final assignment would conclude that \( \text{OUT} \) can take on three different values: 0x01 & 0x01 = 0x01, 0x10 & 0x10 = 0x10, and 0x10 & 0x01 = 0x0. As a result, this approach would over-approximate the influence as 1.6 bits.

Example 3 in Section 4.2, in which \( \text{LOW} \) is added to a variable and later subtracted again, is another example of this type of problem. A transfer-function that analyzed each operation independently would conclude that the influence is non-zero, when in fact it is zero.

Because of these types of problems, transfer-function-based approaches are not able to compute a sound lower bound of information flow, and in practice often require manual annotations to compute a useful upper bound.

### 6.2 Our approach: end-to-end analysis

To avoid over-approximation, we analyze the end-to-end derivation of \( \text{OUT} \) as a whole, rather than analyzing each individual step along the way. Our high-level strategy is to soundly convert some or all of the program to a formula, and then use a decision procedure to reason about the range of \( \text{OUT} \), given the particular assignment of \( \text{HI} \). For programs with a finite number of possible execution paths, and given enough computation time, this approach can theoretically compute the exact influence with guaranteed accuracy. The challenge to this approach is to calculate useful bounds of the influence on real programs, in a reasonable amount of time.

#### 6.2.1 Converting the program to a formula

The first step is to generate a formula that accurately models the program, and which a decision procedure can reason about. We here briefly describe the techniques we use to generate such formulas. The details of these techniques are described in our previous work [1, 5, 19].

At a high level, we first convert some or all of the IA-32 binary program to an intermediate representation (IR) with a smaller instruction set, which makes all side-effects (such as setting and checking condition flags) explicit. If necessary, we convert the program to be loop-free by unrolling loops up to a maximum of some fixed number of times. Finally we compute the weakest precondition [13] over the program. Where we are unable to model the entire behavior of the program, guards are inserted to ensure soundness, effectively constraining the domain of \( \text{LOW} \) to those values which the formula can reason about with guaranteed accuracy.

Generating a formula that accurately models an entire binary program can be quite challenging. Indirect jumps make it difficult to statically determine all possible control flow paths. Modeling loops that could execute an unbounded number of times requires finding loop invariants, which is an open research problem. While system calls can be modeled statically, using a provided \( \text{HI} \) to specify auxiliary inputs, doing so requires significant implementation effort.

As in our previous work [5, 19], we address these problems by only modeling the execution paths we are able to analyze, and using guards to reject formula inputs that would execute an unmodeled execution path. For large programs, we currently model exactly one execution path - the path taken in an actual execution of the program. We leverage an execution trace obtained from the TEMU dynamic taint analysis tool [1, 14, 27] to greatly simplify the problem. The execution trace contains the address of each executed instruction, the instruction itself, the values of each operand of each instruction, and the taint attribute of each operand of each instruction.

The resulting formula accurately relates the program inputs to the program outputs, for inputs that would follow the same execution path. Thus, the formula domain is limited to such inputs, and contains guards to reject inputs outside of this domain. The formula is of the desired form: \( \mathcal{P}(\text{LOW}, \text{HI}) = \text{OUT} \). \( \text{HI} \) is obtained from the execution trace. \( \text{LOW} \) corresponds to inputs that were marked tainted in the execution trace. \( \text{OUT} \) may be an intermediate or final value of any program state, the value of program output, or any combination.

#### 6.2.2 Determine how many values \text{OUT} may take on

The next step is to find how many values \( \text{OUT} \) may take on. We are not aware of any existing tools that can solve this problem directly. We have developed some strategies for reasoning about how many values \( \text{OUT} \) may take on using
current decision procedures.

We first give the formula to the decision procedure. We then pose queries to the decision procedure, which consist of predicates over the free variables; in our case \( \text{LOW} \) and \( \text{OUT} \). The decision procedure responds to these queries either that the predicate is valid, indicating that it holds for all values of \( \text{LOW} \) and \( \text{OUT} \), or responds with a counterexample: an assignment to \( \text{LOW} \) and \( \text{OUT} \) that causes the predicate to be false.

Given this interface, we have developed the following query strategies:

- **Ask for examples of \( \text{OUT} \).** The most straight-forward technique is to simply query the decision procedure for a value of \( \text{OUT} \) that satisfies the formula, then query for another value of \( \text{OUT} \) that satisfies the formula and has not already been found, continuing to query the decision procedure either until no more values of \( \text{OUT} \) can be found (which will take many queries for high influence values), or until we have found enough values to establish that the influence is higher than some given threshold.

- **Positive range queries.** We expect that values that \( \text{OUT} \) may take on will often occur in contiguous ranges. Once we have found a value that \( \text{OUT} \) may take on, we can perform binary searches to establish the left and right boundaries of such a range. Queries posed to the decision procedure will be of the form “All values from proposed-left-boundary to proposed-right-boundary of \( \text{OUT} \) are satisfiable.” Each boundary can be found using a number of such queries less than the log of the size of the co-domain. Note that this type of query requires a universal quantifier, which is unsupported by many decision procedures.

- **Negative range queries.** Similarly, once we have established a value of \( \text{OUT} \) may not take on, we can perform a binary search to find the left and right boundaries of the encompassing contiguous range of values that \( \text{OUT} \) may not take on. Unlike the positive range query approach, this approach does not require universal quantifiers, allowing it to be used on more decision procedures.

- **Partitioning.** We can reason about parts of \( \text{OUT} \) independently to help establish an upper bound of influence. For example, if \( \text{OUT} \) is 32-bits, we can establish whether each individual bit can take on values of both 0 or 1 at most 64 queries. The influence of \( \text{OUT} \) as a whole can be no more than the number of bits that can take on both 0 and 1 values. Tighter bounds can be achieved at greater execution cost by using larger granularities, such as analyzing each byte instead of each bit.

- **Random sampling.** Another approach is to choose random values of \( \text{OUT} \), and query the decision procedure whether it is possible to satisfy the formula with each of those values. We can then use the fraction of these values that are satisfiable to estimate what fraction of values in the whole codomain of \( \mathcal{P} \) are satisfiable. This technique is useful when a significant fraction of the codomain of \( \mathcal{P} \) is satisfiable; i.e. when the influence is large. For example, when analyzing a potential overwrite attack, if the attacker has 30 bits of influence over a 32 bit \( \text{OUT} \), 25% of the codomain is satisfiable, and only a few samples are needed for a statistically significant result. However, when the influence is only a few bits, too many random samples would be needed to achieve a tight influence estimate, though we could still use this approach to set a probabilistic upper bound of influence.

We currently implement the strategies of asking for examples, and negative range queries. We first attempt to get up to some threshold \( t \) number of example values of \( \text{OUT} \). If the decision procedure is not able to find any more examples after finding \( t \) examples, then we are done, and the influence is exactly \( \log x \) with respect to the formula, and at least \( \log x \) with respect to the program. In cases where the formula is complete; i.e. models all relevant parts of the program; then the influence is exactly \( \log x \) with respect to the program.

If we find \( t \) examples, we stop asking for individual examples. At this point, we have established that the influence is at least \( \log t \) both with respect to the formula and with respect to the actual program. We next compute an upper bound using the negative range query strategy to find the lowest value \( \text{OUT} \) can take on \( v_l \), and the highest value \( \text{OUT} \) can take on \( v_h \). We then know that the influence is no more than \( \log(v_h - v_l) \).

### 7 Evaluation

We have implemented the method of calculating influence described in Section 6. We currently query for up to 64 values of \( \text{OUT} \), meaning that we find the exact influence when the influence is up to 6 bits \((6 = \log 64)\), and otherwise establish a sound lower bound of 6 bits of influence.

We first apply it to example programs from Section 4. Each of these programs was written as a C program and compiled using gcc. For these experiments we used 32-bit variables for \( \text{LOW} \) and \( \text{OUT} \) instead of 8-bit variables. We then use the tool on larger constructs known to cause problems for DTADI systems: a switch statement, and a case-conversion using the to upper function. Finally, we demonstrate the scalability and usefulness of our approach on two real programs: samba, and Microsoft SQL server. Using our influence measurement, we are able to verify that an alarm generated by the TEMU [1, 14, 27] DTADI system
alarm in samba is a false positive, and that an alarm in SQL server is a true positive.

7.1 Results

We summarize our results in Table 1. For each experiment we list the program or program-construct evaluated, and how many execution paths are accounted for in the formula. Where possible, we construct a formula including all paths. In these cases, both the lower and upper influence bounds are sound. In other cases, we model only the execution path taken in a given execution trace, as described in Section 6. We next list the time spent performing decision-procedure queries, the measured exact influence or influence bounds, and the lowest and highest value that OUT may take on. Finally, as a point of comparison, we list the actual influence as established by manual inspection.

7.1.1 Baseline experiments

The first two experiments are provided as a baseline reference. In the “No propagation” experiment, OUT does not depend on LOW at all. In the “Direct copy” experiment, LOW is simply copied to OUT. Our measured results are as expected: the influence is found to be exactly 0 in the first case, and between 6 and 32 in the latter case.

The next group of experiments are analogous to the examples from Section 4. In the table lookup test, each of the four bytes of LOW are masked with 0x0f and used as an index into a table with values 0x10 to 0x1f. For each of these experiments, we are able to calculate the exact influence or useful bounds of the influence within a few seconds.

7.1.2 Sanity checked data: switch statements

The gcc compiler, and probably many other compilers, compiles some switch statements to compute a pointer from the switch variable, and then use that pointer as an indirect jump target. Sanity checks ensure that this operation is safe, but this results in a false positive for taint analysis tools when the table lookup policy is enabled and the switch variable is tainted. We confirm that TEMU raises an alarm for this case. However, our influence measurement verifies that LOW’s actual influence over the indirect jump target is only a few bits.

7.1.3 Solving the taint analysis table lookup catch-22

As we described in Section 4, whether data loaded via a tainted pointer should be marked tainted is a configurable policy in most DTADI tools. In real programs, this typically happens when tainted data is used as an index into an untainted table. We next demonstrate that enabling the tablelookup policy can cause DTADI tools to have false positives, that disabling the table-lookup policy can cause them to have false negatives, and that the influence measurement can be used to accurately reason about these problematic cases.

Table-lookups are often used to convert data from one character set to another. As a result, disabling the table lookup propagation policy in DTADI tools can lead to false negatives: tainted data translated in such a way is marked as untainted. We evaluate the gnu libc toupper function as an example of such a translation. In this experiment, we translate each of the four bytes of LOW via toupper, and evaluate the taintedness and influence of the result. When collecting the execution trace for this experiment, we provide the input “aaaa”. As expected, when the table-lookup policy is disabled, TEMU marks the result as untainted. Our influence measurement confirms that the input has at least 6.1 bits of influence over the resulting value, and could have up to 28.6 bits of influence of the resulting value for the execution path examined. The actual influence is higher, due to the unanalyzed execution path where the input bytes are not lower case characters. Nonetheless, the measured influence bounds are sufficient to show that the result is heavily influenced by LOW.

Table-lookups can also be used to select from a small set of values, by restricting the index to a small set of values, or by having duplicate entries in the table. As a result, enabling the table lookup propagation policy in DTADI tools can lead to false positives. In particular, we have observed this to be the case in samba, which we evaluate in Section 7.1.4.

7.1.4 Real-world programs

We next use our influence measurement tool on two real-world programs.

Samba is an open-source implementation of the Windows SMB protocol. Samba uses data from a network request to calculate an index into a table of function pointers, which causes a false positive in TEMU when that function pointer is called. Using our influence measurement tool, we are able to verify that the sanity checks in the program make this operation safe: the input has only a few bits of influence over the function pointer. As a further verification step, we verified that all of the values that the function pointer can take on are within the code segment of the program.

Microsoft SQL server is a closed-source database, and was the target of the well known Blaster worm. Our tool verifies that the alarm generated by TEMU when SQL server is attacked by the Blaster exploit is a true positive. Specifically, we find that the input has at least 6 bits of influence over a return address, and could have as much as a full 32 bits of influence over the return address: i.e., total control. As far as we are aware, the true influence is indeed
32 bits.

8 Discussion and future work

8.1 Accounting for unknown $HI$

In Section 3.3, we showed that influence of $LOW$ over $OUT$ is equal to the maximum information flow, or channel capacity, from $LOW$ to $OUT$, when $HI$ is known. This assumes that the provider of the untrusted input $LOW$ (the potential attacker), knows the complete state of the rest of the program. This is a pessimistic assumption.

In cases where $HI$ is unknown, the influence of $LOW$ over $OUT$ does not change; $P$ still has the same range. However, the information flow from $LOW$ to $OUT$ may be less than the influence of $LOW$ over $OUT$. In practical terms, this comes about when $LOW$ can influence $OUT$ to take on different values, but some uncertainty remains about which value $OUT$ will take on for a given value of $LOW$.

A notable real-world example is the use of pointer encryption [8]. The idea in pointer encryption mechanisms is to store pointers in an encrypted form, and decrypt them just before dereferencing them. Hence, an attacker who is able to overwrite the encrypted pointer cannot predict the value of the unencrypted pointer, generally causing the program to crash when the pointer is unencrypted and dereferenced. If an overwrite vulnerability exists that allows an attacker to overwrite a 32 bit encrypted pointer, then the influence of $LOW$ over $OUT$ will be 32 bits. However, without some knowledge of the encryption key (which is part of $HI$), the maximum information flow from $LOW$ to $OUT$ is 0 bits.

In general, we believe that the difference between influence and channel capacity of $LOW$ over $OUT$ when $HI$ has some uncertainty can be considered a measure of the unpredictability of $LOW$’s influence over $OUT$. Further work is needed to investigate this relationship.

8.2 Improving performance and accuracy of DTADI systems

As we showed in Section 4, the inaccuracies of DTADI systems stem largely from manually generated, ad-hoc taint propagation policies, defined over one instruction at a time. We believe that these problems can be addressed by using the techniques presented in this work to automatically generate taint propagation policies, based on influence. In other words, we may be able to combine the advantages of our current end-to-end calculation approach with the performance advantages of the transfer-function-based approach described in Section 6.1.

The premise of this approach is to identify blocks of code, such as a function, that have a single entry point and single exit point. For each such block of code, the maximum influence (See Section 3.4.2) of each variable read could be computed for each variable written. When the DTADI system is about to enter one of these pre-computed code blocks at run-time, the summary can be used to determine what the taint value of each written variable should be when the block exits.

This approach could improve the accuracy of current DTADI systems, since interactions within the block, such as sanity checks, implicit flows, and arithmetic interactions, would be accounted for. If desired, this approach could also be used to propagate a quantitative or stratified taint attribute instead of a binary taint attribute, which would help keep track of cumulative effects between blocks, and allow for quantitative integrity policies (Section 5.1).

This approach can also improve the performance of DTADI systems, since the taint propagation summary for a block may be less expensive to execute than propagating a taint attribute for each instruction within the block.

There are, however, several challenges that must be addressed before this approach can be implemented. Some of these challenges, and potential solutions are:

- The code of the target program must be analyzed statically. Code that cannot be found or analyzed statically,
such as dynamically generated code, must still be instrumented at run-time (though these summaries can of course be saved for subsequent program runs).

- For our current influence-calculation techniques to work, we must be able to transform the code block to an equivalent loop-free program, and we must be able to resolve the set of possible targets of indirect jumps. An imperfect analysis may suffice though, using runtime guards to detect if a loop executes more times than the static analysis unrolled it, or if an indirect jump transfers control to an unaccounted-for destination.

- Execution of the block must be atomic, or equivalent to atomic. For example, suppose a pre-emptive thread scheduler transfers control to a different thread while a block is executing. The taint status of each variable is at that point not in a well-defined state. When control returns to the first thread, any assumptions made in the static analysis may have been invalidated. Note that this is only a problem if the threads share data; otherwise the block execution can be modeled as atomic. Some approaches to addressing this problem are to either force atomicity, e.g. by disabling interrupts, or to implement a recovery mechanism for when an unexpected control transfer occurs.

- We do not statically know which inputs to the block will have been influenced by LOW, and we need to account for all possible values of the uninfluenced inputs. Depending on the desired accuracy of the influence calculation, e.g. if we want a sound lower or upper bound, it is unclear how to statically account for all of the possible combinations in a scalable way.

Despite these challenges, we believe that this approach is a promising direction for improving the accuracy and performance of DTADI systems.

9 Conclusion

In this work we have proposed influence as a quantitative measure of how much control one variable has over another. We have shown that influence is a useful theoretical tool for reasoning about control. We have proposed and implemented an end-to-end technique for measuring influence in binary programs. We have used our influence measurement technique on a number of synthetic and real-world programs, demonstrating its usefulness and practicality.

We believe that influence can be used to greatly improve the state of using dynamic taint analysis to enforce data integrity policies. As a theoretical tool, it can be used to help reason about policies. As a practical tool, we have demonstrated that influence can be used to perform a deeper analysis of generated alerts, thus vetting false positives. We believe that our techniques can also be extended to supplement or replace the manually written taint propagation rules used in today’s DTADI systems with automatically generated propagation rules that improve the system’s performance and accuracy.

References


